

# Eliminating Sandwich Attacks with the Help of Game Theory

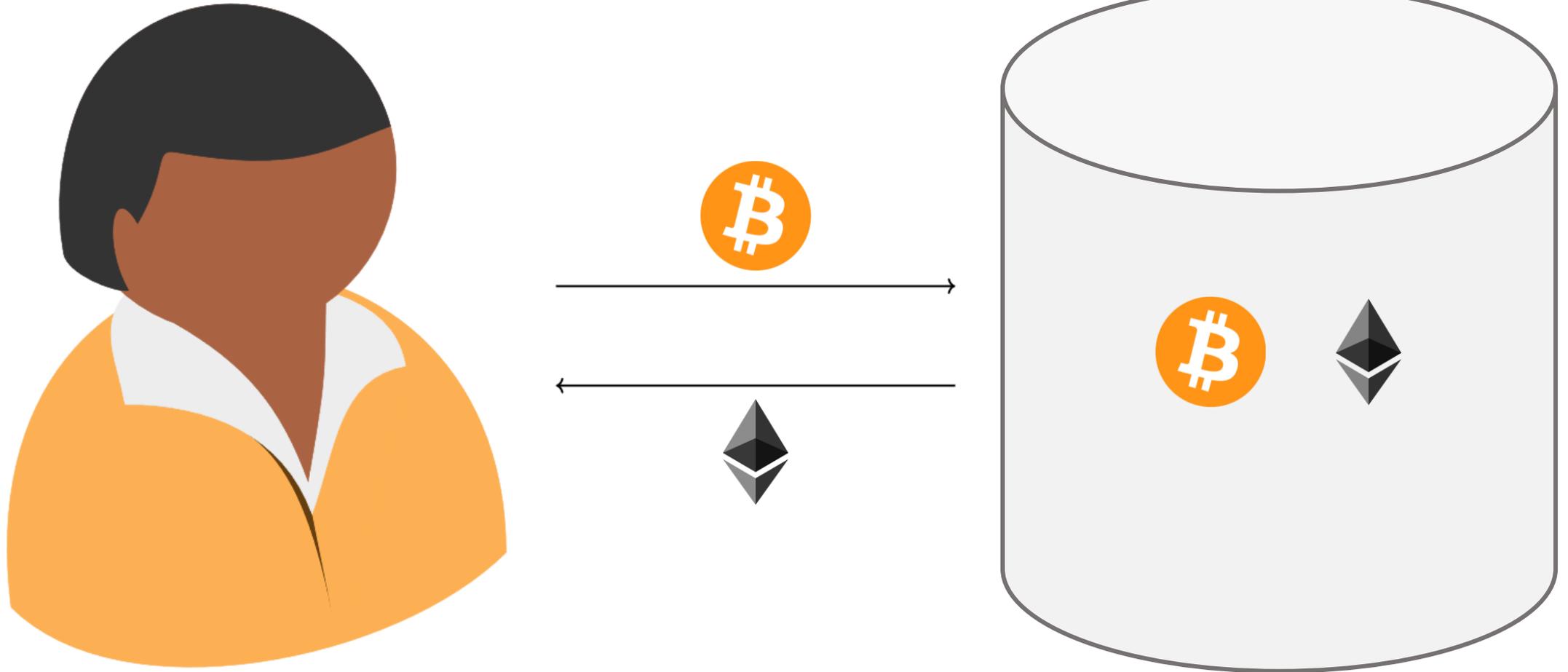


**Lioba Heimbach**, Roger Wattenhofer  
ETH Zurich – Distributed Computing – [www.disco.ethz.ch](http://www.disco.ethz.ch)

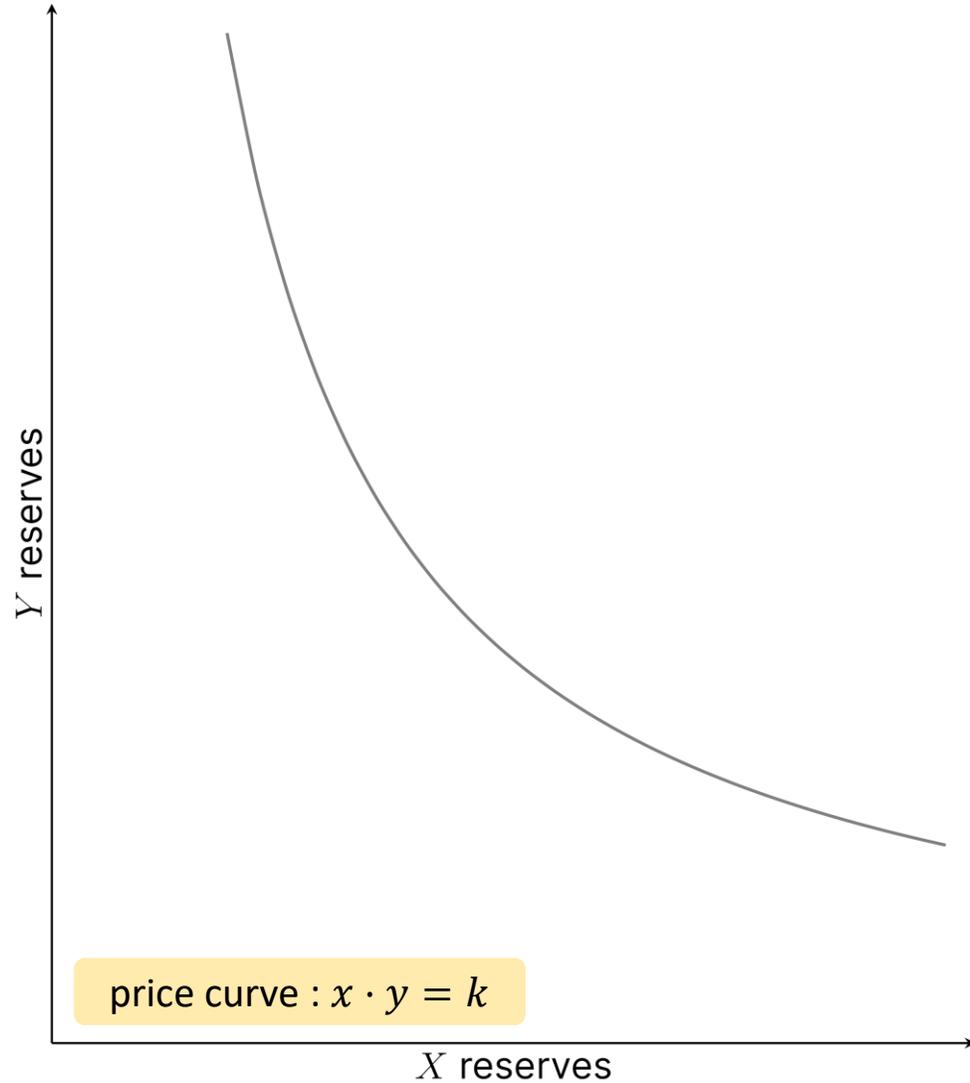
# Decentralized exchanges (DEXes)



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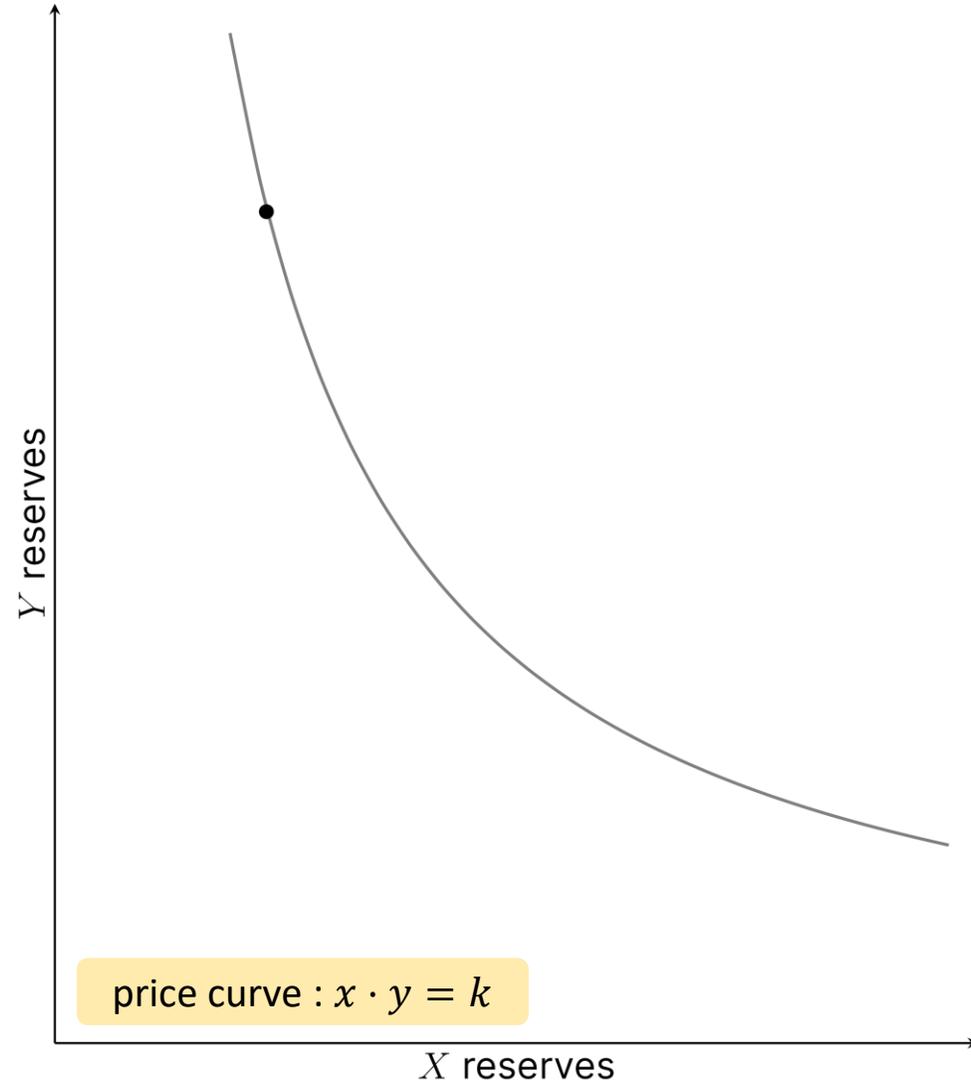


# Constant product market makers (CPMMs)



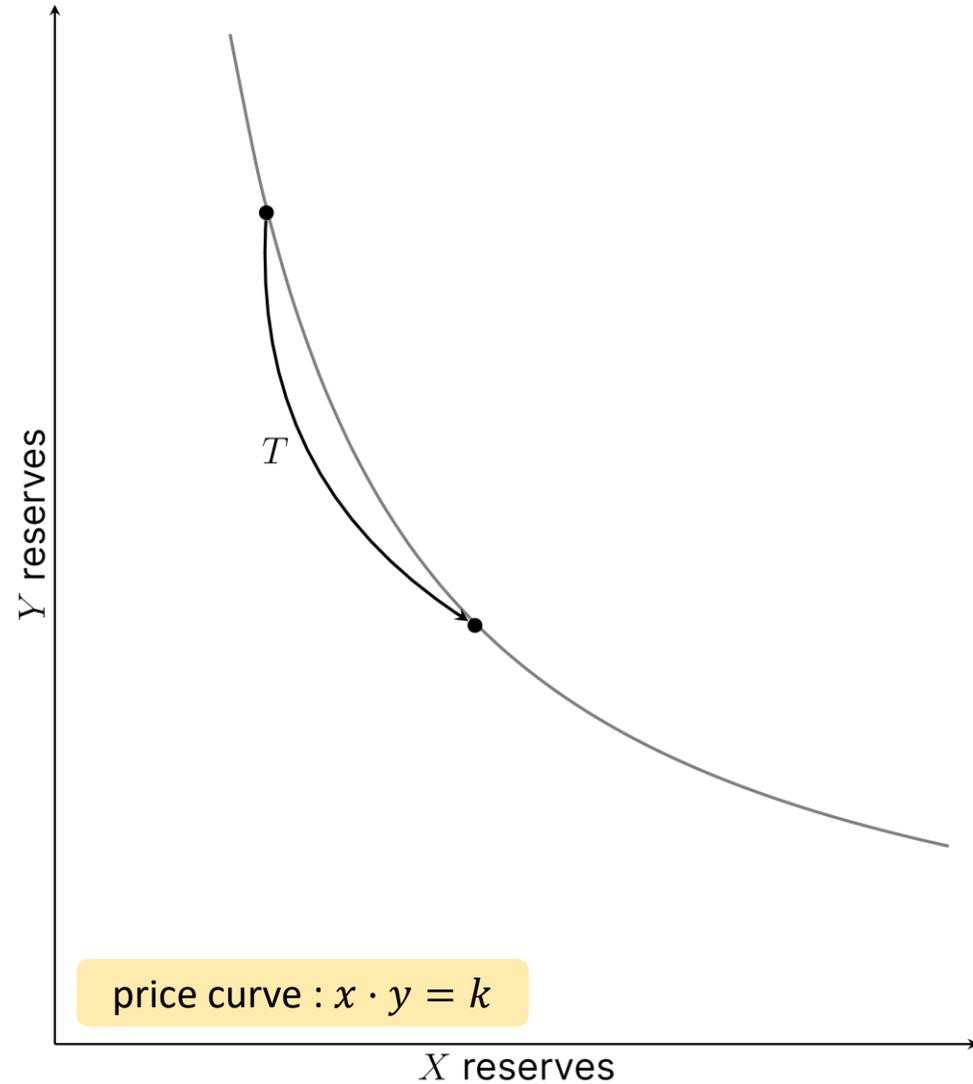
trading along price curve

# Constant product market makers (CPMMs)



trading along price curve

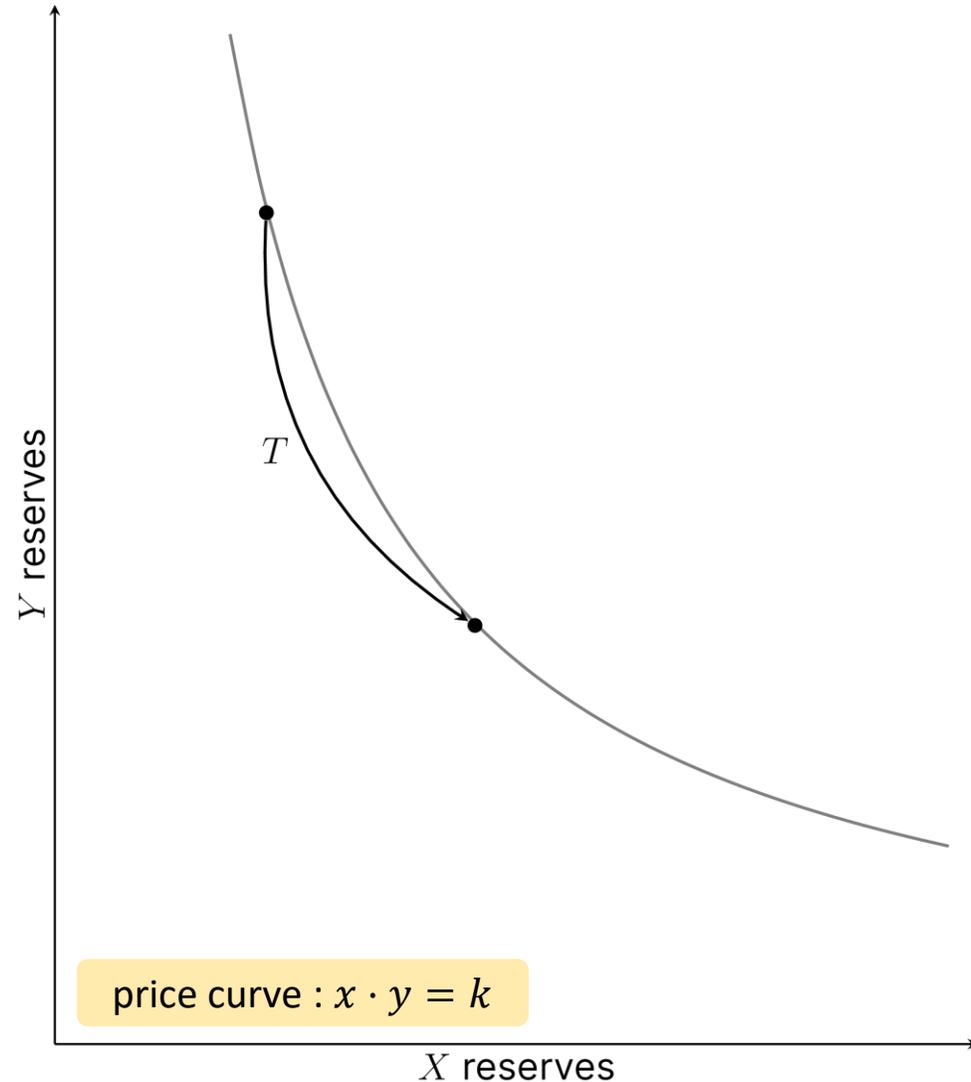
# Constant product market makers (CPMMs)



trading along price curve

$T$ : trade  $X \rightarrow Y$

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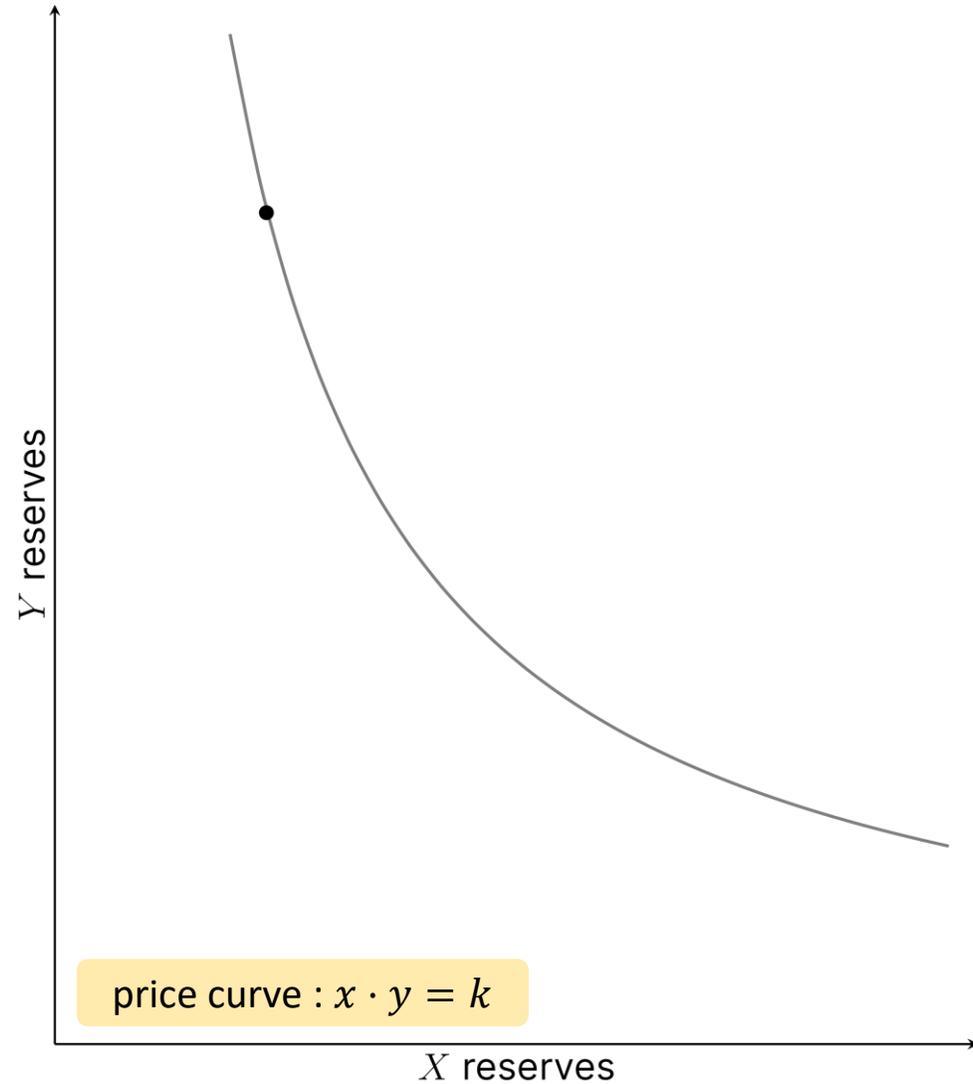


trading along price curve

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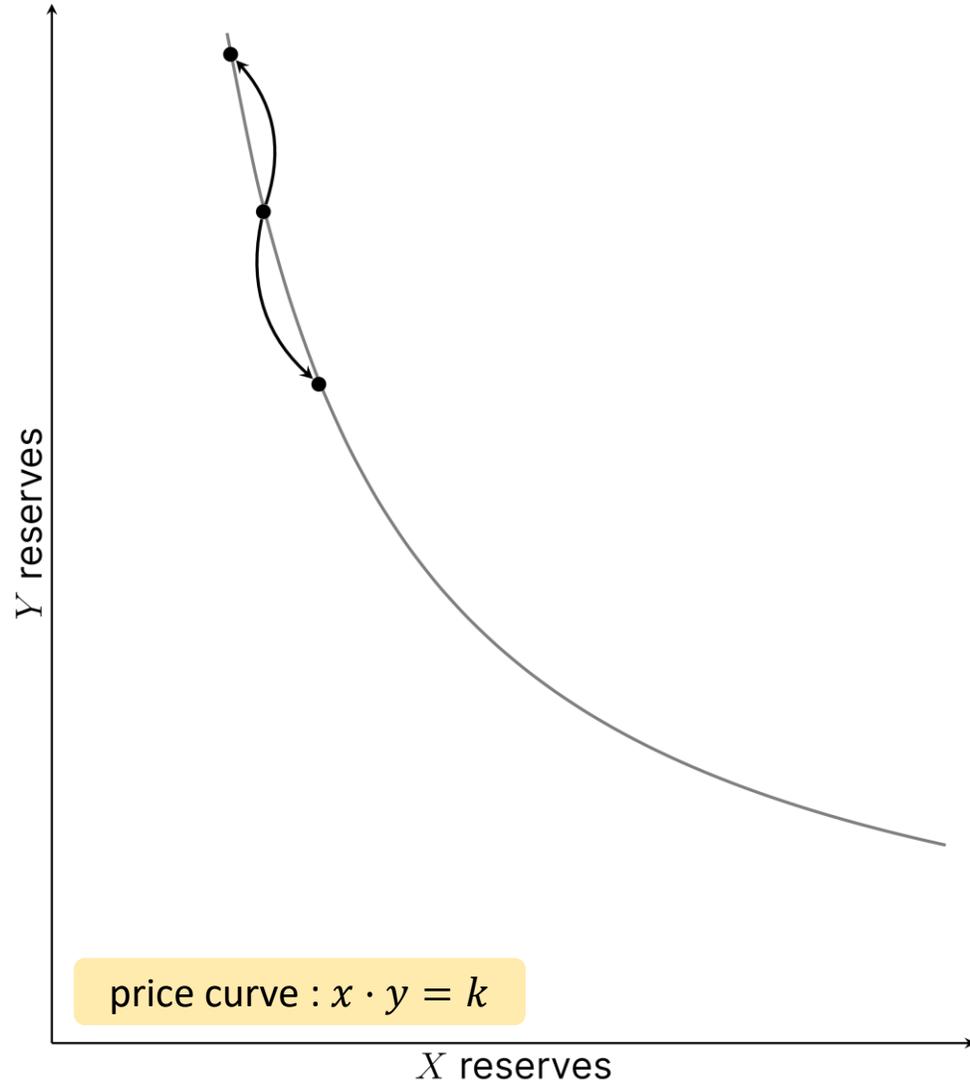
expected slippage  
=  
expected price decrease

# Unexpected slippage



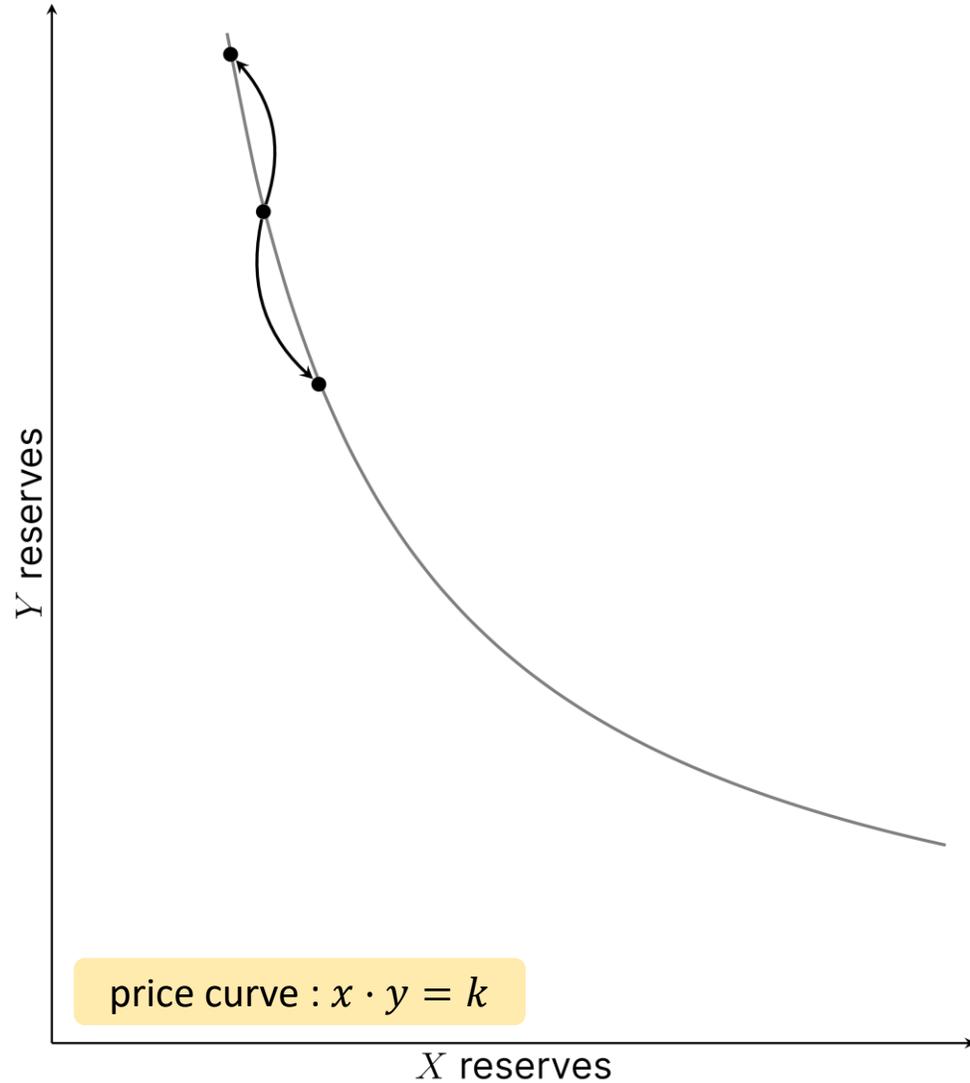
unexpected slippage  
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unexpected price increase/decrease

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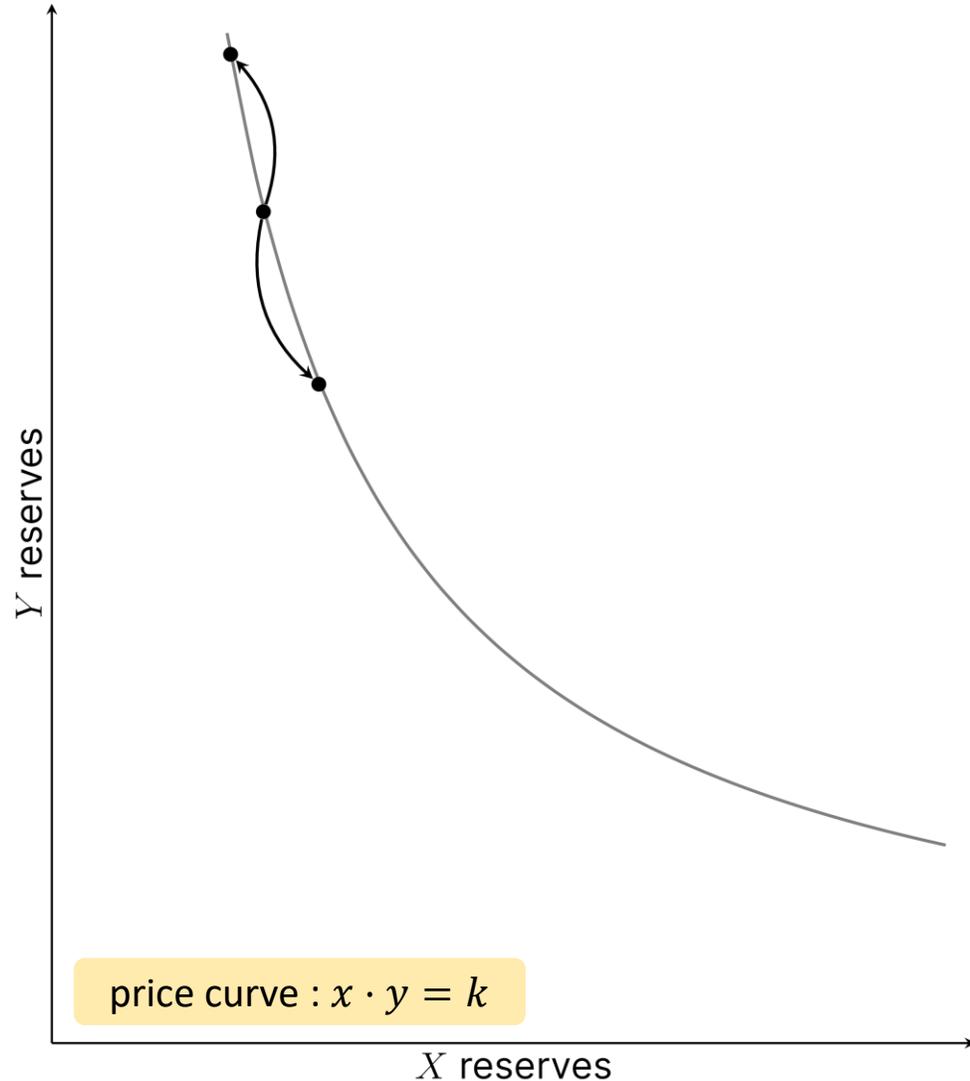
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unexpected slippage  
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unexpected price increase/decrease

slippage tolerance specifies  
maximum price movement

# Unexpected slippage

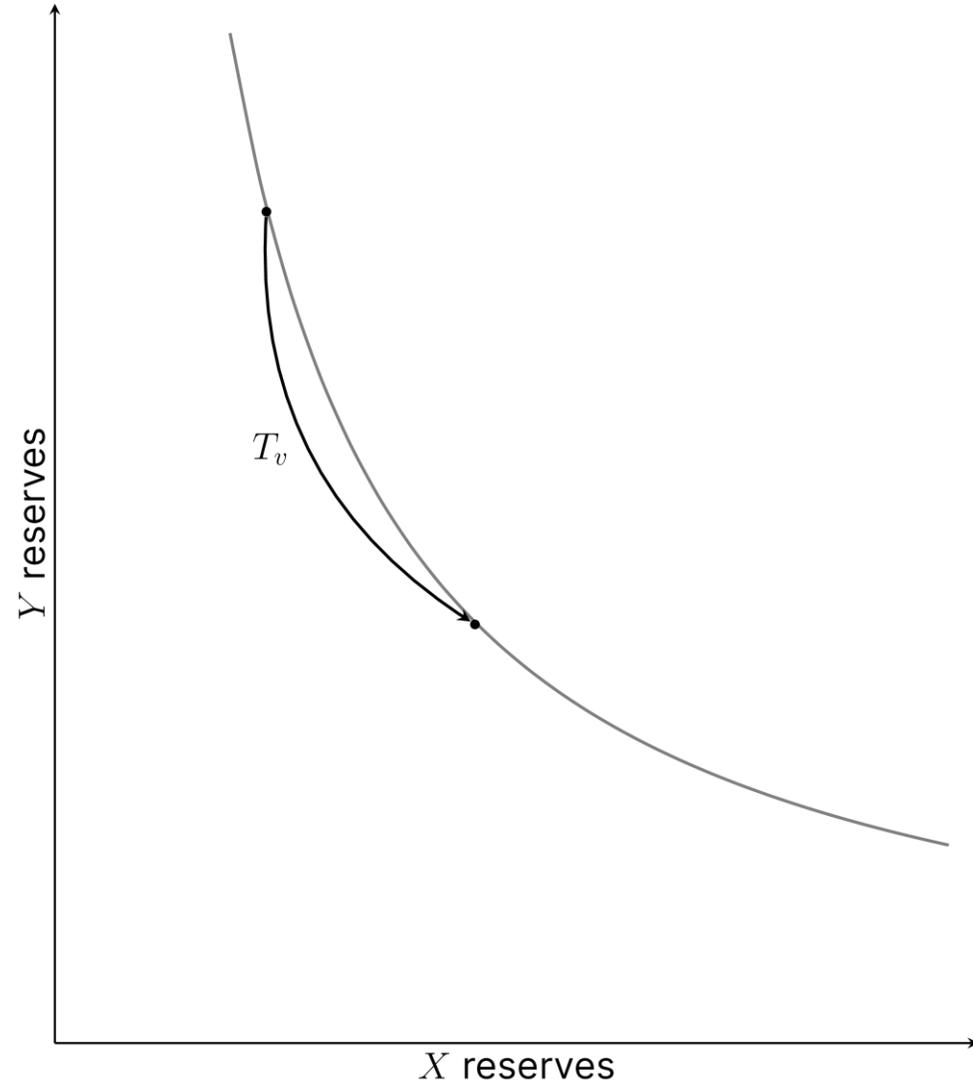


unexpected slippage  
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unexpected price increase/decrease

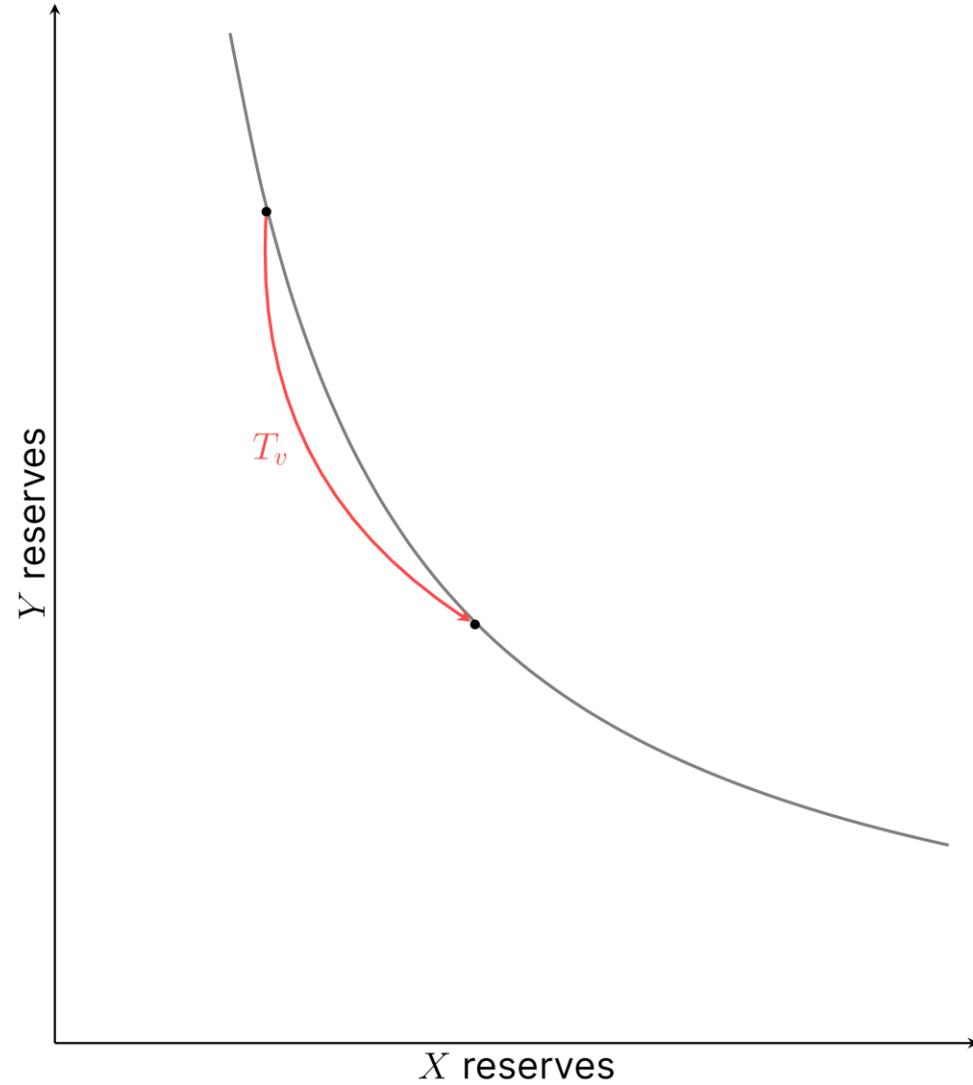
slippage tolerance specifies  
maximum price movement

trade fails if slippage  
tolerance exceeded

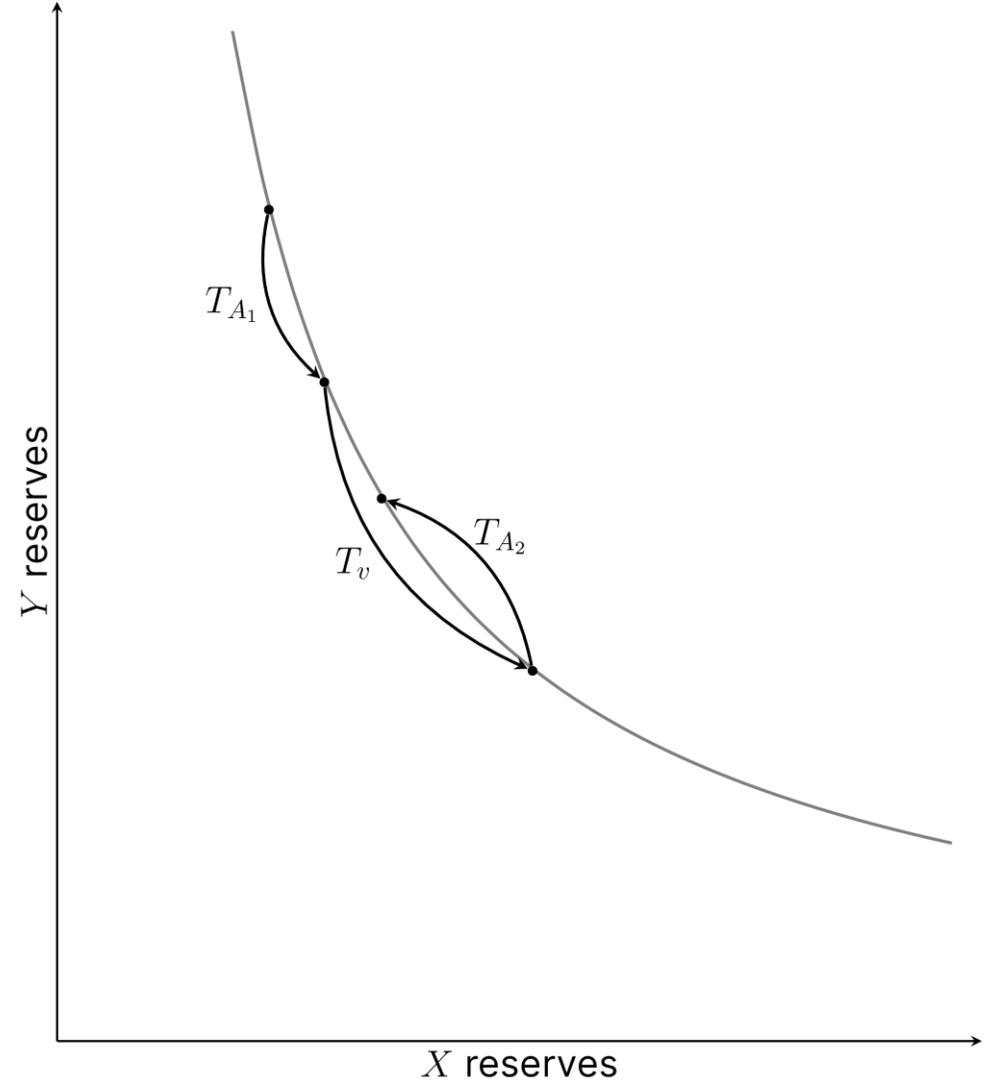
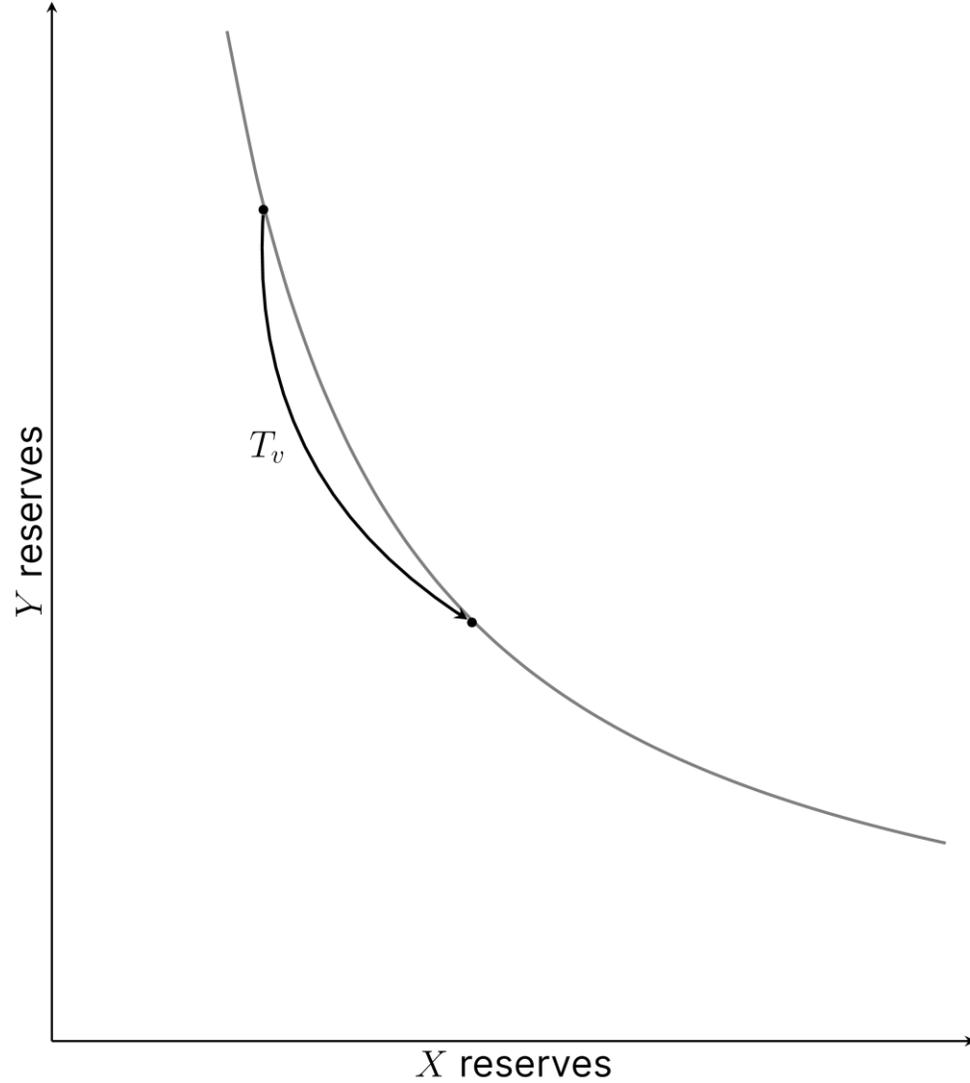
# Sandwich attack mechanism



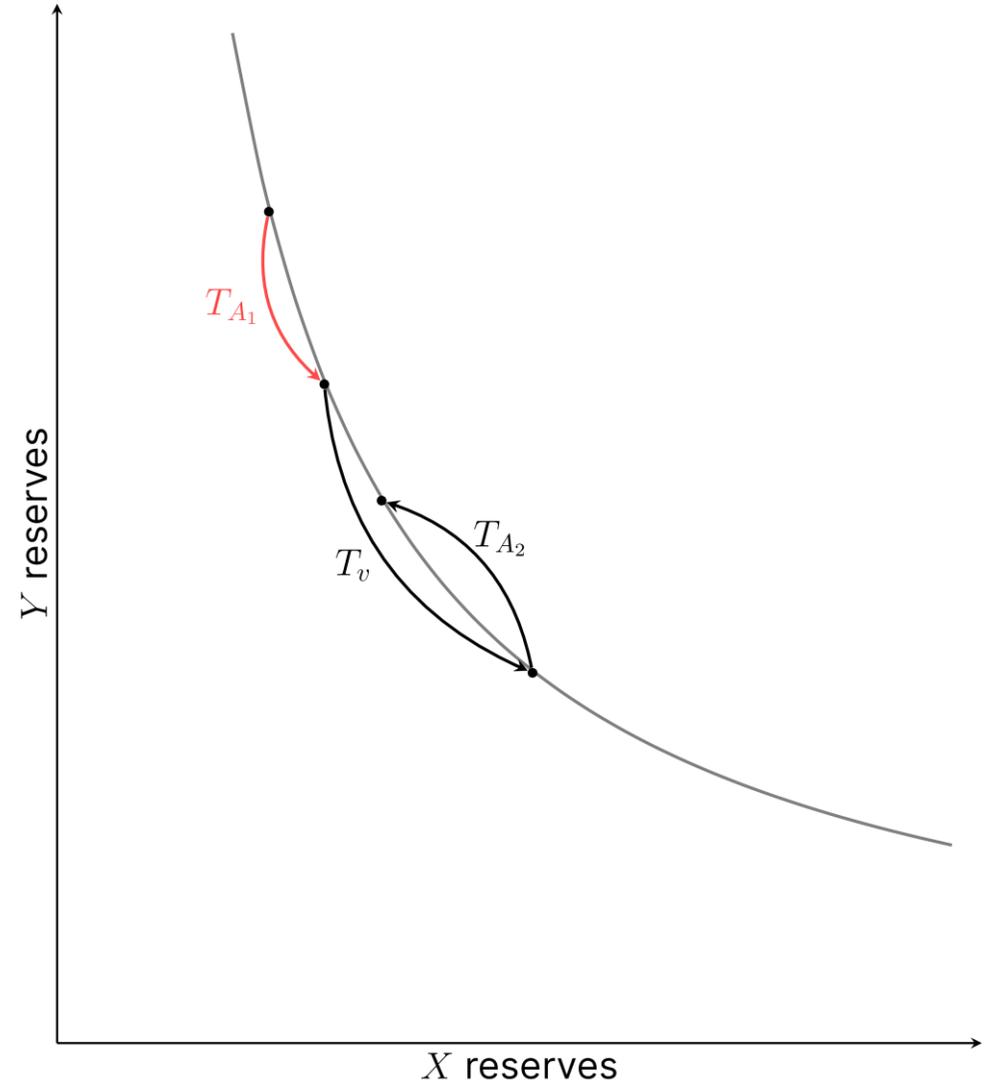
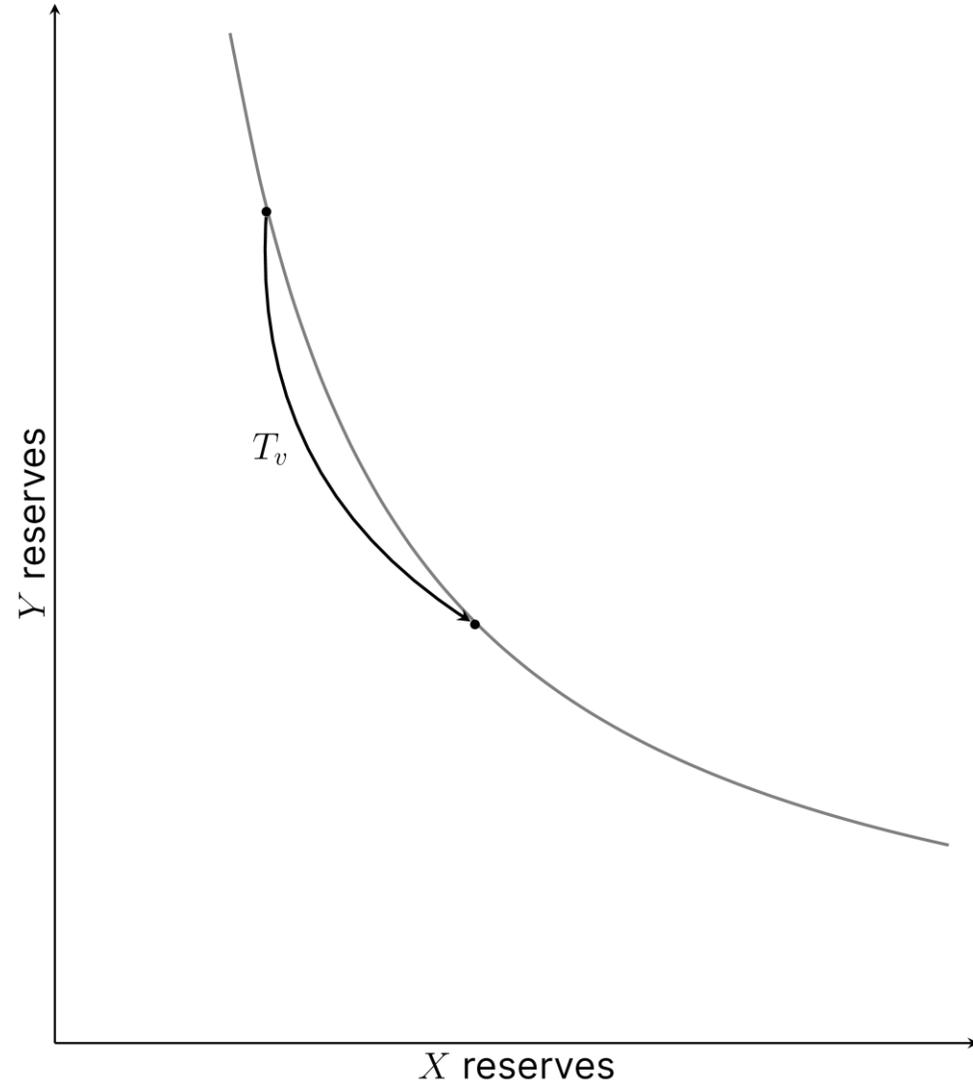
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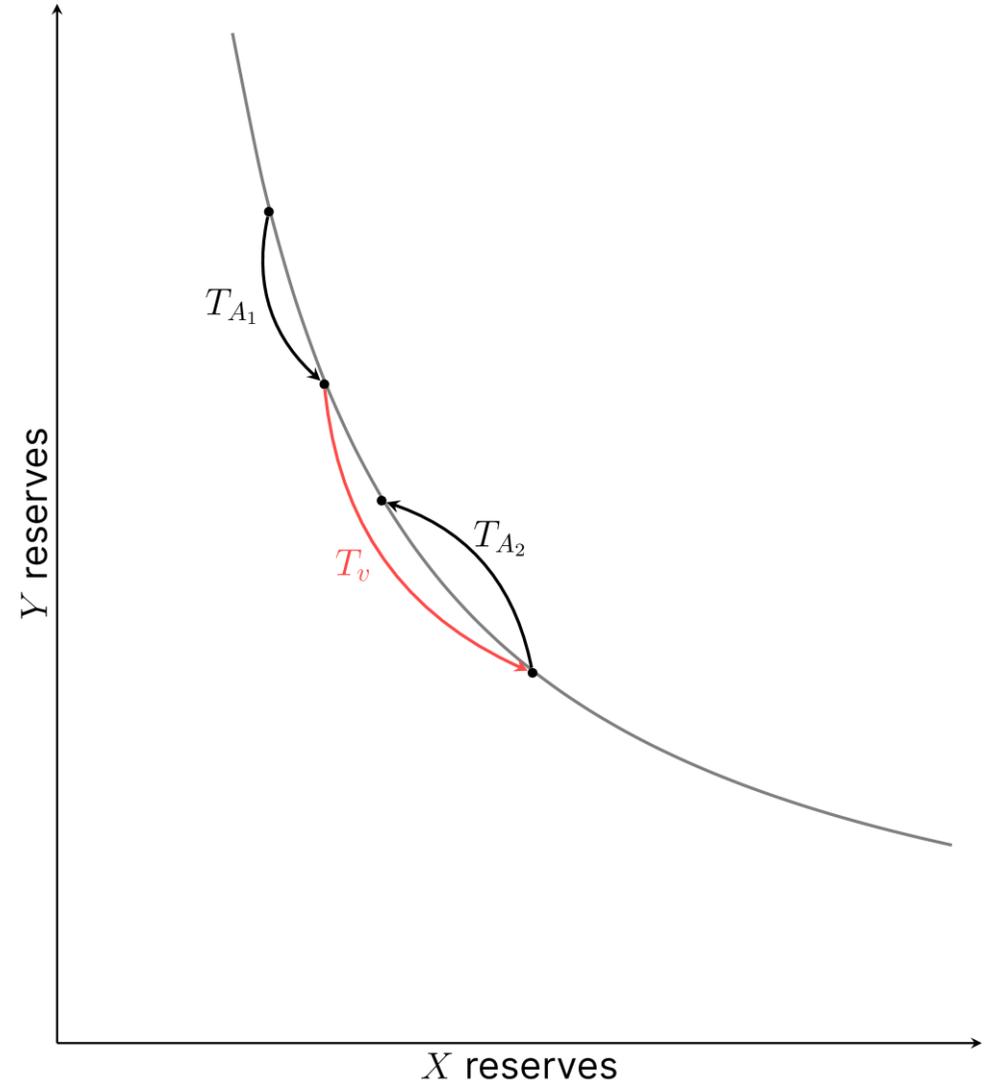
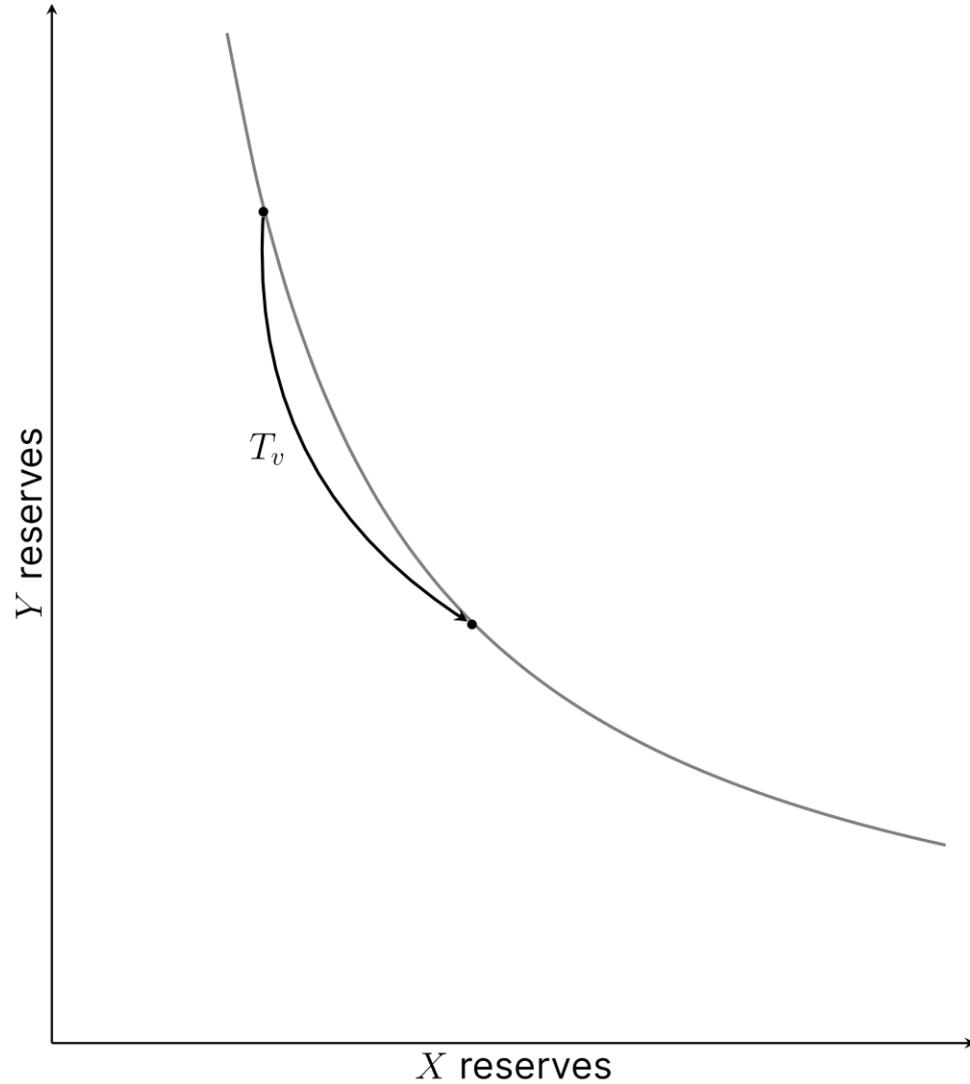
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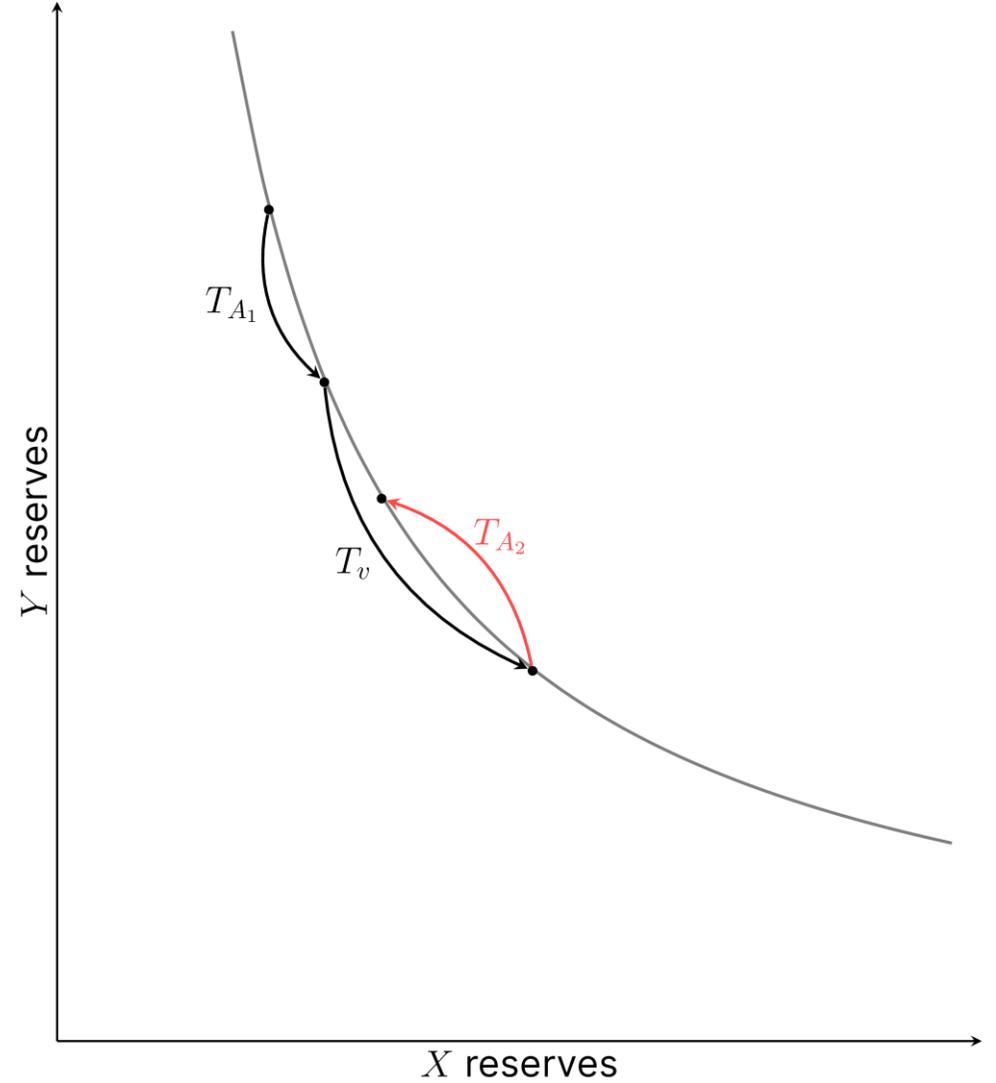
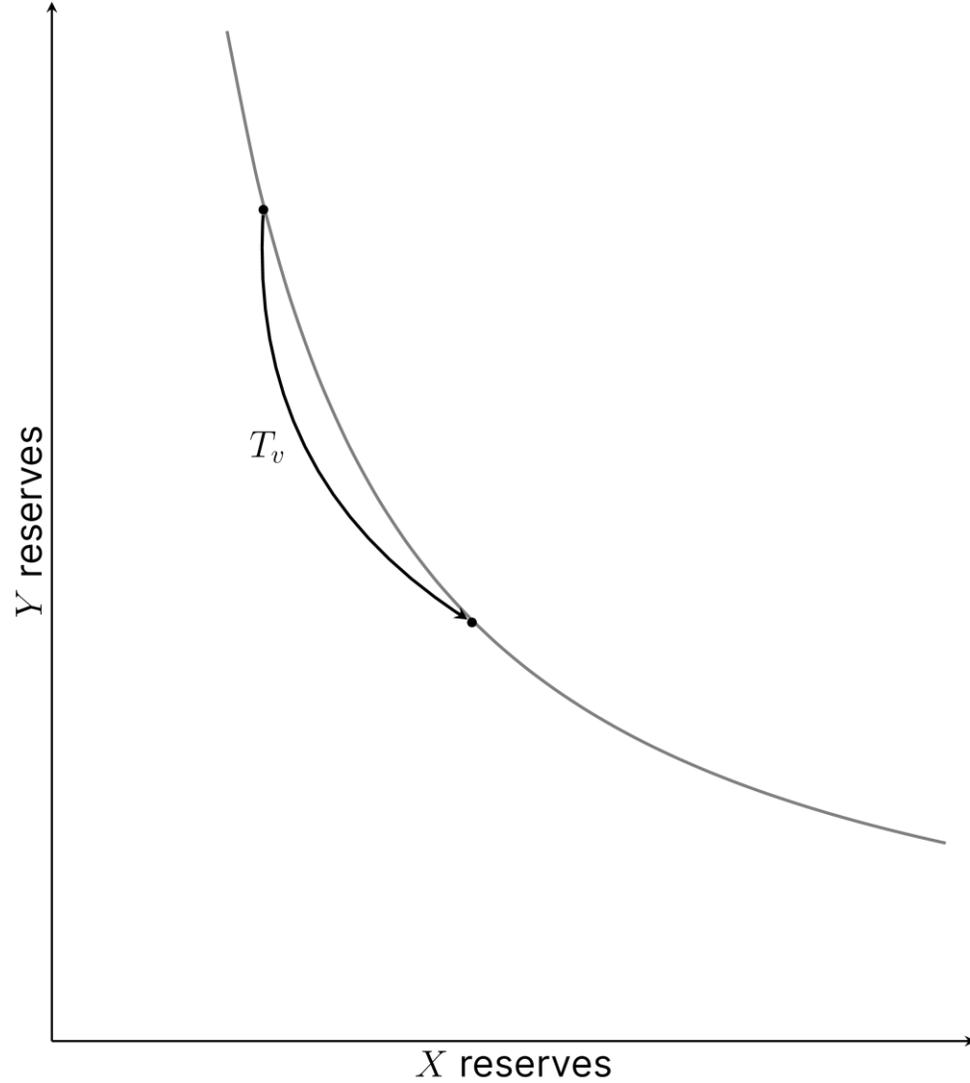
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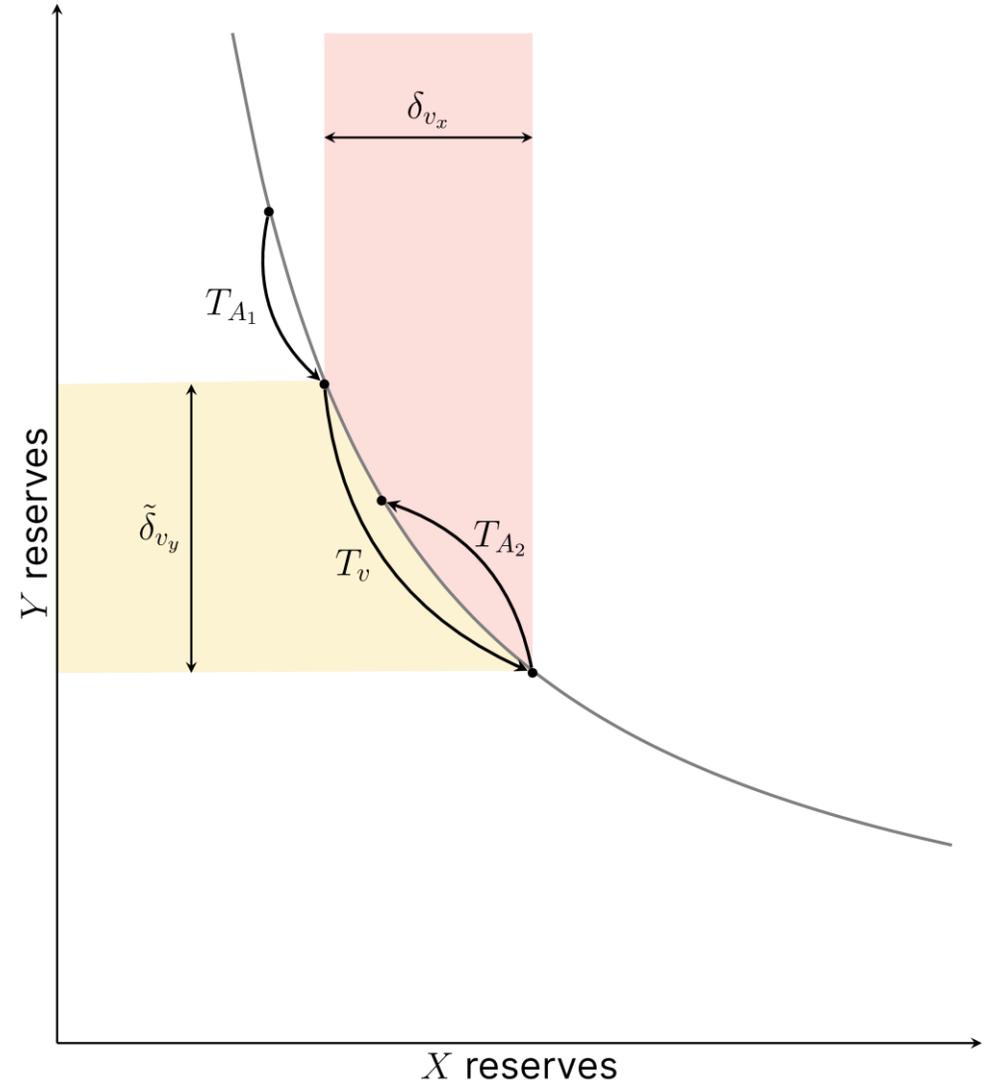
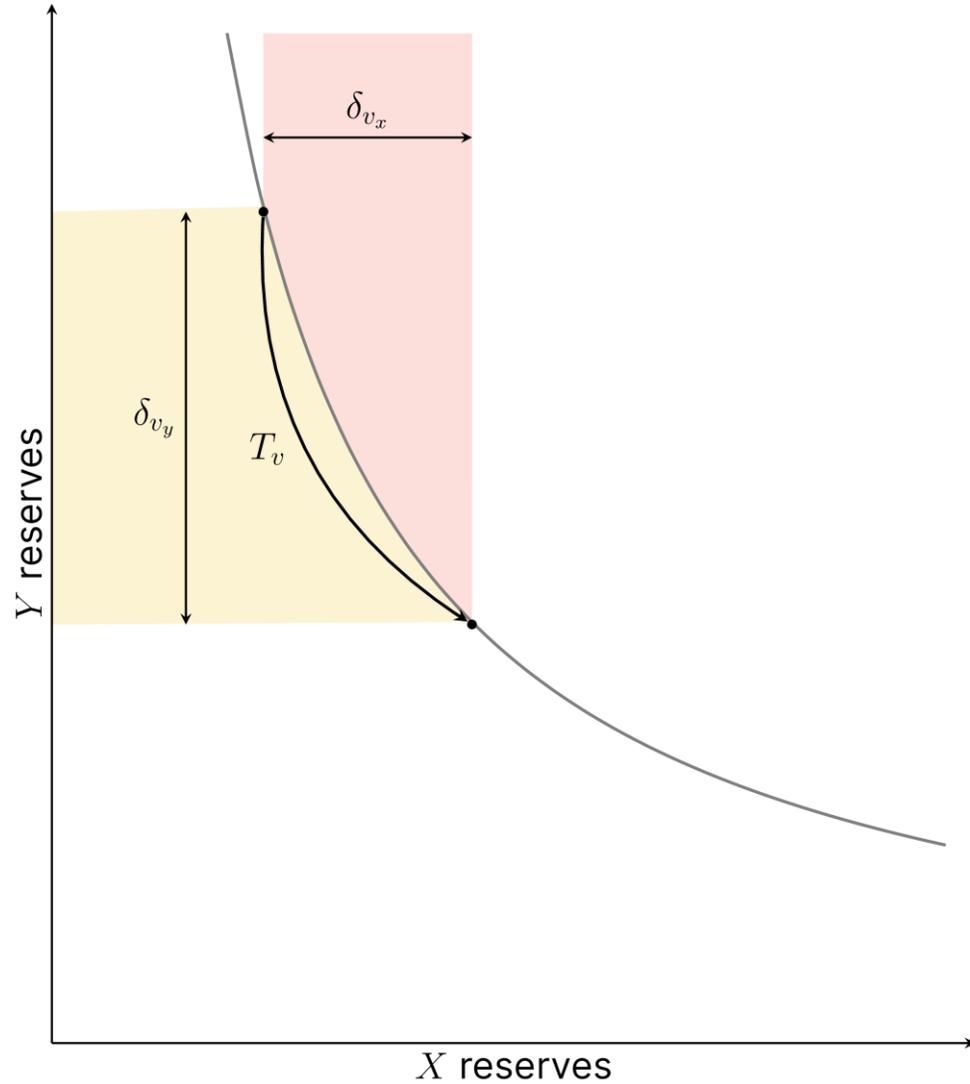
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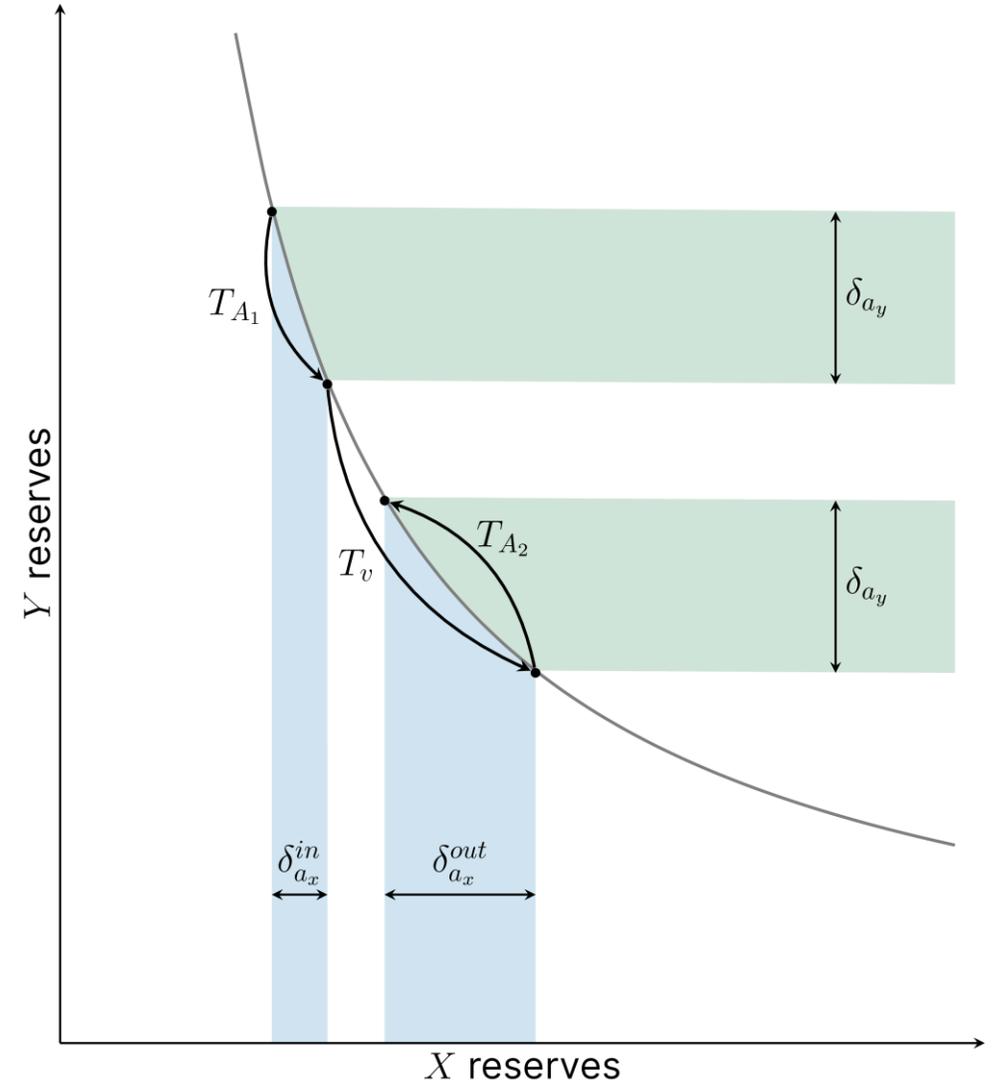
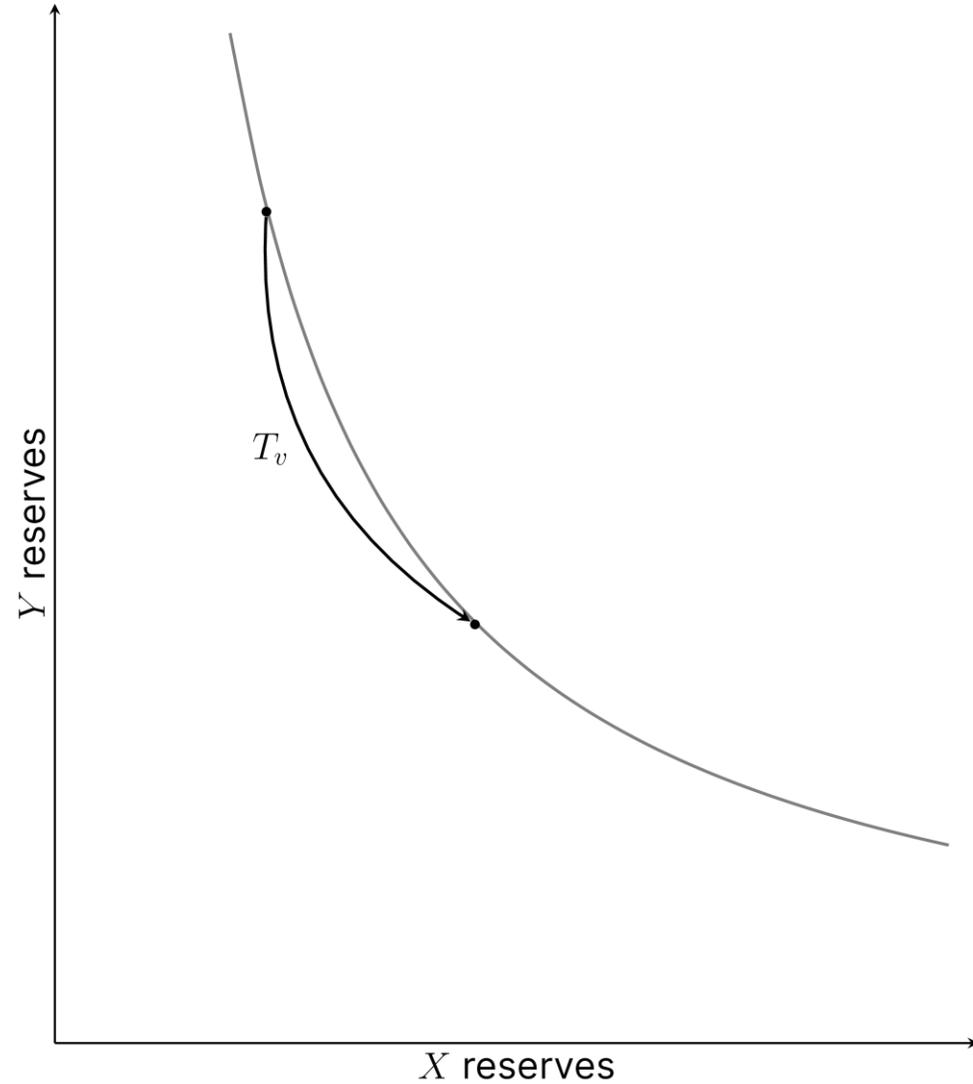
# Sandwich attack mechanism



# Sandwich attack mechanism



# Sandwich attack mechanism



# Sandwich attack game



# Optimal sandwich attack



# Optimal sandwich attack



maximize profit

# Optimal sandwich attack



# Optimal sandwich attack



victim transaction

# Optimal sandwich attack



victim transaction

transaction size ( $\delta_{v_x}$ )

# Optimal sandwich attack



victim transaction

transaction size ( $\delta_{v_x}$ )

slippage tolerance ( $s$ )

# Optimal sandwich attack



victim transaction

transaction size ( $\delta_{v_x}$ )

slippage tolerance ( $s$ )

attacker fees

# Optimal sandwich attack



victim transaction

transaction size ( $\delta_{v_x}$ )

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transaction fee ( $f$ )

# Optimal sandwich attack



victim transaction

transaction size ( $\delta_{v_x}$ )

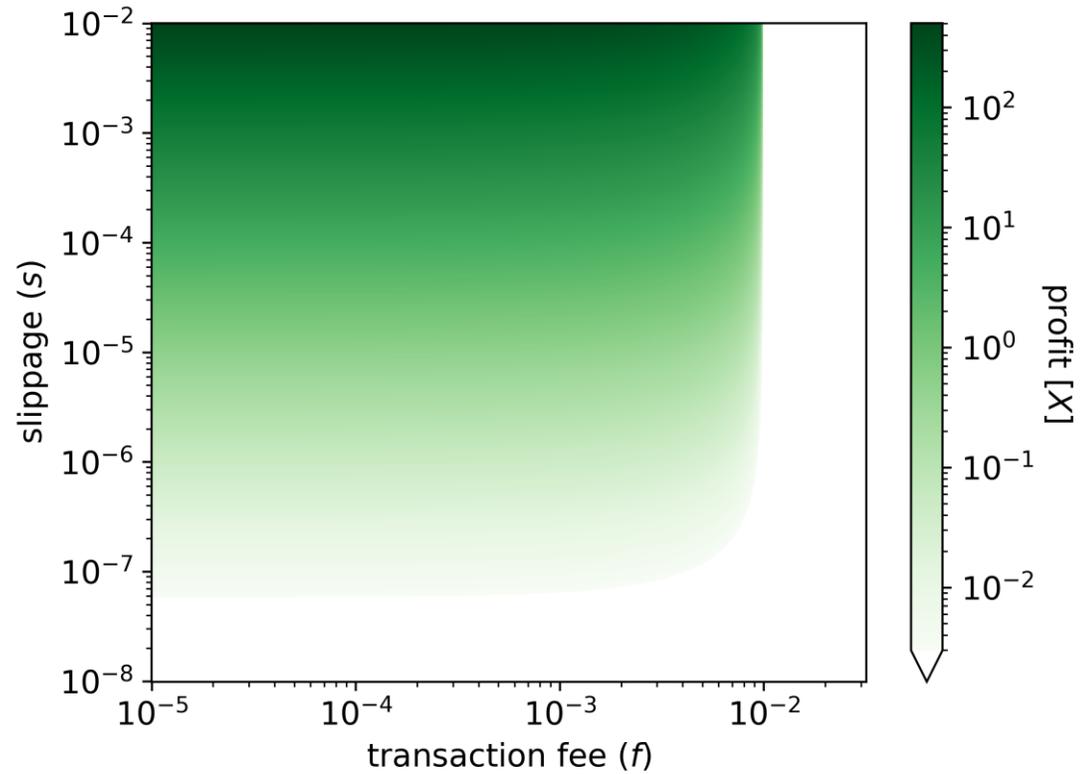
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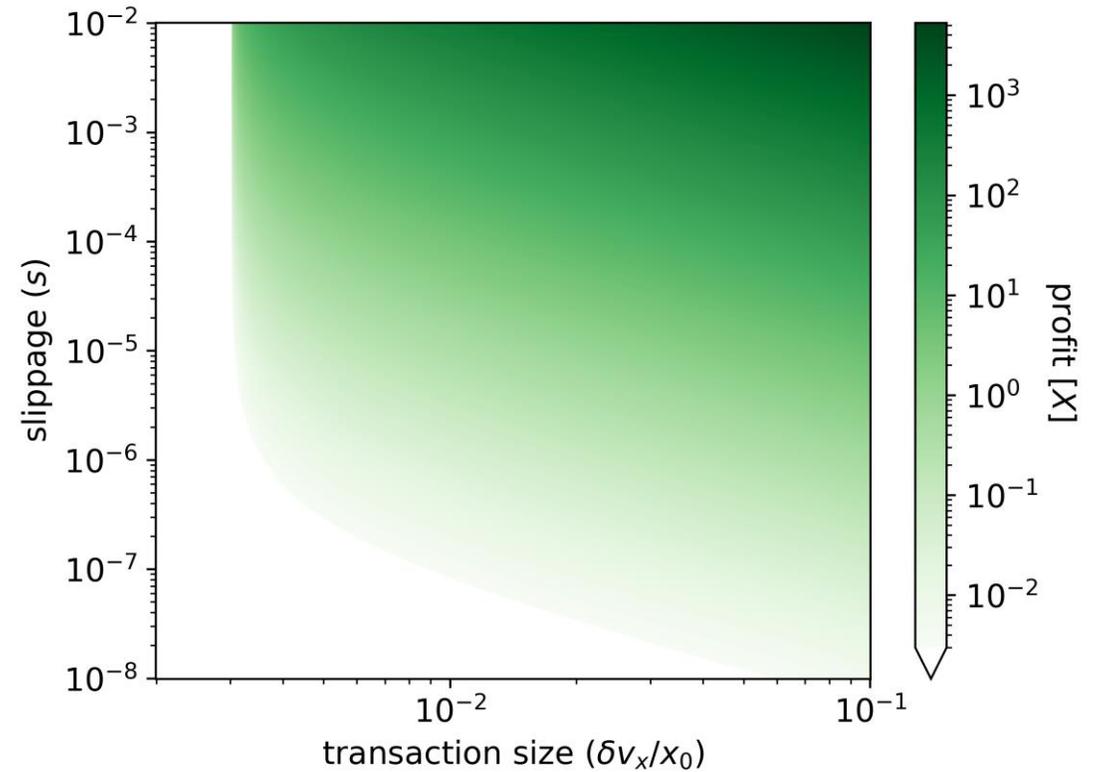
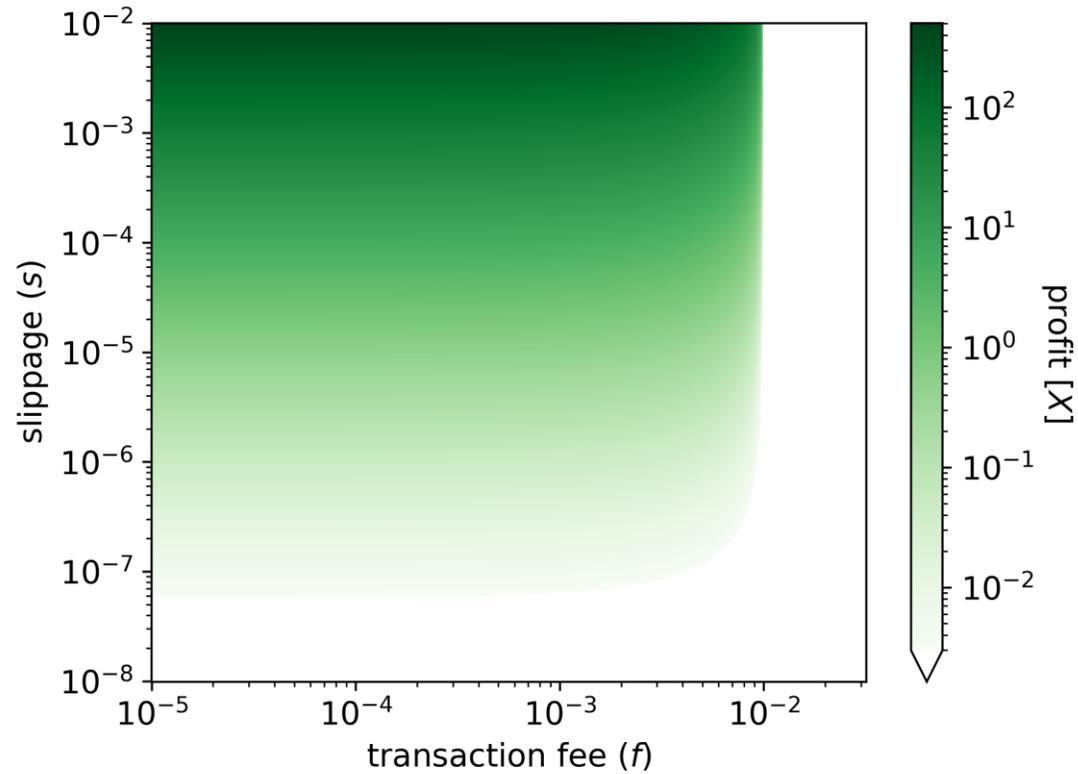
transaction fee ( $f$ )

block fee ( $b$ )

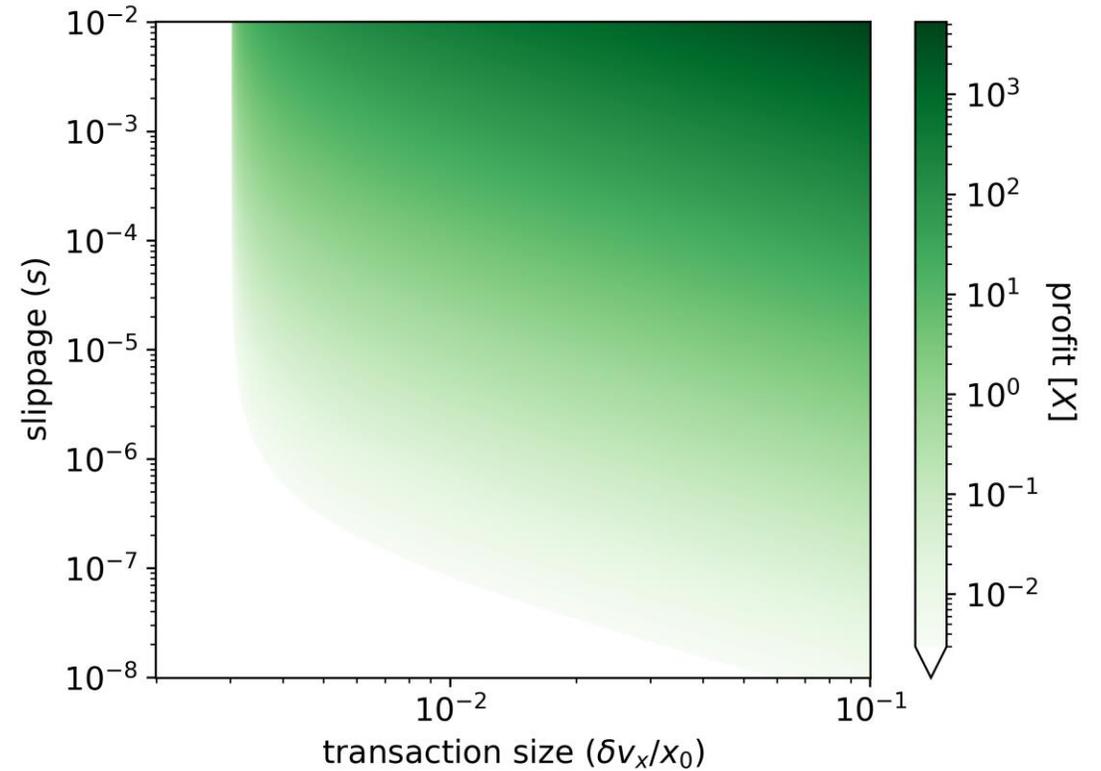
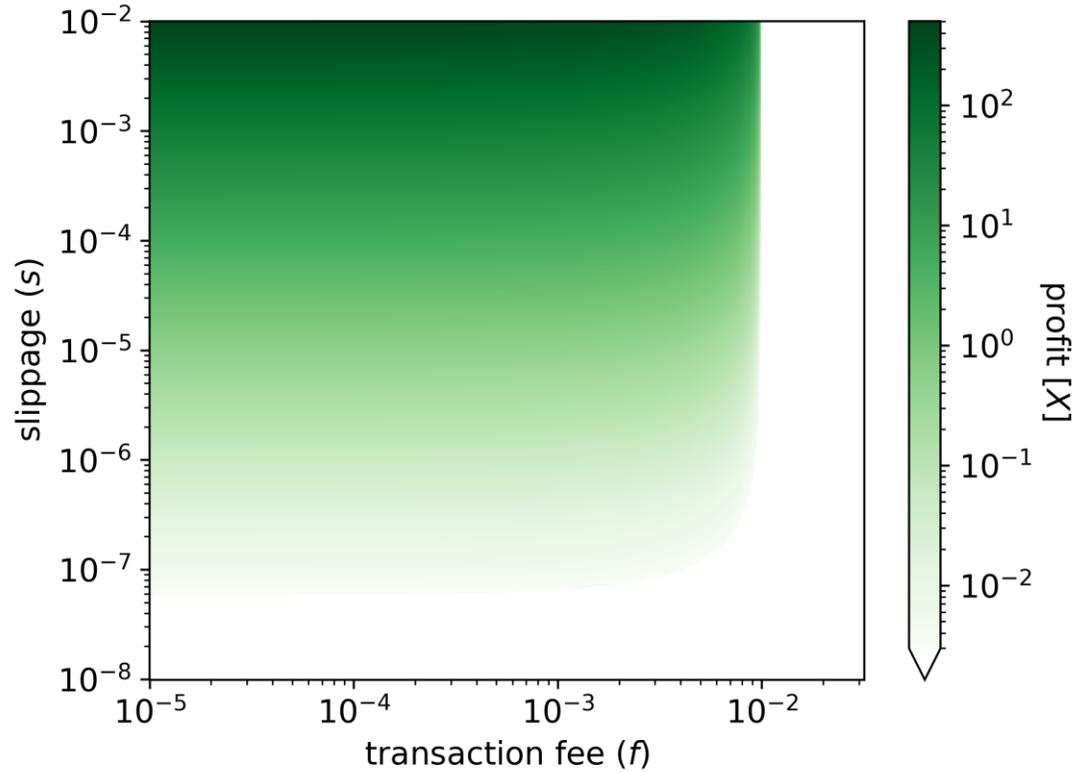
# Optimal sandwich attack



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# Optimal sandwich attack



the attacker's profit cannot exceed the victim's loss

# Setting slippage



# Setting slippage



avoid sandwich attack

# Setting slippage



avoid sandwich attack

avoid transaction failure

# Setting slippage



# Setting slippage



unattackable trade

# Setting slippage



unattackable trade

$s < s_a$  to ensure transaction is unattackable

# Setting slippage



unattackable trade

$s < s_a$  to ensure transaction is unattackable

expected transaction re-sending cost

# Setting slippage



unattackable trade

$s < s_a$  to ensure transaction is unattackable

expected transaction re-sending cost

$s_r < s$  expected transaction re-sending cost does not exceed sandwich attack cost

# Setting slippage



## setting slippage algorithm

Calculate  $s_a$  and  $s_r$

**if**  $s_r < s_a$ :

    set  $s = s_a - \varepsilon$ , where  $\varepsilon \rightarrow 0^+$

**else:**

    set  $s = s_r$

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# Cost comparison

## USDC ↔ ETH

size [\$]	fractional cost ours	fractional cost UNI	ratio cost UNI/ours
10	0,000	$2,267 \cdot 10^{-4}$	$\infty$
100	0,000	$3,545 \cdot 10^{-5}$	$\infty$
1000	$3,554 \cdot 10^{-6}$	$1,632 \cdot 10^{-5}$	4.5924
10000	$1,434 \cdot 10^{-4}$	$5,103 \cdot 10^{-3}$	35.5718
100000	$3,178 \cdot 10^{-4}$	$5,013 \cdot 10^{-3}$	15.7735

## BTC ↔ ETH

size [\$]	fractional cost ours	fractional cost UNI	ratio cost UNI/ours
10	0,000	$7,440 \cdot 10^{-5}$	$\infty$
100	$2,490 \cdot 10^{-6}$	$1,515 \cdot 10^{-5}$	6.0858
1000	$5,829 \cdot 10^{-6}$	$9,229 \cdot 10^{-6}$	1.5832
10000	$4,132 \cdot 10^{-5}$	$5,105 \cdot 10^{-3}$	123.5364
100000	$6,575 \cdot 10^{-5}$	$5,015 \cdot 10^{-3}$	76.2684

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1000	$2,086 \cdot 10^{-6}$	$6,381 \cdot 10^{-6}$	3.0588
10000	$2,612 \cdot 10^{-5}$	$5,101 \cdot 10^{-3}$	195.2647
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## LINK ↔ ETH

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10	0,000	$5,707 \cdot 10^{-5}$	$\infty$
100	$4,470 \cdot 10^{-6}$	$2,032 \cdot 10^{-5}$	4.5450
1000	$1,659 \cdot 10^{-5}$	$1,664 \cdot 10^{-5}$	1.0031
10000	$1,637 \cdot 10^{-5}$	$5,114 \cdot 10^{-3}$	312.3494
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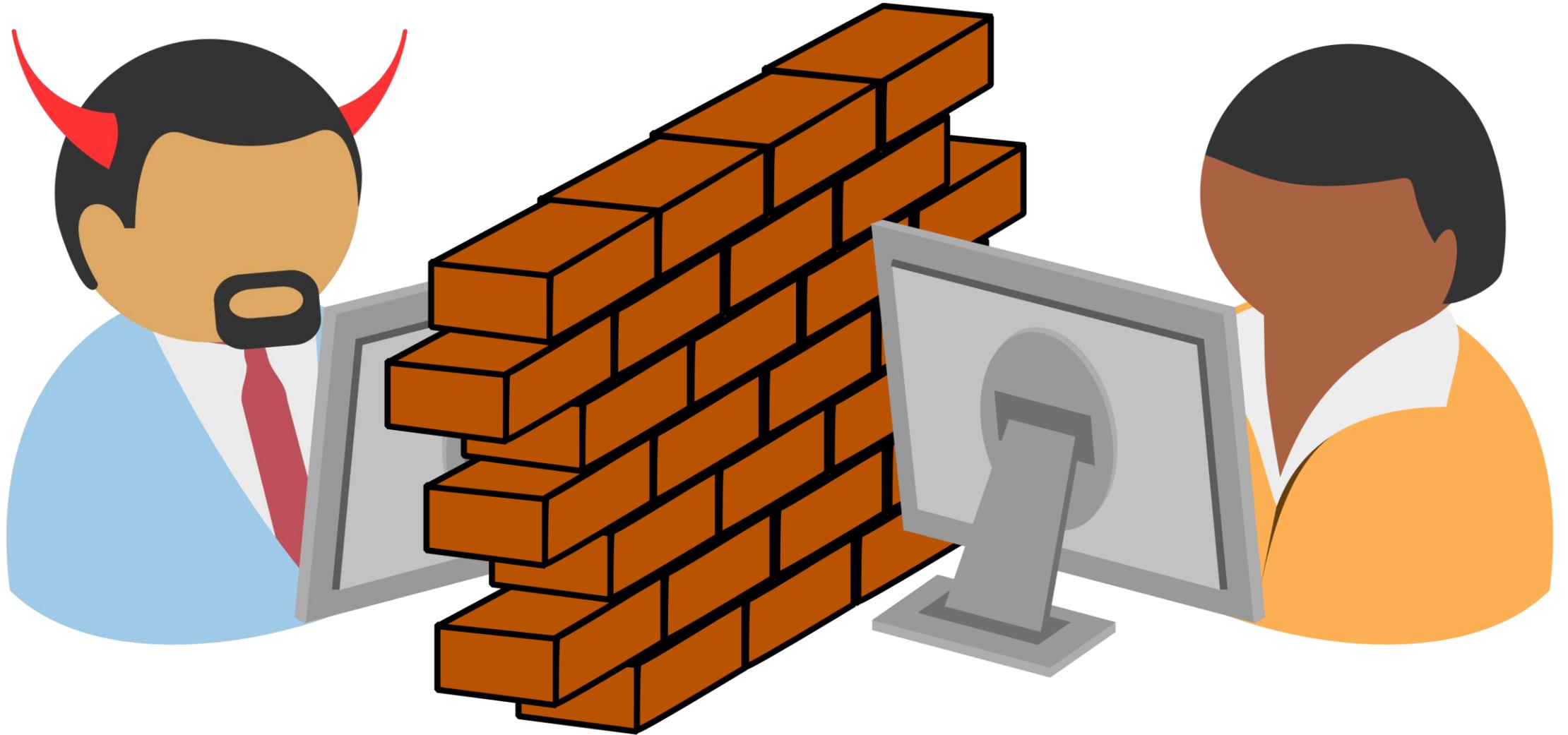
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# Conclusion



Thank You!  
Questions & Comments?



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# Setting slippage

unattackable transaction

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unattackable transaction

$$s \cdot \delta_{v_y} \geq 2b$$

# Setting slippage

unattackable transaction

$$s \cdot \delta_{v_y} \geq 2b$$

victim's maximum loss

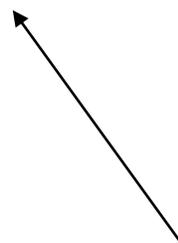


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unattackable transaction

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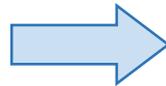
attacker's minimum costs



# Setting slippage

unattackable transaction

$$s \cdot \delta_{v_y} \geq 2b$$



$$s_a = \frac{2b}{\delta_{v_y}}$$

$s < s_a$  ensures that  
transaction is not attackable

# Setting slippage

expected transaction re-sending cost

$$\sum_{i=0}^{\infty} p(s, \delta_{v_x})^i \left( (l + m)b + E(s|\tilde{s} > s)\delta_{v_y} \right)$$

# Setting slippage

expected transaction re-sending cost

$$\sum_{i=0}^{\infty} p(s, \delta_{v_x})^i \left( (l + m)b + E(s|\tilde{s} > s)\delta_{v_y} \right)$$

transaction failure  
likelihood



# Setting slippage

expected transaction re-sending cost

$$\sum_{i=0}^{\infty} p(s, \delta_{v_x})^i \left( (l + m)b + E(s|\tilde{s} > s)\delta_{v_y} \right)$$

Ethereum transaction  
fee for re-sending



# Setting slippage

expected transaction re-sending cost

$$\sum_{i=0}^{\infty} p(s, \delta_{v_x})^i \left( (l + m)b + E(s|\tilde{s} > s)\delta_{v_y} \right)$$

expected price change



# Setting slippage

expected transaction re-sending cost

$$\sum_{i=0}^{\infty} p(s, \delta_{v_x})^i \left( (l + m)b + E(s|\tilde{s} > s)\delta_{v_y} \right)$$
$$= \frac{p(s, \delta_{v_x})}{1 - p(s, \delta_{v_x})} \left( (l + m)b + E(s|\tilde{s} > s)\delta_{v_y} \right)$$

# Setting slippage

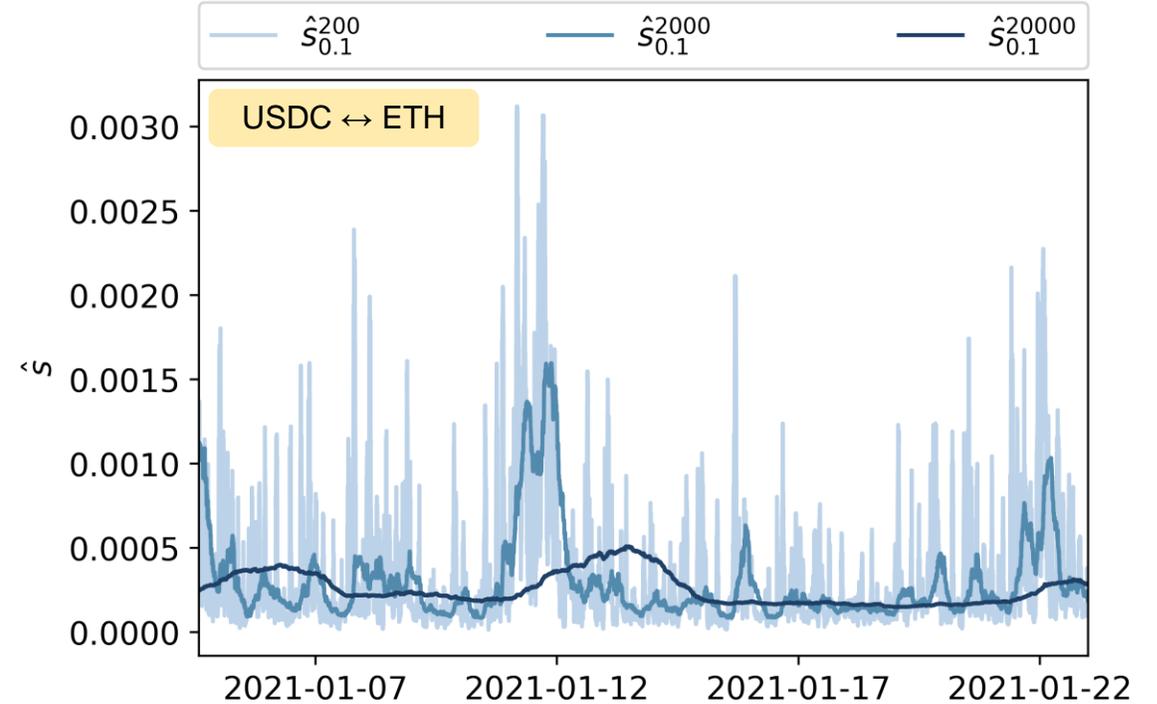
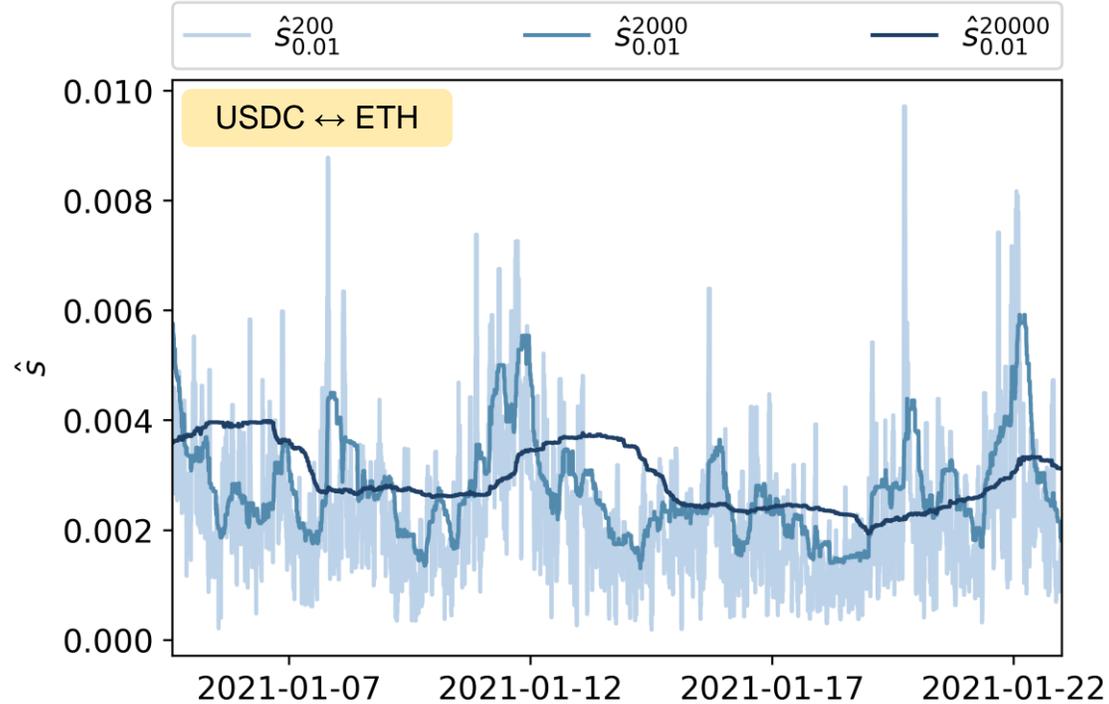
expected transaction re-sending cost

$$\sum_{i=0}^{\infty} p(s, \delta_{v_x})^i \left( (l + m)b + E(s|\tilde{s} > s)\delta_{v_y} \right) \quad \Rightarrow \quad s_r = \frac{p(s, \delta_{v_x})}{1 - p(s, \delta_{v_x})} \left( \frac{(l + m)b}{\delta_{v_y}} + E(s|\tilde{s} > s)\delta_{v_y} \right)$$
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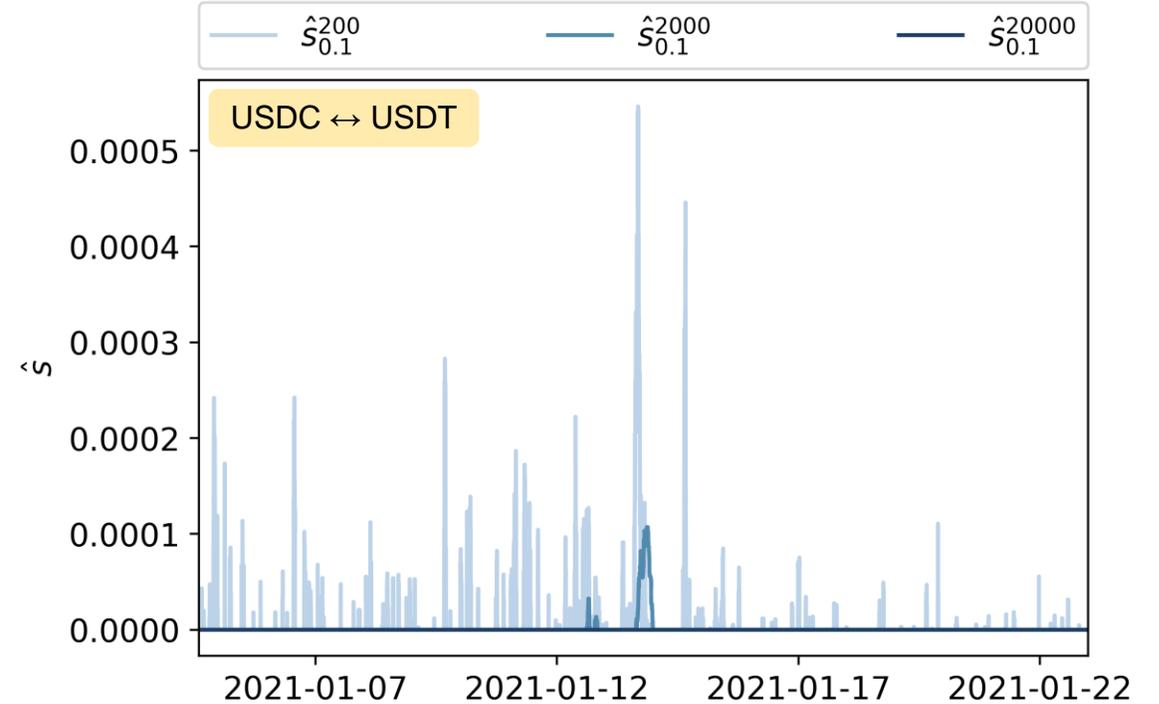
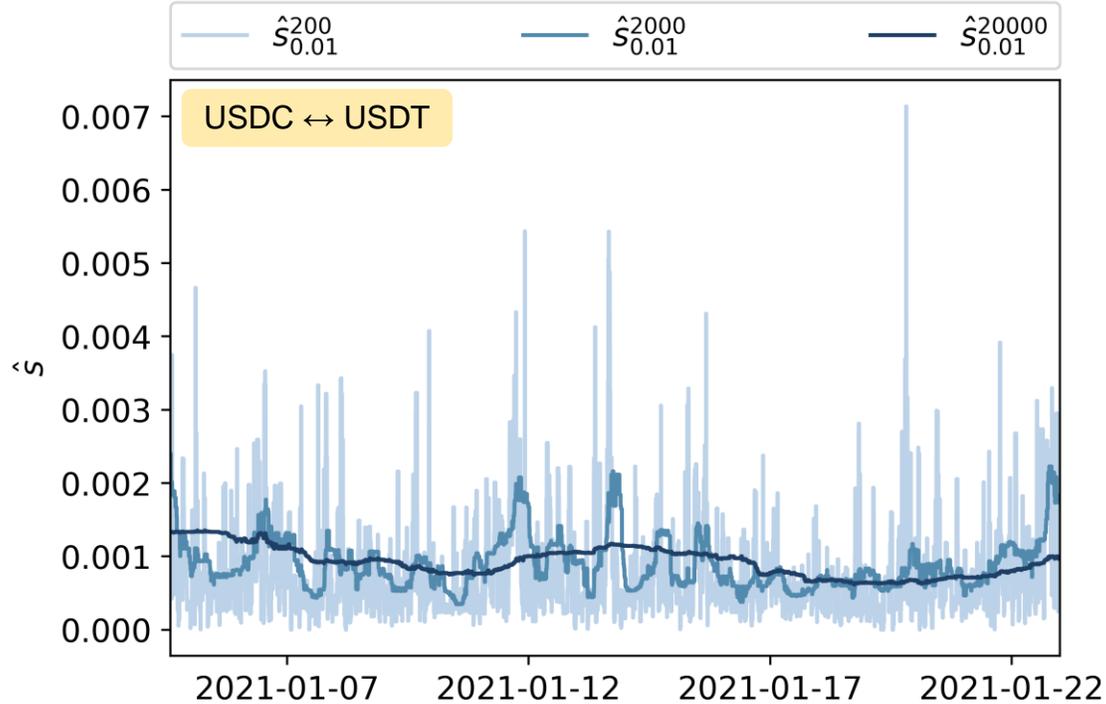
$s_r < s_a$  expected transaction re-sending cost does not exceed sandwich attack cost

Computing lower bound for slippage  
tolerance ( $s_r$ )

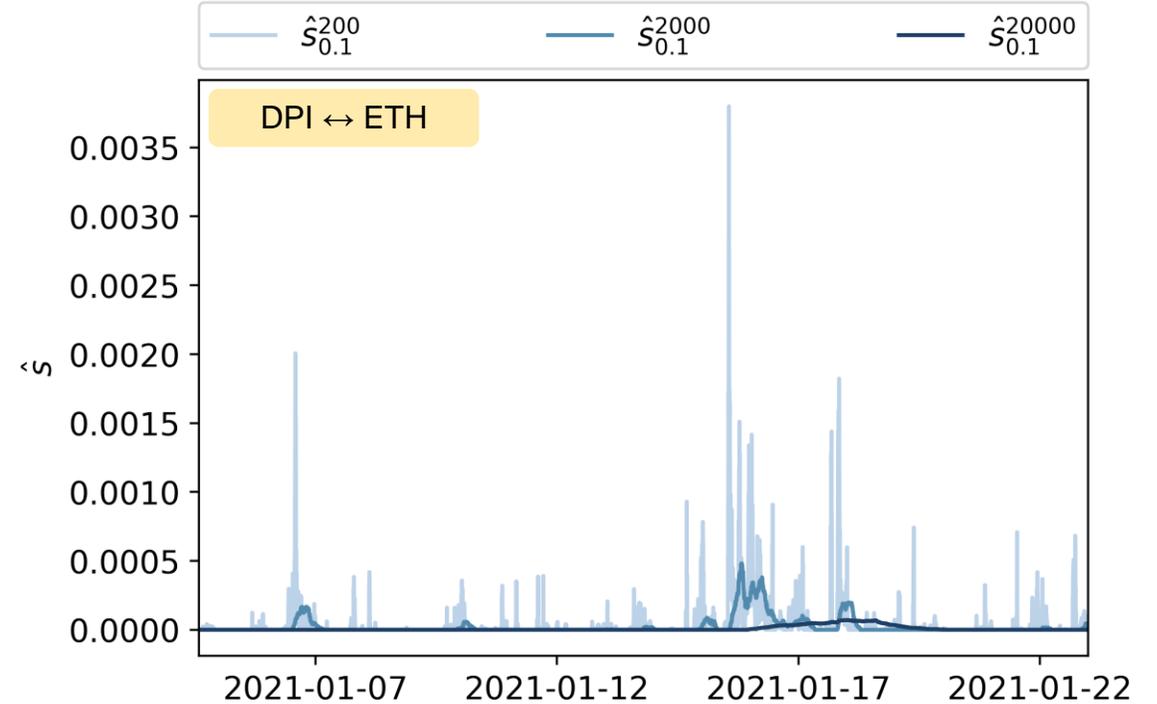
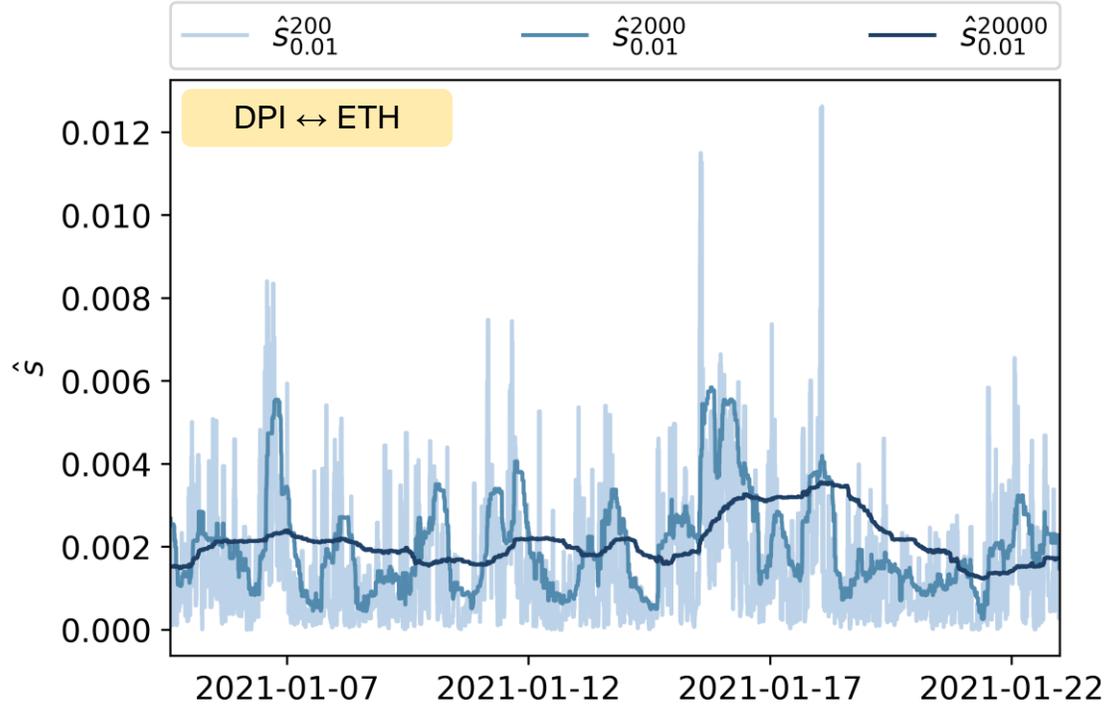
# Computing lower bound for slippage tolerance ( $s_r$ )



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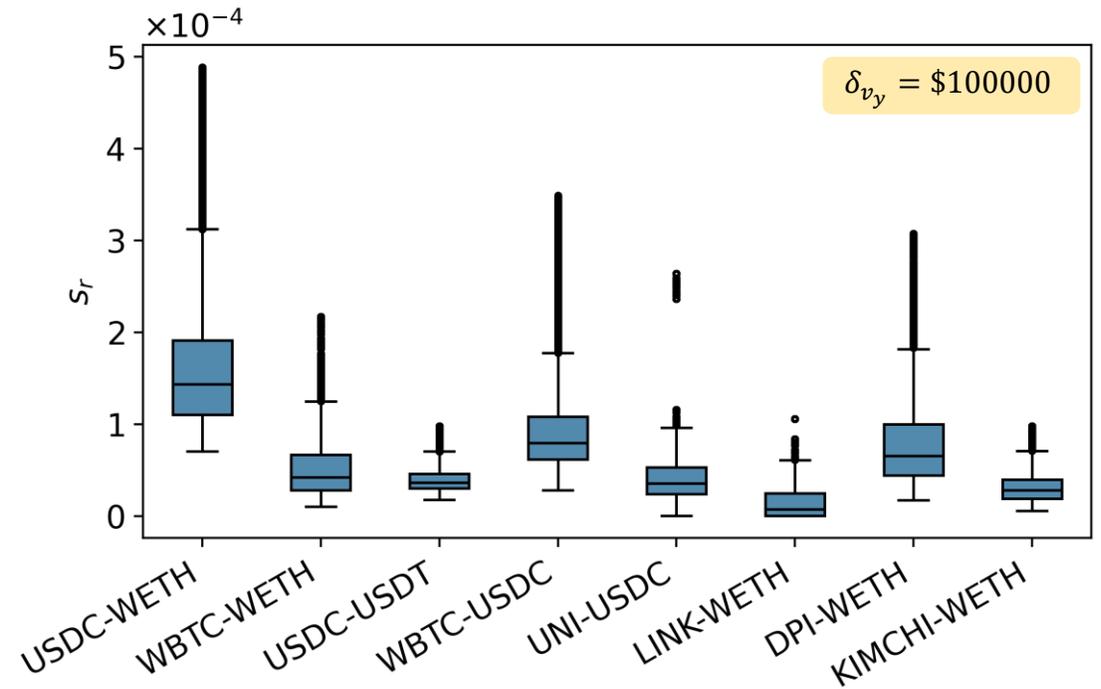
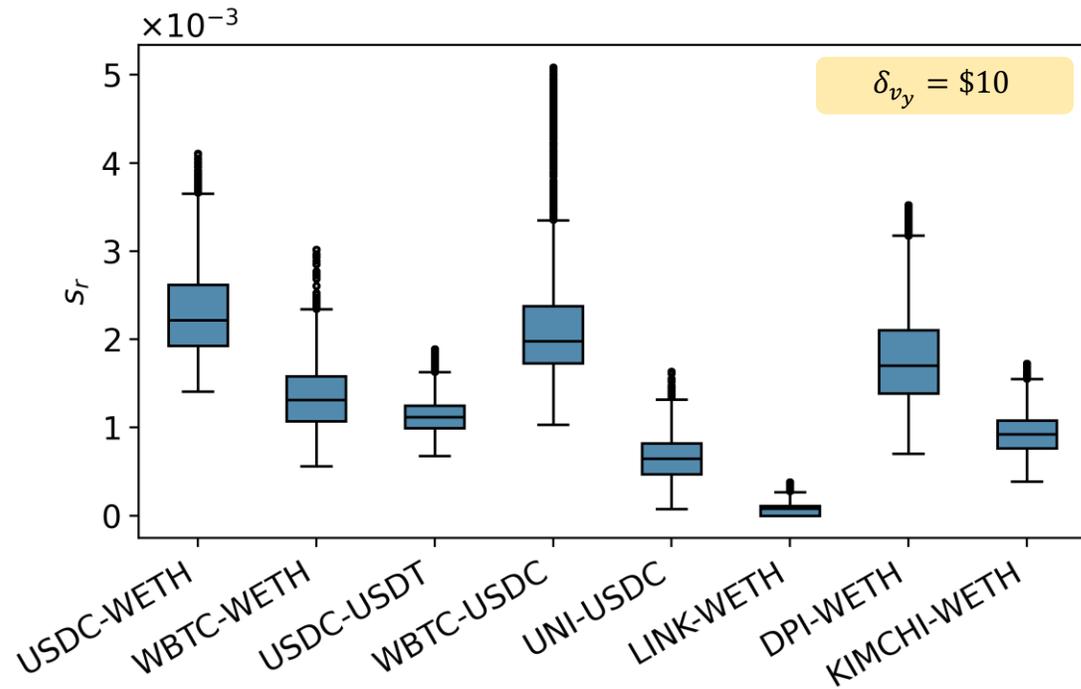


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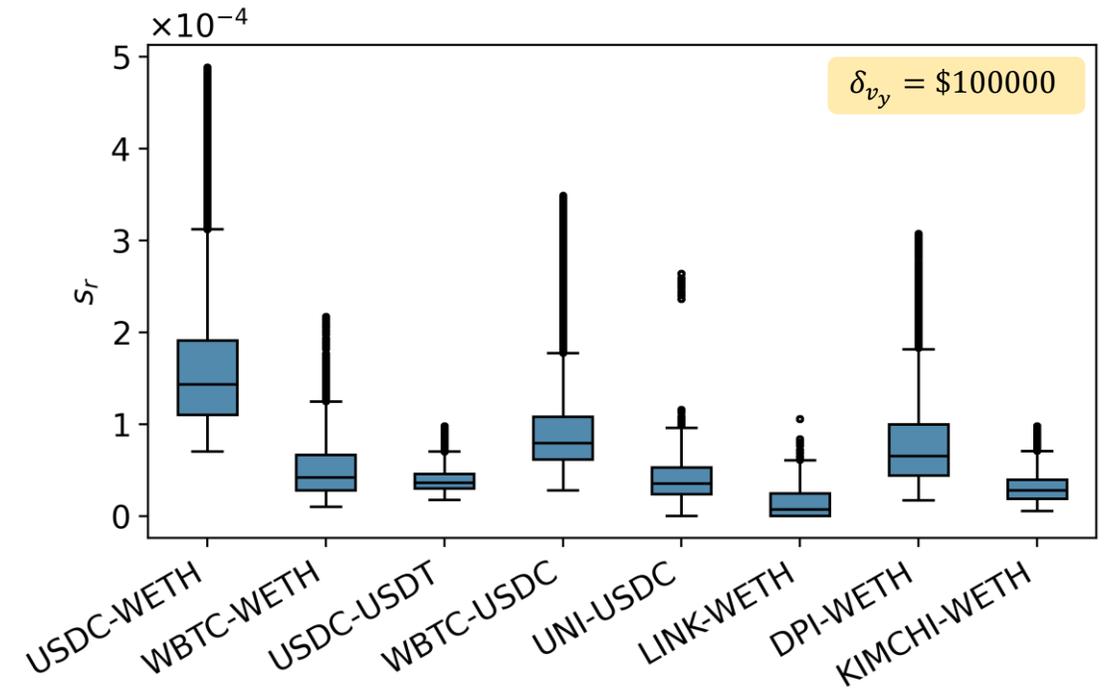
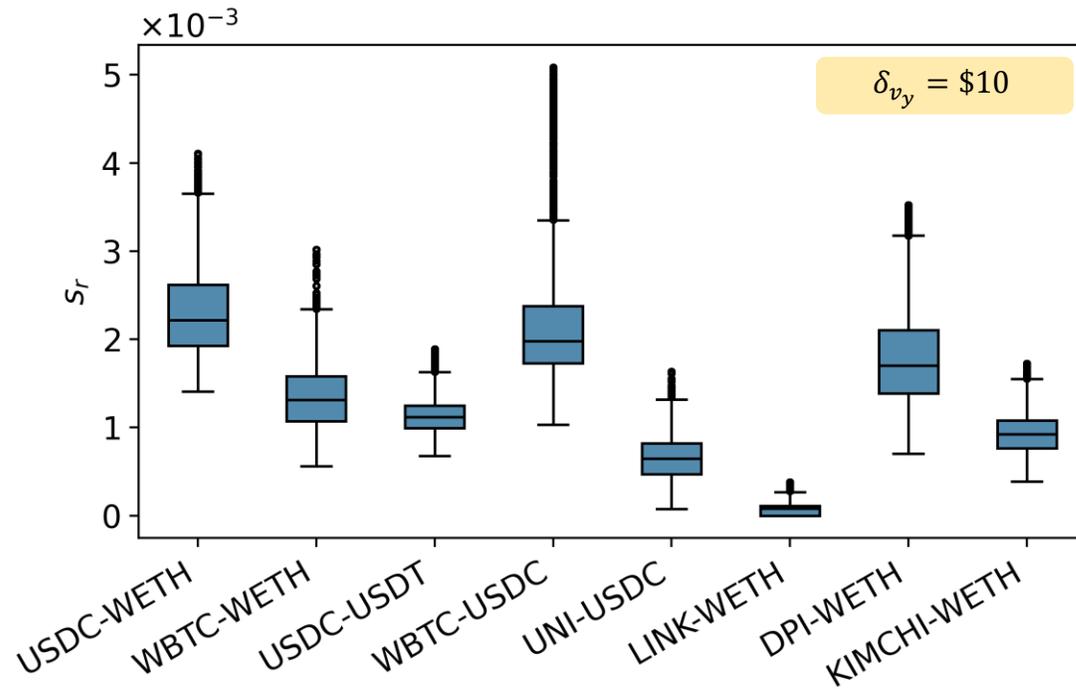
p=0.01	USDC $\rightleftharpoons$ WETH		USDC $\rightleftharpoons$ USDT		WBTC $\rightleftharpoons$ WETH		DPI $\rightleftharpoons$ WETH	
	$\mu$	$\eta$	$\mu$	$\eta$	$\mu$	$\eta$	$\mu$	$\eta$
<b>window size</b>								
200	$-2.37 \cdot 10^{-3}$	0.637	$-8.04 \cdot 10^{-4}$	0.512	$-1.03 \cdot 10^{-3}$	0.611	$-1.65 \cdot 10^{-3}$	0.656
2000	$-2.74 \cdot 10^{-3}$	0.093	$-8.95 \cdot 10^{-4}$	0.06	$-1.22 \cdot 10^{-3}$	0.106	$-2.03 \cdot 10^{-3}$	0.078
20000	$-2.93 \cdot 10^{-3}$	0.014	$-9.27 \cdot 10^{-4}$	0.014	$-1.37 \cdot 10^{-3}$	0.007	$-2.13 \cdot 10^{-3}$	0.045

p=0.1	USDC $\rightleftharpoons$ WETH		USDC $\rightleftharpoons$ USDT		WBTC $\rightleftharpoons$ WETH		DPI $\rightleftharpoons$ WETH	
	$\mu$	$\eta$	$\mu$	$\eta$	$\mu$	$\eta$	$\mu$	$\eta$
<b>window size</b>								
200	$-3.49 \cdot 10^{-4}$	0.042	$-7.35 \cdot 10^{-6}$	0.335	$-1.85 \cdot 10^{-5}$	0.194	$-4.36 \cdot 10^{-5}$	0.213
2000	$-2.99 \cdot 10^{-4}$	0.001	$-1.24 \cdot 10^{-6}$	0.314	$-4.34 \cdot 10^{-6}$	0.148	$-2.18 \cdot 10^{-5}$	0.186
20000	$-2.56 \cdot 10^{-4}$	0.003	0.00	0.310	$-1.04 \cdot 10^{-6}$	0.114	$-7.81 \cdot 10^{-6}$	0.143

# Lower bound for slippage tolerance ( $s_r$ )

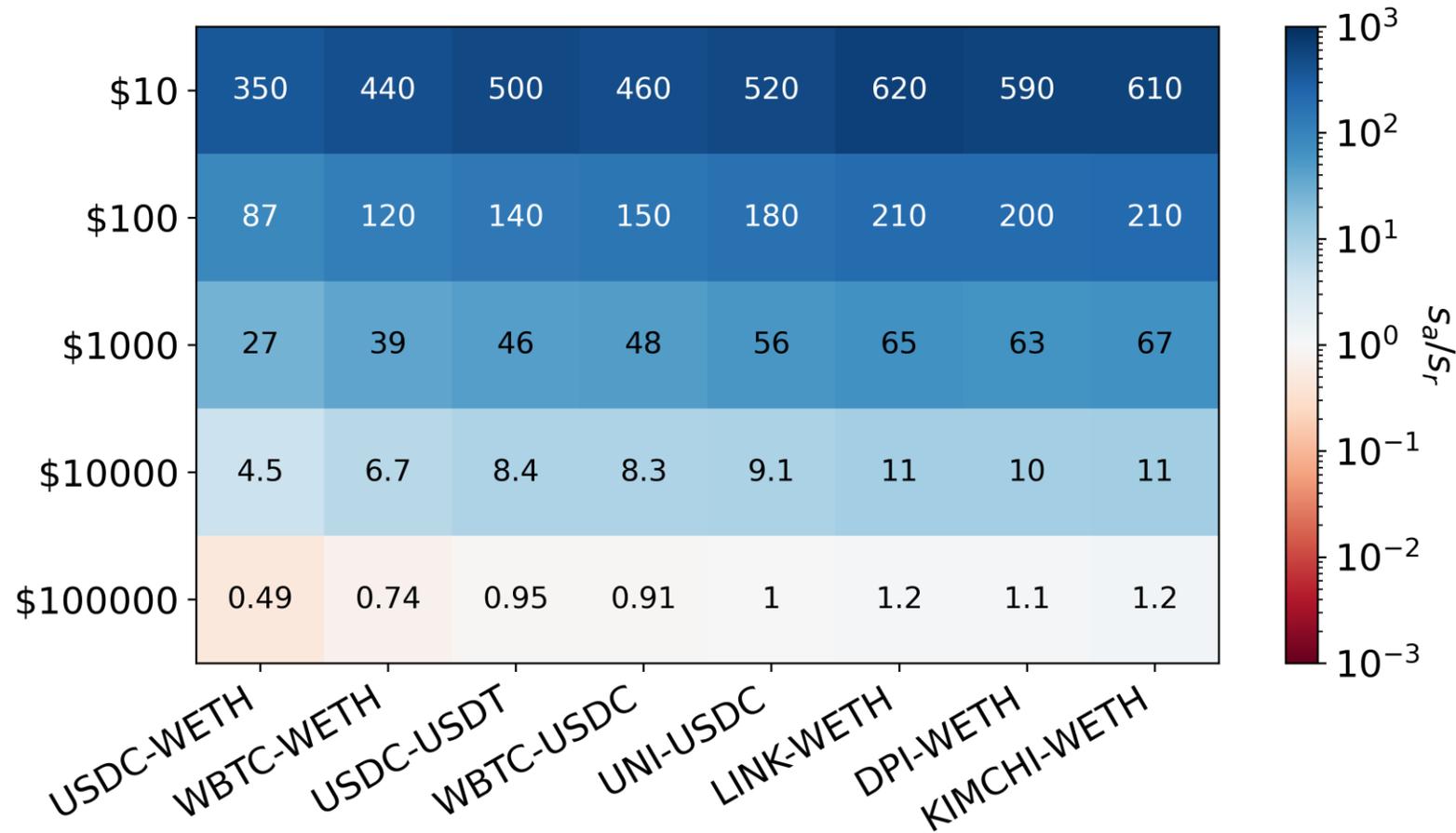


# Lower bound for slippage tolerance ( $s_r$ )

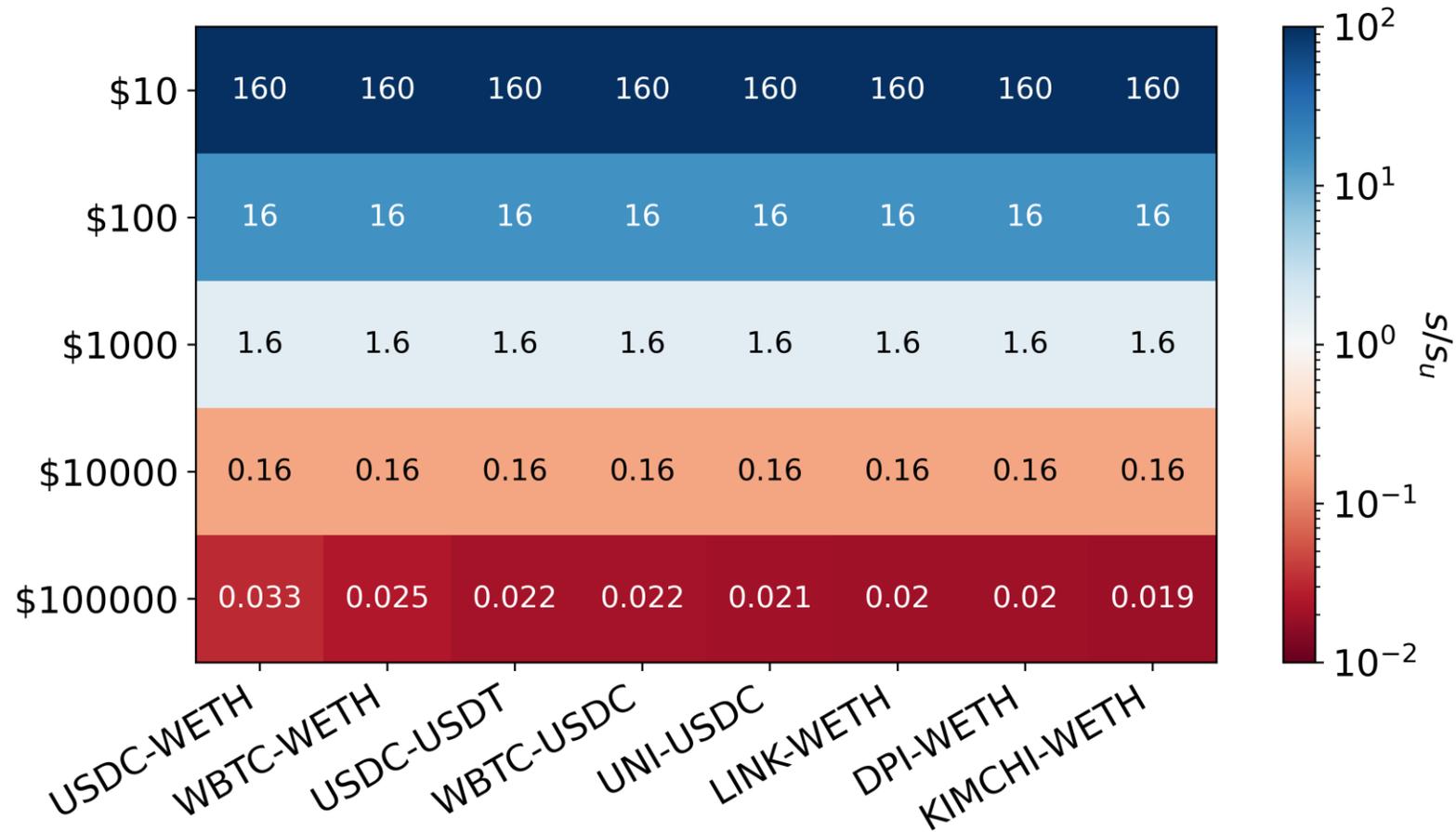


$s_r$  smaller for low volume pools

# Slippage tolerance comparison



# Slippage tolerance comparison



# Outlook: Uniswap V3

concentrated liquidity

# Outlook: Uniswap V3

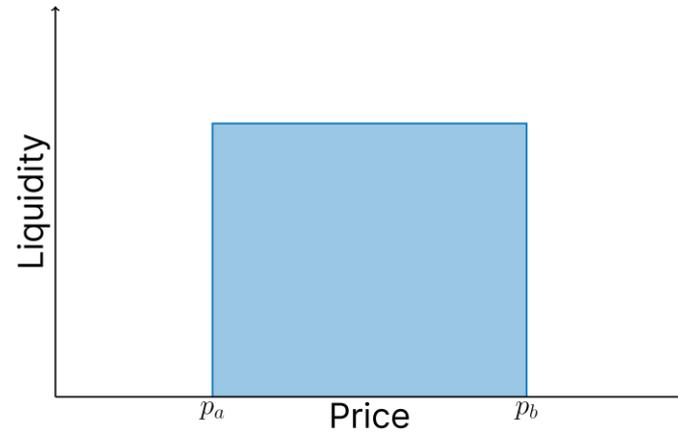
concentrated liquidity



# Outlook: Uniswap V3

concentrated liquidity

liquidity providers choose price range  $[p_a, p_b]$  in which they would like to provide liquidity



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