

Byzantine Preferential Voting



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Wishlist for Christmas



1.



2.

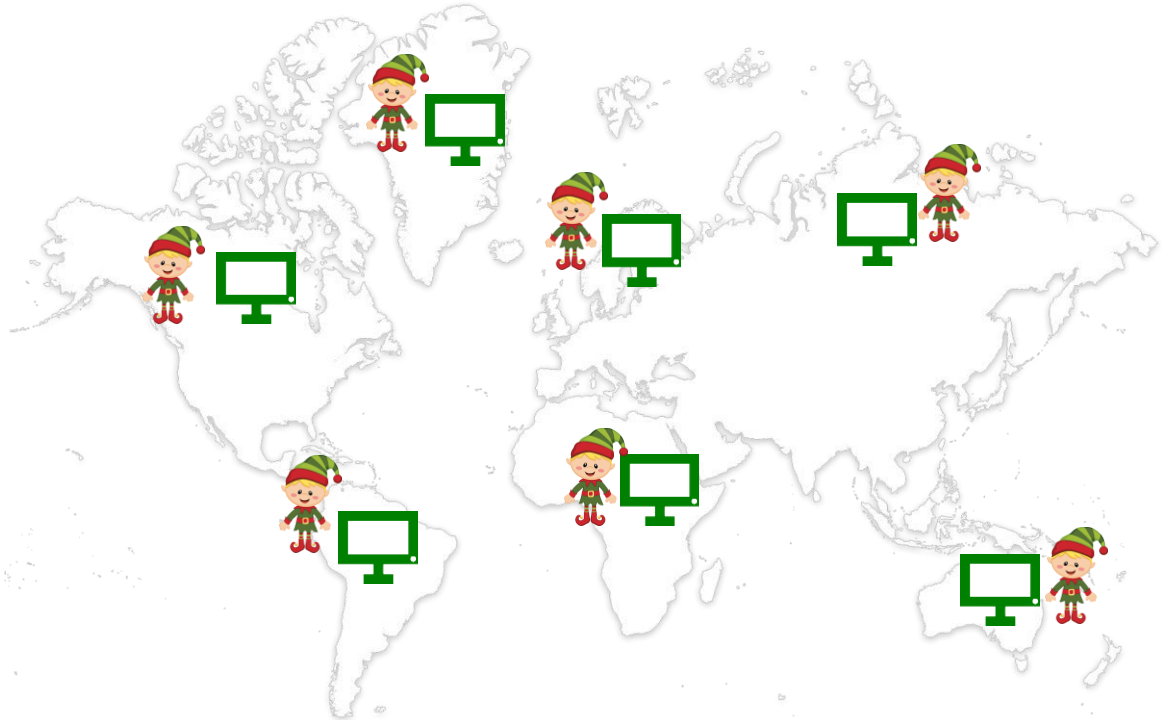


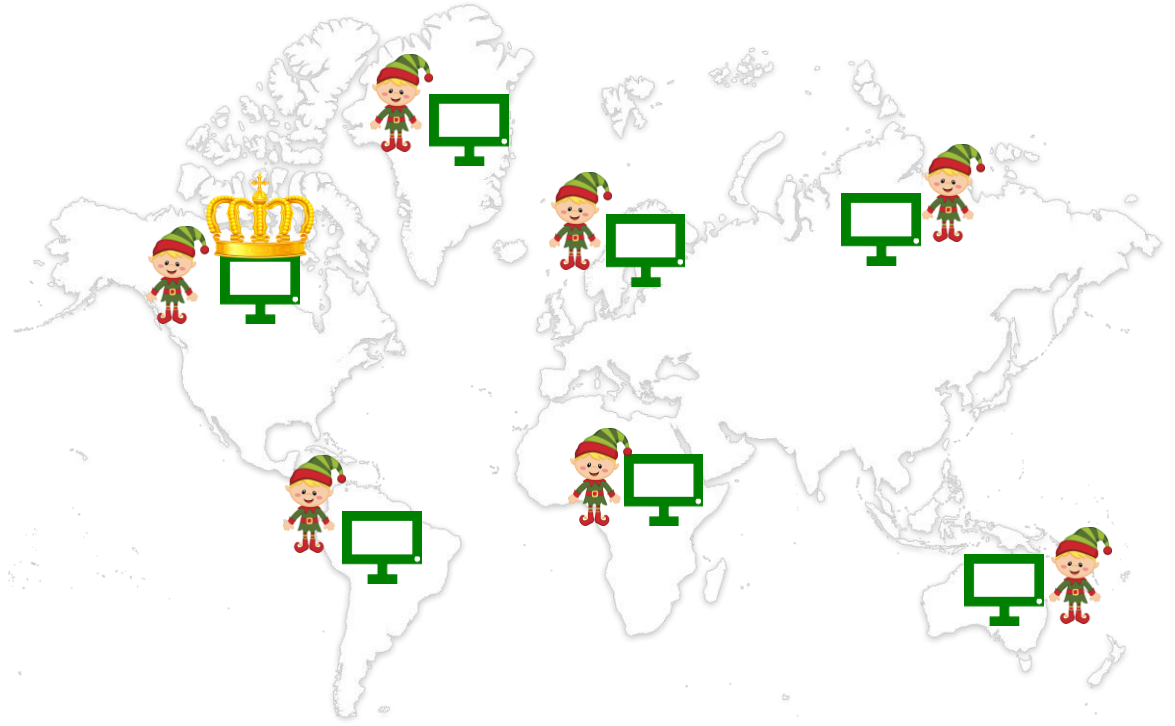
3.



Help from Elfs





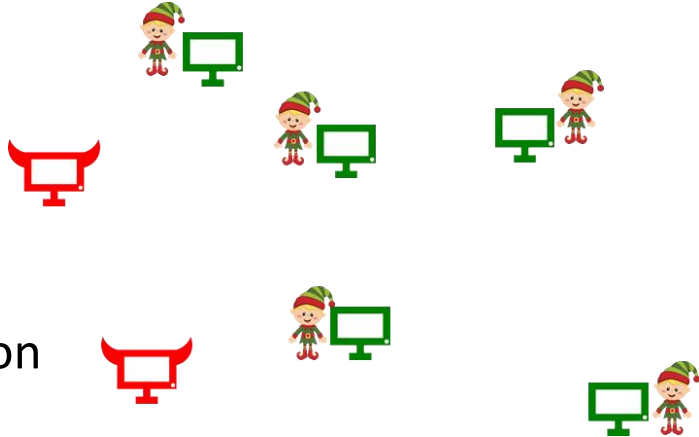




Synchronous Communication

One round:

- broadcast input
- receive input from neighbors
- do local computation



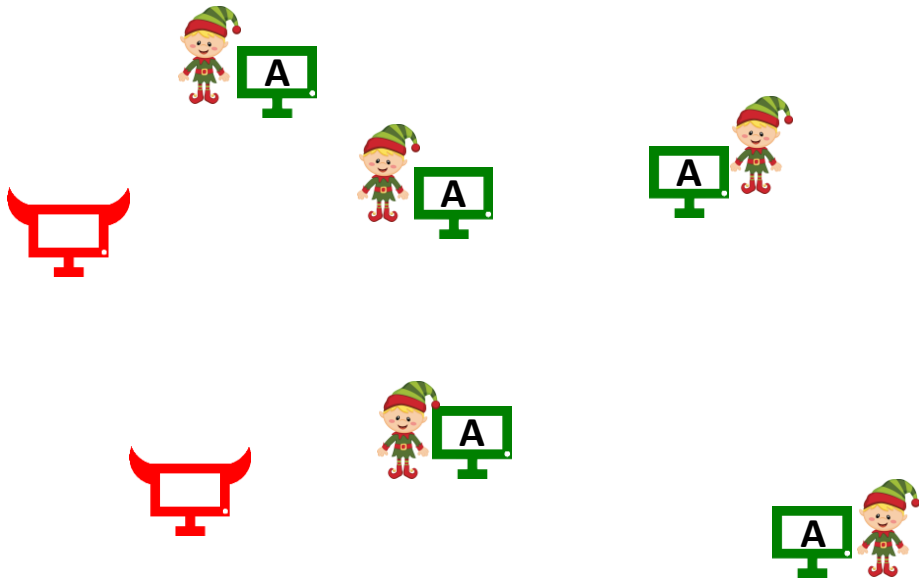
While the Grinch...



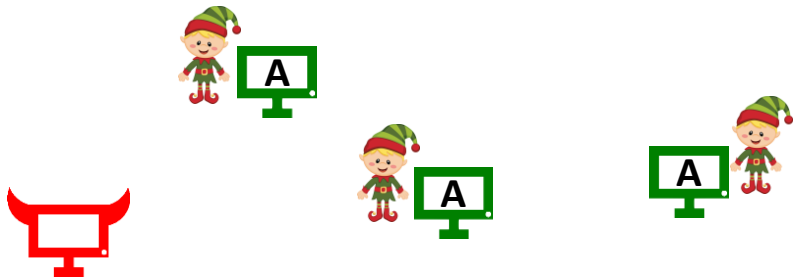
- lies about inputs
- pretends to have different inputs
- knows all other rankings
- knows the protocol
- is unpredictable

Synchronous Byzantine Agreement

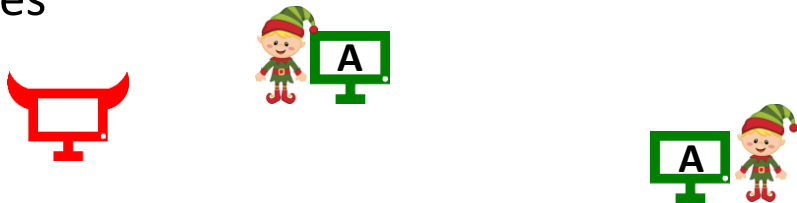
Agreement, Termination, Validity



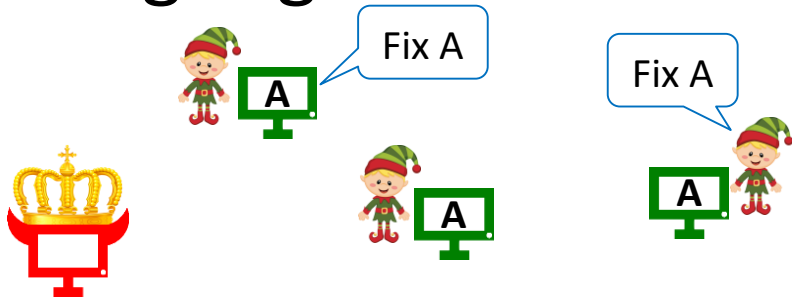
Agreement, Termination, Validity



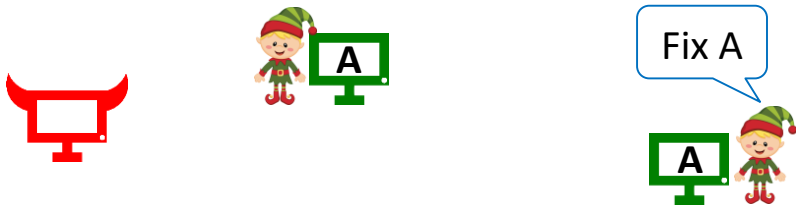
$t < n/3$ Byzantines



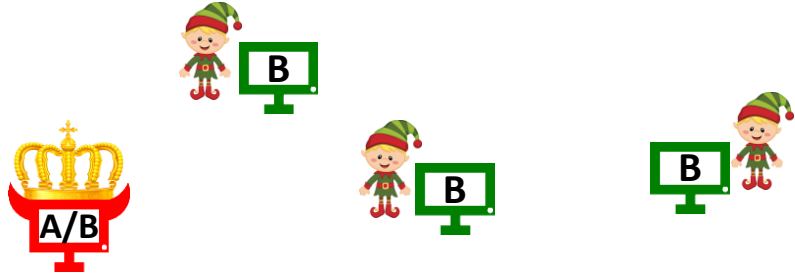
King-Algorithm



- pick $t+1$ kings
- check validity



King-Algorithm

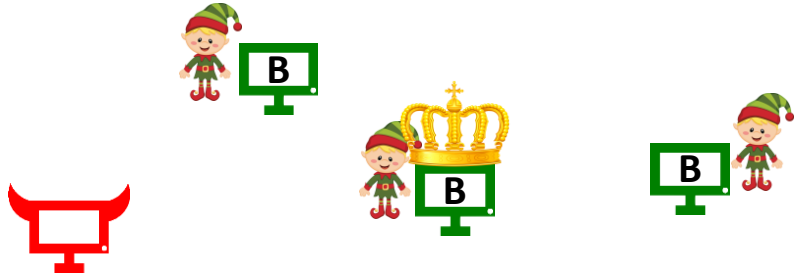


King round:

- adapt input

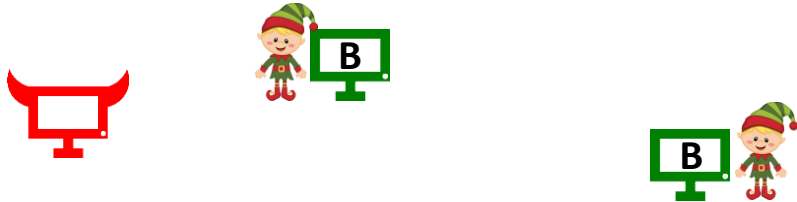


King-Algorithm



King round:

- adapt input



Rankings vs. Top Alternatives



1.

A

B

A

C

2.

B

A

C

B

3.

C

C

B

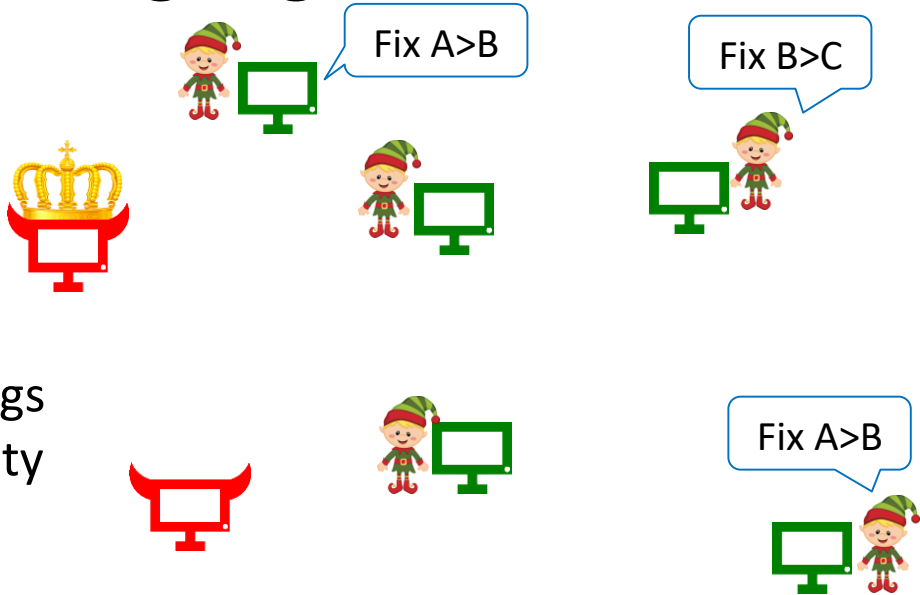
A

Pareto-Validity



-
- | | | | | |
|-----------|----------|----------|----------|----------|
| 1. | A | B | A | C |
| 2. | B | A | C | B |
| 3. | C | C | B | A |
-

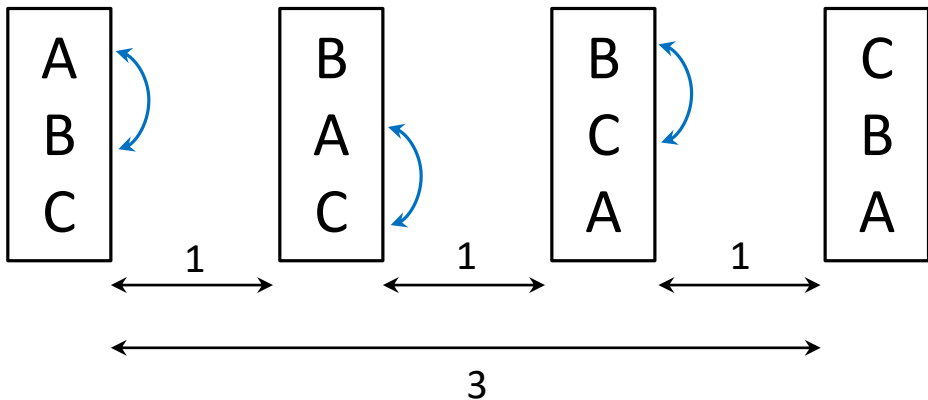
King-Algorithm



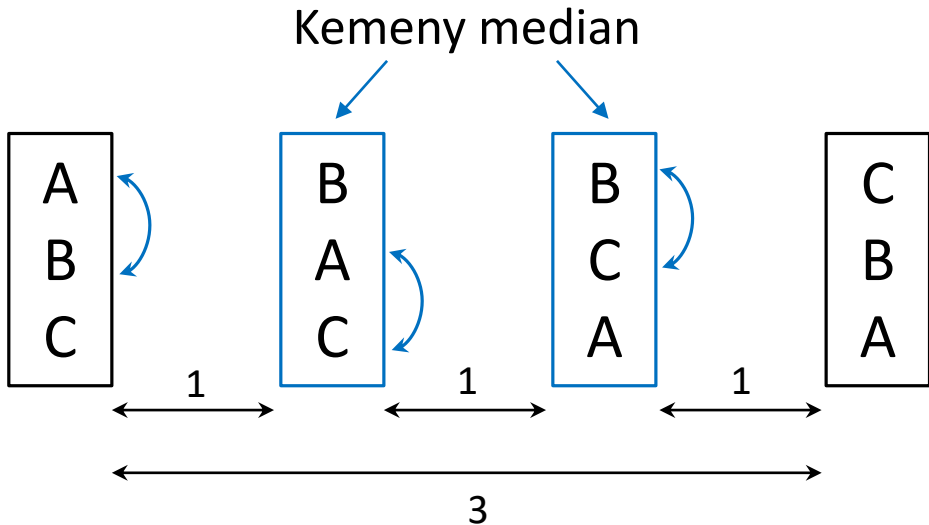
- pick $t+1$ kings
- check validity

Better: Kemeny Median

Kendall tau Distance



Kendall tau Distance





1.

A

B

A

C

2.

B

A

C

B

3.

C

C

B

A

A

B

C



1.

A	B	A	C
---	---	---	---

2.

B	A	C	B
---	---	---	---

3.

C	C	B	A
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A

B

C

B

A

C

A

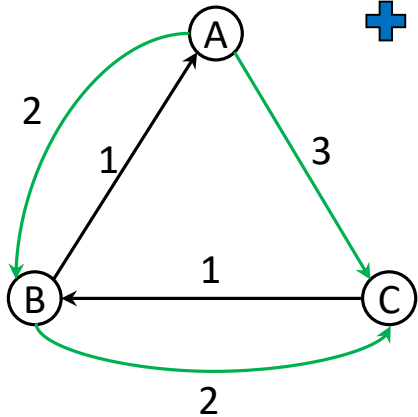
B

C

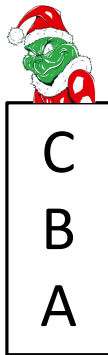
A

C

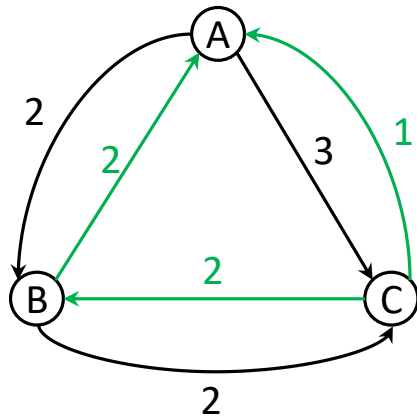
B



+

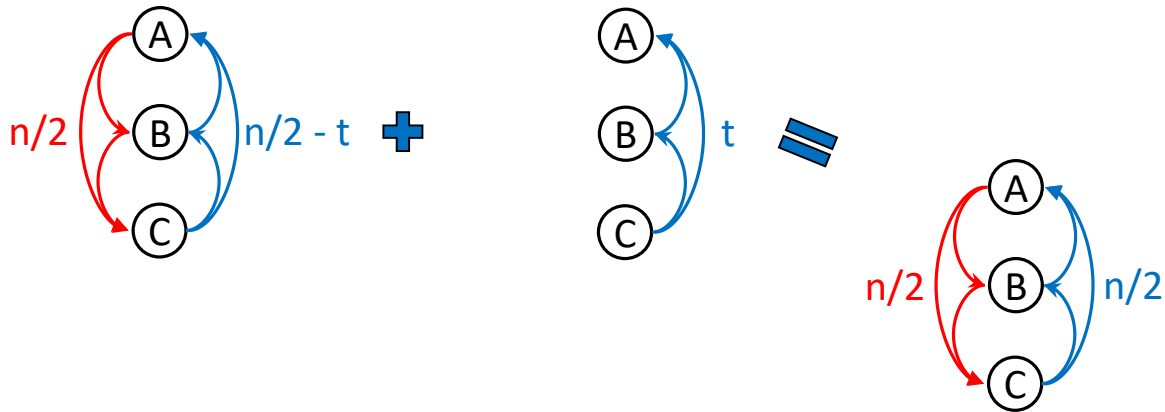


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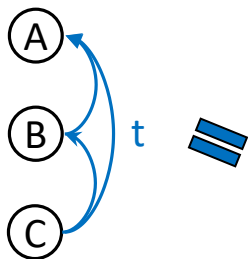
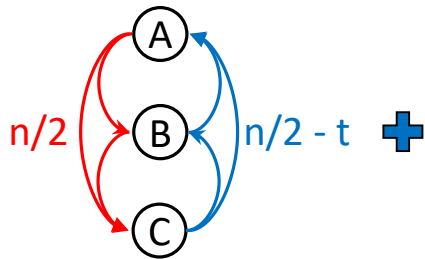


Best Possible Approximation of the Kemeny-Median

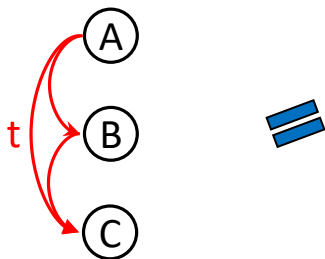
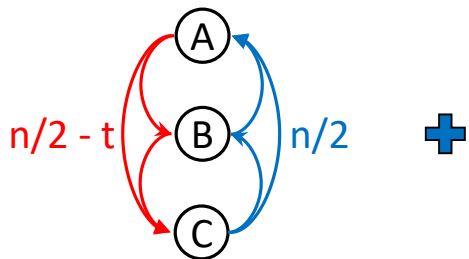
Binary Rankings



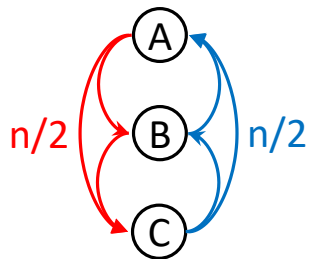
Binary Rankings



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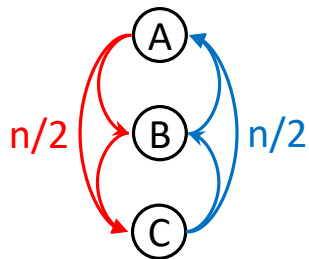
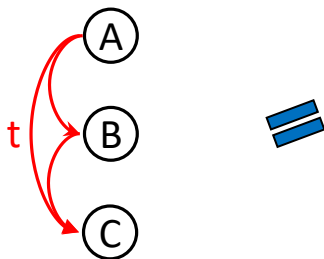
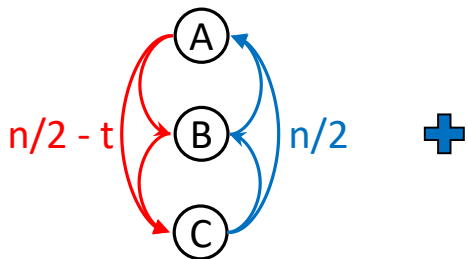
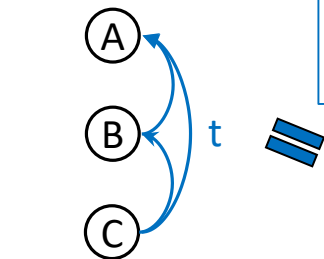
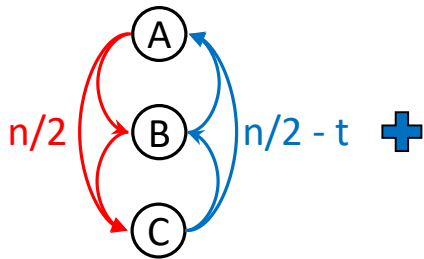


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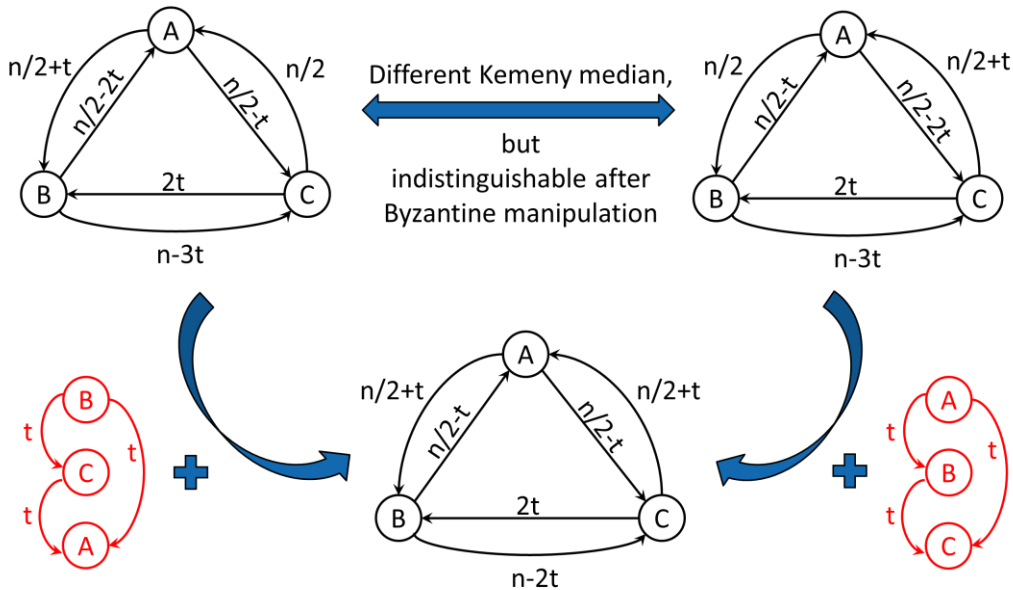


Binary Rankings

$$\frac{n/2}{n/2 - t} < 3$$



Non-Binary Rankings



Algorithm for Kemeny-Median

- Broadcast own ranking
- Choose Kemeny Median locally
- Apply King algorithm with Pareto-Validity

Byzantine Preferential Voting

- Other voting rules
 - e.g. Scoring rules
- Alternative communication models
 - Asynchronous model
 - graphs



Thank You!

Questions & Comments?



Thanks to my co-authors
Yuyi Wang, Roger Wattenhofer