

Mangrove: Fast and Parallelizable State Replication for Blockchains

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Abstract

MANGROVE is a novel scaling approach to building blockchains with parallel smart contract support. Unlike in monolithic blockchains, where a single consensus mechanism determines a strict total order over all transactions, MANGROVE uses separate consensus instances per smart contract, without a global order. To allow multiple instances to run in parallel while ensuring that no conflicting transactions are committed, we propose a mechanism called Parallel Optimistic Agreement. MANGROVE is optimized for performance under *optimistic* conditions, where there is no misbehavior and the network is synchronous. Under these conditions, our protocol can achieve the latency of 2 communication steps between creating and executing a transaction.

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1 Introduction

Scalability remains a major challenge for blockchain systems. Arguably, no single blockchain currently offers sufficient throughput to support traditional Web 2.0 applications in a trustless manner [46]. In the modern blockchain landscape, users are fragmented across numerous Layer-1, Layer-2, and even Layer-3 chains. This fragmentation raises concerns about the interoperability and latency of decentralized applications built on top of these chains.

Techniques like sharding, where network nodes are divided into groups to process transactions in parallel [55, 4], have gained considerable attention as potential solutions to the problem. Although sharding has been proven to enhance system performance, the techniques come with drawbacks and limitations. Specifically, sharded systems experience significant latency (or abortion rate) when dealing with smart contracts with high contention. Furthermore, they require cross-shard agreement for transactions spanning multiple shards.

Since it has been established that consensus is not necessary for applications like payments [34, 32], the research on consensus-less payment systems [13] has offered a remarkably simple alternative solution to the problem of scaling. Foregoing consensus, these systems offer a model in which every validator can parallelize processing and execution of all transactions without limitation. In contrast, sharding protocols assume a rigid division of validators that complicates the system and limits the potential for parallelizability. However, consensus-less systems can support only a limited range of applications, as consensus is necessary for general smart contracts.

45 **Our Contributions.** We address the following research question:

46 “Can a protocol supporting consensus exhibit the advantages of consensus-less payment
47 systems?”

48 and answer in the positive. We summarize our contributions in the following.

- 49 ■ We propose the Replicated Actor Model, a novel execution model for blockchain systems
50 based on externally owned accounts (user actors) and smart contracts (reactive actors),
51 that makes dependencies explicit with parallelizability in mind.
- 52 ■ We introduce Parallelizable Optimistic Agreement (POA), a consensus primitive that can
53 be used to achieve consensus on the stream of incoming transactions for individual smart
54 contracts. POA instances are designed to run in parallel, while ensuring that conflicting
55 (i.e., double-spending) transactions cannot be committed.
- 56 ■ The resulting system, called MANGROVE, combines limitless parallelization, low latency,
57 and support for general smart contracts. In MANGROVE, no single validator can delay the
58 entire system’s progress, and congestion at one smart contract does not impede the rest of
59 the system. In other words, the transaction throughput of different smart contracts can
60 be scaled horizontally by validators. Additionally, our system achieves optimal latency in
61 optimistic conditions, where users or validators do not misbehave, and the network is
62 synchronous. Under these conditions, a block producer can commit a transaction to a
63 smart contract in *two* communication steps.

64 2 Related Work

65 **Consensusless Systems.** Blockchain-based systems use consensus mechanisms as their core
66 building block. However, consensus tolerating Byzantine faults [39] is inherently slow. First
67 blockchain systems such as Bitcoin [42] and Ethereum [18] are notorious for their limited
68 performance.

69 However, it has been established that consensus is not necessary for many applications,
70 such as payments [34, 32]. Designs such as Fastpay [13], Astro [22], and Accept [41] propose
71 remarkably simple solutions that inherently parallelize the workload. Validators in these
72 systems can easily add computational resources to process more transactions. Tonkikh
73 et al. [54] and Bazzi et al. [14] show that even dependencies between transactions of the
74 same issuer can be resolved without consensus. Other systems, such as Groundhog [45],
75 Setchain [20], and Pod [8] avoid consensus by using commutative semantics. Frey et al. [30]
76 and Sridhar et al. [52] recently introduced new consensus-free objects, inspired by Byzantine
77 fault-tolerant CRDTs [35]. MANGROVE is orthogonal to these efforts, as it focuses on the
78 interplay between all types of objects (with- or without consensus). Albouy et al. [6] show
79 how a consensusless system can also provide anonymity properties in a lightweight fashion.

80 Despite their numerous advantages, consensusless systems are inherently unsuitable
81 for many applications, as general smart contracts require consensus [7]. The CoD [48]
82 primitive alleviates this problem to a limited extent, by mixing payment system-like logic
83 with consensus as fallback. In turn, it exhibits the problems of consensus systems, like poor
84 parallelizability.

85 Sui [16, 37] is a modern blockchain system that recognizes the mentioned problems and
86 incorporates a consensusless component in its design. Sui relies on consensus only for complex
87 tasks, like ordering accesses to the same shared objects. We further increase scalability, by
88 allowing parallelism even for shared objects. In addition, MANGROVE outperforms Sui in the
89 number of communication rounds needed for transaction execution. Our proposed system

shares many characteristics with Basil [53], namely parallel execution of non-conflicting transactions and fast commits under optimistic conditions. Contrary to Basil, in MANGROVE users do not have to drive progress themselves and benefit from lower latency.

Fast Byzantine Consensus. Martin and Alvisi [40] present an algorithm that achieves Byzantine Consensus in just two communication steps under optimistic conditions, specifically assuming an honest leader and a synchronous network. They introduce a parameter $p \leq f$, which represents the number of failures supported by the fast path and show a resilience bound of $n \geq 3f + 2p + 1$. Subsequent work explores the potential and pitfalls of fast consensus, both for single-shot consensus and state machine replication [49, 1, 33]. Recently, Kuznetsov et al. [38] and Abraham et al. [2] revisited this topic, pointing out that for the category of protocols where the set of proposers is a subset of the validators, a lower resilience bound of $n \geq \max(3f + 1, 3f + 2p - 1)$ can be achieved.

In contrast to prior [38] that limits the set of proposers to a subset of validators, our protocol allows all users to act as proposers. This generality requires us to meet the more stringent resilience bound of $n \geq 3f + 2p + 1$ by Martin and Alvisi. Our protocol, MANGROVE, matches this bound and thus achieves optimal resilience in this setting.

Parallel Execution. Parallelization is a natural way to improve scalability and can be applied at various levels in blockchains. Parallel execution [31, 10, 26, 43] aims to accelerate the local execution of transactions by the validator across cores, while distributed execution [36] leverages multiple machines per validator. Both approaches concentrate on improving local execution, whereas our work targets the elimination of the bottleneck of the single agreement mechanism.

Sharding. Sharding [3, 9, 24, 4] is a technique of splitting the system state among disjoint groups of validators called shards. As shown in [4], while sharding is efficient when a transaction only accesses a part of the system within one shard, it can result in high latency or abortion rate [5] for transactions that span multiple shards, especially for highly contested actors. In MANGROVE, “popular” actors do not slow the progress of the whole system. Instead, actors progress independently, ensuring that the system’s overall performance remains unaffected by the contention of individual actors.

3 Replicated Actor Model

Today, it is common for blockchains to define a total order over all transactions [42, 18]. Thus, the ensuing sequential and atomic execution of transaction bundles is often the only considered execution model. The obtained atomic composability property allows for (potentially counterintuitive) applications such as flash loans [44].

In this work, we challenge the status quo of this execution model. To this end, we define the replicated actor model, which foregoes global sequential ordering and is more suited for parallelism. In Appendix A we discuss the model’s expressiveness and even propose an extension, which optionally allows for the reintroduction of (targeted) atomic composability.

Our model is closely related to the object model of Sui [16]. We differentiate between the following four types of components.

Actors. A *user actor* is associated with a digital signature key pair. We say that a key pair (user) *controls* a user actor. *Reactive actors* are analogous to smart contracts and can be

132 thought of as a Turing machine with arbitrary state that can be changed via computations.
 133 Actors can emit new transactions.

134 **Objects.** *Owned objects* are objects owned by some actor, e.g. gas, tokens, or NFTs. Every
 135 type of owned object is associated with a set of actions that can be performed over it. These
 136 actions are specified in a global *read-only object* containing the type definition. For example,
 137 for gas objects or tokens, those actions may include splitting and merging. Ownership of
 138 objects can be transferred. Assume actor A owns a gas object O worth 10 coins and wants
 139 to transfer 2 coins to actor B . Then A might perform `split([8, 2])` on O to receive two
 140 objects worth 8 and 2 coins respectively, and transfer the latter to B .

141 **Users.** A *user* is an external entity associated with a key pair, who interacts with the
 142 system by creating and giving instructions to actors through their user actors.

143 **Validators.** The *validators* are the network participants in charge of running MANGROVE.
 144 Validators participate in the broadcast and consensus algorithms and are responsible for
 145 keeping a consistent state of the system by maintaining the ownership records of each owned
 146 object and the state of actors.

147 3.1 Validators

148 We consider a set of n validators, denoted by $\mathcal{V}$, which we assume to be known to all users
 149 and validators. We require that at most f of them are Byzantine [39]. We call non-Byzantine
 150 validators *honest*. Additionally, under optimistic conditions and when less than p validators
 151 are Byzantine, a transaction can be committed in two communication steps. MANGROVE
 152 assumes the participation of $n \geq 3f + 2p + 1$ validators.

153 Each validator maintains a dedicated state associated with each actor in the system which
 154 we call an *entity*. We denote an entity of validator V corresponding to an actor A with $V.A$.
 155 Different entities may be located on different machines at the validator's discretion and can
 156 communicate with each other.

157 Entities of different validators communicate via Outer Links, and entities within a validator
 158 communicate via Inner Links. The Inner and Outer Links implement Perfect Links [19] and
 159 expose the following interface:

- **function** $Send(m, A)$: sends message m to A
 - **callback** $Deliver(m, A)$: fired upon receiving message m from A

160
 161 Apart from direct messages, validators use two agreement primitives: Parallel Optimistic
 162 Agreement (POA), which is used for transactions involving reactive actors, and Parallel
 163 Optimistic Broadcast (POB), which is used for transactions that involve only user actors.
 164 Both primitives contain a fast path, consisting of (i) a broadcast step and (ii) a single voting
 165 step. In case of a failure (and only in case of failure), the fast path is followed by a failover
 166 mechanism (slow path) that ensures safety and liveness. Both primitives run in consecutive
 167 instances and are described in Section 5 and Appendix C respectively.

168 Through these agreement primitives, we ensure that honest validators have a consistent
 169 view of the state of each reactive actor and the ownership of owned objects.

3.2 Transactions

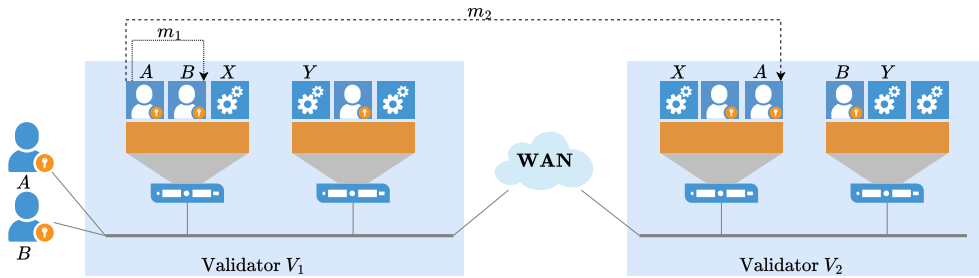
Every transaction in our system *consumes* owned objects, meaning that once a transaction is executed, the objects it consumed no longer exist. Every transaction would consume a *gas* object to pay for computation fees, the economics of which we leave outside the scope of this work. Every transaction has a *Code* field, that specifies a list of commands to perform when a transaction is being executed. These commands can be (a) actions over owned objects a transaction consumed or created, (b) creating owned objects, (c) creating new actors, and (d) issuing new transactions. The model differentiates between user and reactive actor transactions.

User Actor Transactions. Users can instruct a user actor they control to issue a transaction. Transactions issued by the user actor are categorized based on the presence of a recipient. If a transaction does not have a recipient, it is referred to as a UA transaction. If it does have a recipient, which is always a reactive actor, it is referred to as a UA-RA transaction.

A UA transaction is of the form $\langle A, sn, [O_1, \dots, O_k], Code \rangle$ where A , a user actor, is the sender, $sn \in \mathbb{N}$ is a sequence number and it *consumes* owned objects $O_1, \dots, O_k$ (that must be owned by A) and performs actions specified in *Code* over them. *Code* is allowed to create new owned objects at other user actors (arbitrarily many of those), but not reactive actors. It may also spawn new reactive actors. The reason a UA transaction can create new owned objects at user actors but not reactive actors is that the former is commutative whereas the latter requires agreement on the order.

UA-RA transactions are of the form $\langle A, sn, X, [O_1, \dots, O_k], Code_{pre}, Call, Code_{post} \rangle$ instead. That is, they additionally include a recipient X that must be a reactive actor and a *Call* field specifying a function call to perform on X . A reactive actor might issue its own transactions as a result of processing a *Call*. *Code_{pre}* can operate over the consumed objects and prepare them for input into the function call. *Code_{post}* can instead operate over the objects returned by the function call and, for example, decide whether and which additional transactions to spawn based on them. The pre- and post-processing *Code* blocks may spawn transactions of their own and can be executed in parallel to any other transaction since they do not have access to the internal state of the reactive actor.

► **Definition 1 (Conflicting Transactions).** Two user transactions tx and tx' with $tx \neq tx'$ and $tx.sender = tx'.sender$ are said to be conflicting if $tx.sn = tx'.sn$.



■ **Figure 1** System entities. The validators V_1 and V_2 maintain the user actors corresponding to users A and B , and reactive actors, e.g., X and Y . The message m_1 is sent from $V_1.A$ to $V_1.B$ via Inner Links and a message m_2 to $V_2.A$ via Outer Links. Entities can be spread across multiple machines and organized independently by each validator.

201 Users are responsible for issuing non-conflicting transactions with consequent sequence
 202 numbers. Moreover, users are also responsible for making sure that a user actor they are
 203 issuing a transaction for will eventually own the objects consumed by the transaction. We
 204 highlight that a user failing to adhere to these requirements has no global impact on the
 205 system, but just on the actors controlled by them.

206 **Reactive Actor Transactions.** Unlike user actors, reactive actors only issue transactions as
 207 a potential result of executing an incoming transaction.

208 A reactive actor transaction (RA-RA) is always sent to another reactive actor and shares
 209 the same structure as a UA-RA transaction, except it omits the sequence number. This
 210 omission is because the order of outgoing RA-RA transactions is determined by the order
 211 of incoming transactions. The sender is the reactive actor that produced the transaction.
 212 Upon receiving either a UA-RA or an RA-RA transaction, a reactive actor might perform
 213 computation to change its state based on the current state and *Call* data specified in the
 214 transaction.

215 3.3 Network and Computation Model

216 The partial synchrony settings of Global Stabilization Time (GST) and Unknown Delta [27]
 217 constitute the gold standard of assumptions under which modern blockchains are designed
 218 to operate. MANGROVE is designed to function in the GST network model, i.e., correctness
 219 is ensured even in complete asynchrony, and liveness is achieved after an arbitrary point
 220 in time called Global Stabilization Time, or GST for short. Before GST, messages can
 221 be delayed with arbitrary delay, but every message sent at time t must be delivered by
 222 $\max(t + \Delta, GST + \Delta)$. The parameter Δ is assumed to be known and fixed.

223 We assume the time required for local computations and messaging internal to a validator
 224 to be negligible.

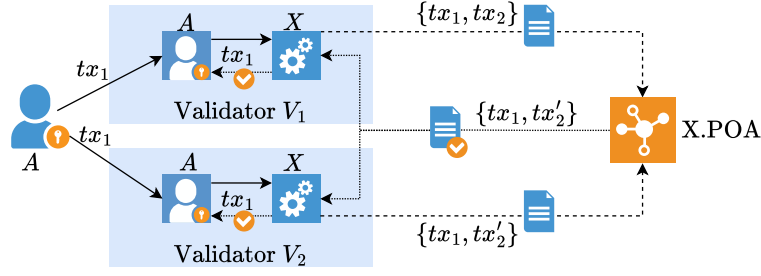
225 4 Mangrove Overview

226 The core principle behind MANGROVE is to have a dedicated agreement mechanism *per actor*.
 227 In practice, agreement is achieved differently for the different types of transactions.

- 228 ■ For user actors, validators should agree on *outgoing transactions* for each given sequence
 229 number. This, paired with sequential transaction execution, guarantees them a consistent
 230 view of the system [22]. To this end, UA transactions are disseminated through Parallel
 231 Optimistic Broadcast (POB), and the agreement follows either from the fast path if the
 232 optimistic conditions are met, or from the failover mechanism in case they are not.
- 233 ■ Instead, for reactive actors, the validators must agree on *incoming transactions*. Thus,
 234 both UA-RA and RA-RA transactions go through the Parallel Optimistic Agreement
 235 (POA) mechanism of the reactive actor of the transaction recipient. The consecutive
 236 POA instances provide a total order of *incoming transactions* to execute on a reactive
 237 actor. Importantly, since agreement is inherited from the POA properties, a dedicated
 238 agreement on the user actor can be optimistically skipped, thus also providing two step
 239 finalization latency in the fast path.

240 Since POB is simpler and less general than POA, we describe POA in Section 5 and POB
 241 in Appendix C. The complete process for handling UA and UA-RA transactions is detailed
 242 in Section 7.2, while the processing of RA-RA transactions is described in Section 7.3.

243 Both POA and POB were designed with three main goals in mind:



■ **Figure 2** Mangrove UA-RA transaction processing. First, user A broadcasts tx_1 to all $V_i.A$, who relay it to $V_i.X$ (full arrows). Then all $V_i.X$ propose tx_1 and other transactions they have to X.POA (dashed arrows). Finally, when tx_1 is included in a block decided by X.POA, all $V_i.X$ notify $V_i.A$ of the decision (dotted arrows).

- 244 (i) They have a low good-case latency, that is, they terminate in two communication steps
- 245 under optimistic conditions.
- 246 (ii) A system running multiple instances in parallel can be sure that at most one transaction
- 247 for each pair of user and sequence number is decided across all instances.
- 248 (iii) A system running multiple instances in parallel does not suffer bottlenecks.

249 Wait-Free Locking.

250 To achieve these goals, the POA and POB instances do not communicate directly but instead
 251 obtain locks via Inner Links to the user actor entities introduced in Section 3. These entities
 252 provide security against conflicting transactions by (locally) tying a sequence number to a
 253 transaction. To describe this process more precisely, we introduce the following notation,
 254 also used throughout the remainder of this work:

255 **Notation.** U denotes an arbitrary user, $V.A$ denotes an arbitrary user actor entity of
 256 an arbitrary validator, and $V.X$ denotes an arbitrary reactive actor entity of an arbitrary
 257 validator.

258 User actor entities maintain the following two data structures.

259 ► **Definition 2** (Slow-Path Locked). *Each $V.A$ maintains a map $SPLocked$, mapping sequence*
 260 *numbers to transactions. If $V.A.SPLocked[tx.sn] = tx$, we say that $V.A$ SP-locked (slow-path*
 261 *locked) tx .*

262 ► **Definition 3** (Fast-Path Locked). *Each $V.A$ maintains a map $FPLocked$, mapping sequence*
 263 *numbers to transactions. If $V.A.FPLocked[tx.sn] = tx$, we say that $V.A$ FP-locked (fast-path*
 264 *locked) tx .*

265 Intuitively, SP-locking a transaction ensures that $V.X$ will never propose a conflicting
 266 transaction in the slow path, whereas FP-locking a transaction ensures $V.X$ will never vote
 267 for a proposal containing a conflicting transaction in the fast path. However, note that V
 268 can FP-lock tx and SP-lock tx' with tx and tx' being conflicting. That might happen in
 269 a case V received tx from a user but received a lot of votes for a proposal containing tx' ,
 270 which “forces” V to propose tx' in the slow path.

271 We describe the interplay between the different building blocks of MANGROVE and their
 272 correctness in Section 7 and in Appendix F.

5 Parallel Optimistic Agreement

This section describes the algorithm used by validators to agree on a block B of transactions to be executed at a reactive actor X . For every validator V and reactive actor X , $V.X$ has a *pool*, that is, a set of transactions that $V.X$ wants to execute on X . This algorithm is defined assuming a designated validator L , called leader. The Parallel Optimistic Agreement (POA) primitive has an interface consisting of:

- **function** `INITIATE( $k, pool$ )`: start the k -th instance with a transaction *pool*
- **callback** `DECIDE( $k, B$ )`: decide a block B in k -th instance

First, in the *fast path* the leader broadcasts its proposed block and all other validators cast their votes. A validator decides on a block once it receives *enough* votes, a process we refer to as a fast-path decision. Following the fast path, and only if necessary, a *slow path* (whose components are described in Section 6) is initiated to ensure liveness in cases where users or the leader misbehave or the network experiences asynchrony. We refer to a decision made in the slow path as a slow-path decision.

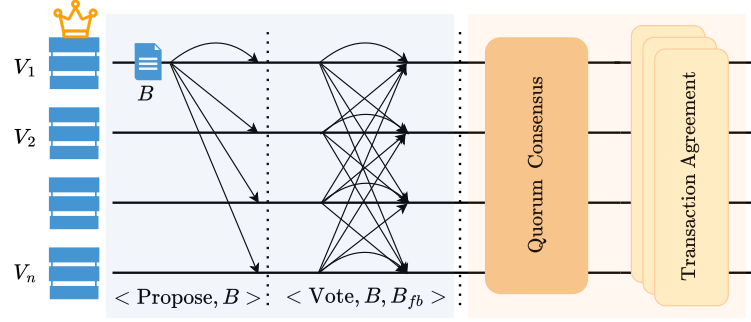


Figure 3 POA scheme. In the fast path (blue rectangle), the leader (in this case V_1) broadcasts their proposal B . Then, validators cast their vote on the proposal, and append their own transactions B_{fb} . In case the fast path fails, validators participate in the slow path (orange box), which consists of one instance of Quorum Consensus and multiple instances of Transaction Agreement.

5.1 Properties

A single instance of POA satisfies the following properties.

► **Property 4** (Agreement). *If two honest validators decide blocks B and B' respectively, then $B = B'$.*

► **Property 5** (Termination). *Every honest validator eventually decides a block.*

► **Property 6** (Fast Termination). *If L is honest, at most p validators misbehave, the system has reached GST, and for every UA-RA transaction $tx \in L.X.pool$ the user who issued tx is honest, then all honest processes decide and stop sending messages in two communication steps.*

► **Definition 7** (Emitted transaction). *We say that a transaction tx is emitted if it is either (i) a user transaction from an actor A signed and broadcast at the moment where the whole system is in the state such that there exists an honest validator $V.A$ who will eventually*

298 *execute a transaction with a sequence number $tx.sn - 1$ and who will eventually own all*
 299 *objects consumed by tx or (ii) produced by a reactive actor at an honest validator.*

300 ► **Property 8 (Validity).** *(I) If a transaction tx is present in the pool of all honest validators*
 301 *at the start of the protocol and L is honest, then tx is included in the decided block. (II) If a*
 302 *transaction is included in the decided block, it was emitted.*

303 ► **Property 9 (No Conflict).** *Conflicting transactions cannot be simultaneously decided within*
 304 *POA instances, even if those correspond to different reactive actors.*

305 5.2 Multi-Instancing

306 **Leader Oracle.** POA is designed to run in multiple instances, and to ensure liveness of
 307 the system, it is essential to have honest leaders. We assume all validators have access to a
 308 common *leaderOracle* function, which given an instance number outputs a leader for that
 309 instance. We require this function to output an honest leader infinitely often. This can
 310 be achieved by a random choice (assuming a common random source) or by a round-robin
 311 approach.

312 **Switching instances.** A validator who decides in a POA instance at time t , broadcasts
 313 their decision along with the proof (in practice it can be a single aggregate signature). By
 314 time $\max(t + \Delta, GST + \Delta)$, every honest validator will receive a proof. Upon receiving such
 315 a valid proof, validators rebroadcast the proof and decide. This mechanism allows for the
 316 following property.

317 ► **Property 10 (Common Termination).** *If an honest validator decides in the k -th POA instance*
 318 *at time t , then every honest validator decides in this instance by at most $\max(t + \Delta, GST + \Delta)$.*

319 The following property guarantees the progress of each validator.

320 ► **Property 11 (Multi-Termination).** *For all honest validators V and reactive actors X , $V.X$*
 321 *eventually decides in the k -th instance of POA for X .*

322 5.3 Algorithm

323 At the start of the protocol, $L.X$ forms a block consisting of all $tx \in L.X.pool$ and broadcasts
 324 it. Upon receiving a block B an honest validator $V.X$ broadcasts its vote plus its own block
 325 (called a *fallback block*) consisting of all transactions $tx \in V.X.pool$. The vote is for B in case
 326 (i) for every UA-RA transaction $tx \in B$, tx is correctly signed, (ii) $V.A$ manages to FP-lock
 327 tx , ensuring there is no conflicting transaction and tx can be executed and (iii) V emitted
 328 every RA-RA transaction from B . Otherwise, $V.X$ broadcasts a negative vote.

329 If at any time a validator $V.X$ receives $n - p$ votes for some block B , $V.X$ decides B , we
 330 call it a fast-path decision. Upon fast-path deciding, a validator broadcasts a proof that
 331 B can be safely decided (in practice, this can be an aggregated threshold signature [47] of
 332 $n - p$ votes). In case a validator does not receive $n - p$ votes in 3Δ time or those votes are
 333 for different blocks, they wait until they have $n - f$ votes and propose in the slow path.

334 The slow path consists of two steps: Quorum Consensus (described in detail in 6.1), fol-
 335 lowed by the parallel Transaction Agreements (described in 6.2) for every UA-RA transaction
 336 decided in Quorum Consensus. A validator proposes to Quorum Consensus according to the
 337 following cases.

Algorithm 1 Parallel Optimistic Agreement on **V.X** (High Level)

```

1: Uses: Outer Links, Inner Links, Quorum Consensus, Transaction Agreement

2: function INITIATE( $k$ ,  $pool$ ) ▷ For Leader
3:    $proposalBlock \leftarrow pool$ 
4:   Broadcast via Outer Links  $proposalBlock$ 

5: upon once  $time \leq 3\Delta$  and received proposal  $B$  do
6:   for all  $tx : \text{UA-RA transaction} \in B$  do ▷ In parallel
7:      $A \leftarrow tx.sender$ 
8:     Request  $V.A$  via Inner Links to FP-lock  $tx$ 

9: upon once all  $V.A$  responded to an FP-lock request do
10:  if all FP-locks are successful then  $Vote \leftarrow B$ 
11:  else  $Vote \leftarrow \perp$ 
12:   $fallBackBlock \leftarrow pool$ 
13:  Broadcast via Outer Links  $\langle Vote, fallBackBlock \rangle$ 

14: upon once exists a block  $B$  with at least  $n - p$  votes do
15:  Decide  $B$  in POA

16: upon once  $Time > 3\Delta$  and exists block  $B'$  with at least  $n - p - 2f$  votes do
17:  for all  $tx : \text{UA-RA transaction} \in B'$  do ▷ In parallel
18:     $A \leftarrow tx.sender$ 
19:    Request  $V.A$  via Inner Links to SP-lock  $tx$ 

20: upon once all  $V.A$  responded to an SP-lock request and all SP-locks succeeded do
21:  Propose  $B'$  to Quorum Consensus

22: upon once  $Time > 3\Delta$  and (received  $n - f$  votes) and (there is no block with  $n - p - 2f$ 
    votes or not all SP-Locks succeeded) do
23:   $B'' \leftarrow$  all transactions present in at least  $n - 2f$  fallback blocks
24:  Attempt to (analogously) SP-lock all UA-RA transactions in  $B''$ 
25:   $B'' \leftarrow B'' \setminus \{\text{transactions that failed to SP-lock}\}$ 
26:  Propose  $B''$  to Quorum Consensus

27: upon event  $\langle \text{decide in Quorum Consensus} \mid B_{qc} \rangle$  do
28:  for all  $tx : \text{UA-RA transaction} \in B_{qc}$  do ▷ In parallel
29:     $A \leftarrow tx.sender$ 
30:    Request  $V.A$  via Inner Links to propose  $tx$  to Transaction Agreement

31: upon once all  $V.A$  responded to an Transaction Agreement request do
32:   $Fails \leftarrow$  all UA-RA transactions from  $B_{qc}$  which  $V.A$  did not decide in Transaction
    Agreement
33:   $B_{POA} \leftarrow B_{qc} \setminus Fails$ 
34:  Decide  $B_{POA}$  in POA

```

Algorithm 2 Parallel Optimistic Agreement on V.A (High Level)

```

1: upon event  $\langle \text{FP-lock request} \mid tx, X \rangle$  do
2:   if a conflicting transaction is FP-locked then respond fail to  $V.X$ 
3:   if execution preconditions for  $tx$  are not met then respond fail to  $V.X$ 
4:   Respond success to  $V.X$ 

5: upon event  $\langle \text{SP-lock request} \mid tx, X \rangle$  do
6:   if a conflicting transaction is SP-locked then respond fail to  $V.X$ 
7:   Respond success to  $V.X$ 

8: upon event  $\langle \text{Transaction Agreement request} \mid tx, X \rangle$  do
9:   Try to SP-Lock  $tx$ 
10:  Propose an SP-Locked transaction with sequence number  $tx.sn$  to Transaction Agreement instance  $tx.sn$  of  $A$ 

11: upon event  $\langle \text{decide in Transaction Agreement} \mid tx', sn \rangle$  do
12:   if  $tx' = tx$  then respond “Transaction Agreement  $sn$  Success” to  $V.X$ 
13:   else respond “Transaction Agreement  $sn$  Failure” to  $V.X$ 

```

- 338 (i) There was some block B for which $V.X$ received at least $n - p - 2f$ votes. In this case,
 339 it is possible that some other validator received $n - p$ votes for B , so $V.X$ attempts
 340 to SP-lock all UA-RA transactions in B , and if it succeeds, proposes B to Quorum
 341 Consensus.
- 342 (ii) If either there was no block for which $V.X$ saw $n - p - 2f$ votes or $V.X$ was not able
 343 to SP-lock some transaction in the block, $V.X$ forms a block to propose to Quorum
 344 Consensus based on the fallback blocks received.

345 In particular, a transaction tx is included in the Quorum Consensus proposal of $V.X$ if
 346 and only if $V.X$ saw tx in at least $n - 2f$ fallback blocks and (in the UA-RA case) was able
 347 to SP-lock tx .

348 After deciding a block B in the Quorum Consensus, for each UA-RA transaction $tx \in B$
 349 from user A , $V.X$ sends tx to $V.A$, who proposes SP-Locks and proposes it to A ’s Transaction
 350 Agreement instance number $tx.sn$. If a conflicting transaction tx' was SP-Locked before,
 351 then tx' is proposed.

352 Upon deciding in the Transaction Agreement instance number $tx.sn$, $V.A$ notifies $V.X$
 353 whether tx was decided or not. After receiving all such notifications, $V.X$ decides on the
 354 block B_{POA} , which is formed from B but omitting those UA-RA transactions which were
 355 not decided in their corresponding Transaction Agreement instances.

356 **Intuition.** The reason to broadcast a fallback block is for verifiers to know the pools of each
 357 other, which would allow for a “good” proposal to Quorum Consensus in case the fast path
 358 fails. More precisely, knowing each other’s pools, verifiers will propose “popular” transactions
 359 to Quorum Consensus, making them committed in the slow path and thus ensuring liveness.

360 The 3Δ threshold consists of Δ for the leader’s broadcast, Δ for verifiers’ votes, and Δ
 361 for the possible shift in times at which the leader and verifier initiate the primitive.

362 One needs a Transaction Agreement after Quorum Consensus to preclude committing
 363 conflicting UA-RA transactions on different reactive actors. Note that if the fast path

succeeds, it ensures that no conflicting transaction can be committed; hence, we only need the Transaction Agreement in case the fast path fails.

We provide a high-level pseudocode for POA for a reactive actor X in Algorithms 1 and 2. For a precise description, please see Appendix D.

6 Slow Path

In this section, we describe the two components of the slow path of POA and POB: Quorum Consensus and Transaction Agreement.

6.1 Quorum Consensus

```
- function PROPOSE( $k, B$ ): start the  $k$ -th instance with proposal  $B$ 
- callback DECIDE( $k, B$ ): decide a block  $B$  in  $k$ -th instance
```

A Quorum Consensus is a partial-synchrony consensus algorithm, meaning it exposes an interface of proposing and deciding a block, and it satisfies Agreement, Termination, and Quorum Validity:

► **Property 12** (Quorum Validity). (I) If a transaction tx is such that tx is in the proposal of every honest validator, then tx is included in the decided block.
 (II) If some transaction tx is included in the decided block, then tx is in the proposal of at least $n - 3f$ honest validators.

▷ **Claim 13.** There exists an algorithm that solves consensus with Quorum Validity.

Proof. The proof applies Theorem 5 and Definition 2 of [21] to Quorum Validity. Throughout the proof we use terms and notation from [21].

Consider some input configuration $c \in \mathcal{I}_{n-f}$. We claim that a block B consisting of transactions that are present in at least $n - 2f$ proposals in $\mathcal{I}_{n-f}$ belongs to $\bigcap_{c' \in \text{sim}(c)} \text{val}(c')$. Consider an input configuration c' with at least $n - f$ elements (if there are less than $n - f$ elements in c' , then any block is admissible). We deduce that $|\pi(c) \cap \pi(c')| \geq n - 2f$, therefore, for each $tx \in B$, tx is present in at least $n - 3f$ proposals of c' , therefore, can be included in the block decided for c' . Conversely, if some transaction is present in every proposal of c' , then it is present in at least $n - 2f$ proposal of c and hence included in B . Thus, $B \in \text{val}(c')$. ◀

In Appendix B we discuss how modern high-throughput BFT protocols could be adapted to instantiate practical high-throughput Quorum Consensus.

6.2 Transaction Agreement

Transaction Agreement is a simple consensus primitive used to provide agreement on which transaction tx should be committed at sequence number sn for a given user A . Though it is possible to agree on this proactively, i.e., prior to submitting a transaction to POA, that would imply an additional latency for a UA-RA transaction under optimistic conditions, hence, MANGROVE does it *retroactively* instead, i.e., after the decision in the Quorum Consensus has been made.

```
- function PROPOSE( $tx$ ): propose transaction  $tx$ 
- callback DECIDE( $tx$ ): decide a transaction  $tx$ 
```

The Transaction Agreement primitive should satisfy the specification of a partially synchronous multi-valued Strong Byzantine Agreement, namely:

- Every process can propose and decide a (not necessarily binary) value.
- *Agreement*. If two honest processes decide v and v' respectively, then $v = v'$.
- *Quorum Validity*. If all honest processes propose the same value, only that value can be decided. Furthermore, if the value is decided, it was proposed by at least $n - 3f$ honest validators.
- *Termination*. Given a partially synchronous network, every correct process eventually decides.

This agreement primitive can be implemented as a special case of Quorum Consensus with blocks of size one.

7 Transaction Processing

7.1 Transaction Execution Properties

First, we informally present several properties of transaction processing in MANGROVE. These are grouped into *correctness* properties, which are common among many distributed systems, *Fast Execution* properties, demonstrating the ability to process transactions with low latency, and *Parallelization* properties, showing the ability to make progress independently at different actors. Full formal definitions as well as proofs of all properties are given in Appendix F.

Correctness Properties. Reactive actors adhere to the Agreement, Validity, Total Order, and Integrity properties of Total Order Broadcast [25], with respect to emission and execution of transactions. User actors instead follow the Agreement, Validity, and Integrity properties of Byzantine Reliable Broadcast [17].

Fast Execution Properties. MANGROVE is designed so that under optimistic conditions, transactions are executed with low latency. Table 1 summarizes conditions needed for a transaction tx of a given type to be executed fast. Those conditions are: *Honest author* (in case of user transactions) — the user who issued a transaction is honest, *synchrony* — the system is after GST, *honest leader* (in case of UA-RA or RA-RA with recipient X) — there exists an honest validator L who will start a POA instance for X as a leader as soon as it has tx in its pool, *good pool* — for every UA-RA transaction $tx' \in L.X.pool$ a user who emitted tx' is honest. The *latency* column shows how many communication steps are needed before every honest validator executes tx . The *resilience* column shows how many misbehaving validators the system can tolerate.

Transaction Type	Honest Author	Synchrony	Honest Leader	Good Pool	Latency	Resilience
UA	✓	✓			2δ	$\leq p$
RA-RA		✓	✓	✓	2δ	$\leq p$
UA-RA	✓	✓	✓	✓	$2\delta^* / 3\delta^\dagger$	$\leq p$

Table 1 Conditions and execution latency for the fast-path of different transaction types. Latency across validators is denoted δ , while latency within a validator is ignored. * When emitted by the leader. $\dagger$ For other validators.

There are instances where the *good pool* condition is not met due to user misbehavior, preventing fast transaction execution. Specifically, this occurs only when honest validators see conflicting transactions (Line 14, Algorithm 6). In such cases, an honest validator will have evidence of the user’s misbehavior (namely, two signed conflicting transactions) and may initiate punishment (e.g. destroy the gas object). We emphasize that users can only affect the liveness of the fast path and in this case, all honest transactions are still committed in the slow path (that is, Validity I of POA holds no matter the user’s misbehavior).

Parallelization Property. Classical blockchain systems address the double-spending problem [42] by totally ordering transactions. While effective, this introduces significant redundancy because many transactions are non-conflicting, meaning they can be executed in any order without affecting the outcome and therefore do not require total ordering.

Mangrove achieves optimal parallelization by ordering only the transactions that require it. It avoids ordering UA transactions entirely since these only create objects at user actors, and such operations are commutative. For reactive actor transactions, Mangrove maintains a partial order by keeping a separate ordered chain for each reactive actor. For example, given two reactive actors X and Y and a set of transactions $\{tx_1^X, \dots, tx_k^X, tx_1^Y, \dots, tx_l^Y\}$ (where tx_i^A is a transaction with receiver A), Mangrove maintains two ordered sets $\{tx_1^X, \dots, tx_k^X\}$ and $\{tx_1^Y, \dots, tx_l^Y\}$ but does not impose an order between these sets.

For a system with a transaction set T and for a reactive actor X , denote $T_X \subseteq T$ the subset of transactions with X as a receiver. The longest ordered chain in Mangrove is then $\max_{X \in RAs} |T_X|$, whereas in classical systems like Bitcoin and Ethereum, the chain length is $|T|$. This length, $\max_{X \in RAs} |T_X|$, is optimal unless additional assumptions are made about reactive actor behavior.

The creation of multiple short chains is beneficial in two ways. First, each chain can be maintained by a separate machine (running V.X) at each validator. This allows throughput to be scaled horizontally. Secondly, the throughput of an application (corresponding to an RA actor) depends solely on the length of its associated chain, and doesn’t degrade when other applications experience high load.

7.2 User Transactions

Each user keeps a sequence number of the last issued transaction for each user actor it controls. When issuing a new transaction tx from a user actor A , a user must first check that A has all owned objects consumed by tx . If a user fails to do so, tx may never be executed, precluding all consecutive transactions from A . Note, though, that this only halts A and not the rest of the system. After a user checks owned objects for tx , it assigns a new sequence number to it, signs it, and broadcasts it to all V.A-s using Parallel Optimistic Broadcast. In Parallel Optimistic Broadcast, a user sends tx to all V.A-s, those attempt to FP-lock it, and if the FP-lock is successful, broadcast a vote for tx . Once a validator obtains $n - p$ votes for tx , it fast-path decides tx , broadcasts a proof and stops sending messages. When unable to decide in the fast-path, validators invoke Transaction Agreement to ensure safety and liveness in case of asynchrony and validators’ misbehavior. For pseudocode, see Appendix C.

For a UA transaction tx from A with a sequence number sn and consumed objects $O_1, \dots, O_k$, it is *executed* if (i) tx is decided in Parallel Optimistic Broadcast, (ii) a transaction from A with a sequence number $sn - 1$ is executed and (iii) A owns $O_1, \dots, O_k$. See the pseudocode for UA transactions in Algorithm 3.

For a UA-RA transaction tx from A to X with a sequence number sn and consumed

Algorithm 3 UA Transaction Processing

```

1: Uses: Parallel Optimistic Broadcast pob
2: upon event  $\langle \text{pob}[A, k].\text{Decide} \mid \text{sender}, tx \rangle$  do ▷ On V.A
3:   if  $k = tx.sn$  and  $\text{VerifySig}(A, tx)$  then
4:      $pending \leftarrow pending \cup \{tx\}$ 
5: upon exists  $tx \in pending$  :  $tx$  is UA and  $executed[tx.sn - 1]$  and
    $tx.consumedObjects \subseteq ownedObjects$  do ▷ On V.A
6:    $pending \leftarrow pending \setminus \{tx\}$ 
7:    $effects \leftarrow \text{VM.Execute}(tx.Code)$ 
8:    $ownedObjects \leftarrow ownedObjects \setminus tx.consumedObjects \cup effects.createdObjects$ 
9:    $executed[tx.sn] \leftarrow true$ 

```

479 objects $O_1, \dots, O_k$, *V.A* sends it to *V.X* if *tx* is correctly signed by *A*, *V.A* have not seen
 480 any other transactions with sequence number *sn*, and (ii) and (iii) hold. *tx* is *executed* as
 481 soon as it is decided in the POA of *X*. Note that execution crucially does not rely on (ii)
 482 and (iii) to hold. We would like to highlight here that UA-RA transactions *do not use* an
 483 agreement mechanism on the sending user actor. See the pseudocode for UA-RA transactions
 484 in Algorithm 4.

Algorithm 4 UA-RA Transaction Processing

```

1: Uses: Outer Links ol, Inner Links il, POA poa
2: upon event  $\langle \text{Emit UA-RA Transaction} \mid A, X, [O_1, \dots, O_k], Code, Call \rangle$  do ▷ On U
3:   if not  $executed[A][sns[A] - 1]$  or  $\{O_1, \dots, O_k\} \not\subseteq ownedObjects[A]$  then
4:     return Error("Not possible to emit")
5:    $tx \leftarrow \text{Sign}(\langle A, sns[A], X, [O_1, \dots, O_k], Code, Call \rangle)$ 
6:    $sns[A] \leftarrow sns[A] + 1$ 
7:   for all  $V \in \mathcal{V}$  do trigger  $\langle ol.Send \mid V, tx \rangle$ 
8: upon event  $\langle ol.Deliver \mid tx : \text{UA-RA Transaction} \rangle$  do ▷ On V.A
9:   if not  $\text{VerifySig}(A, tx)$  or  $FPLocked[tx.sn] \neq \perp$  then return
10:   $FPLocked[tx.sn] \leftarrow tx$ 
11:  await  $executed[tx.sn - 1]$  and  $tx.consumedObjects \subseteq ownedObjects$ 
12:  trigger  $\langle il.Send \mid tx.receiver, tx \rangle$ 
13: upon event  $\langle il.Deliver \mid tx, A \rangle$  do ▷ On V.X
14:   if  $tx \notin executed$  then  $pool \leftarrow pool \cup \{tx\}$ 

```

7.3 Reactive Actor Transactions

485
 486 When a reactive actor *V.X* decides a block, it starts executing transactions of that block in
 487 a deterministic order. Some transactions might create outgoing transactions when executed.
 488 Upon creating an outgoing transaction *tx* that consumes owned objects $O_1, \dots, O_k$, *V.X*
 489 checks its owned objects. If it owns all required objects, *V.X* sends *tx* to the receiver via
 490 inner links, and receiver adds *tx* to the pool. If some objects that transaction consumes are
 491 missing, then this transaction is immediately dropped and has no effect. For the pseudocode,
 492 please see Algorithm 7 in Appendix E.

8 Discussion and Outlook

In general, a transaction may result in a *cascade* of multiple subsequent transactions. Classical systems guarantee that such cascades appear to be executed atomically and in isolation. Moreover, they immediately execute the whole cascade of a transaction after agreeing on the initial transaction, whereas MANGROVE (in the worst case) performs a separate agreement for each individual transaction in the cascade. Therefore, in the case of deep cascades, we expect classical solutions to complete the execution of the cascade faster. Empirical study of the workload types under which either approach performs better is subject to future research.

Finally, we acknowledge that the bit complexity and message complexity of POA are relatively high. However, the primary objective of this work is to demonstrate the feasibility of a system that supports smart contracts while enabling maximal parallelization. Optimizing these complexities is an important consideration, which we leave as future work.

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657 A Model Expressiveness

658 Most common applications can be easily adapted from something resembling Ethereum’s smart
659 contract model to our model with a gain in scalability and without a loss in expressiveness
660 apart from the obvious loss of free atomic composability. For the most part, this is equivalent
661 to how these applications would be designed for the Move VM [15], on the Sui [29] and
662 Aptos [28] blockchains.

- 663 ■ **Token:** A token is primarily defined by a data type for owned objects that adheres
664 to a specific interface. Additionally, a token might have an associated reactive actor
665 responsible for minting new tokens or handling a reserve.
- 666 ■ **Decentralized Exchange:** Each liquidity pool of a decentralized exchange should be
667 its own reactive actor. This allows asynchronous access to different liquidity pools. One
668 popular heavily congested contract does not impede access to any of the other liquidity
669 pools.
- 670 ■ **NFT Marketplace:** The marketplace would be a reactive actor owning all the (NFT)
671 objects currently for sale. Buyers can interact by sending accepted tokens as payment
672 and receiving ownership of the desired object. Sellers can interact by sending it new
673 objects to put up for sale or delisting items, receiving back the object.

674 More generally, we argue the replicated actor model (Section 3) does not lose expressiveness.
675 This can be shown by providing a general framework of translating applications from
676 Ethereum’s smart contract model to our model. However, atomic composability is not
677 inherently guaranteed at the protocol level. If it is intended, it has to be specifically designed
678 into applications and users could be charged additional fees at the application layer for the
679 privilege.

680 **Gas.** To incentivize validators to perform computations, our system uses *gas objects*, a type of
681 owned object. Each transaction needs to consume at least a gas object. As validators process
682 the *Call* and *Code* fields, they are compensated through fees deducted from the provided gas
683 object. The amount of gas required depends on the complexity of the transaction, ensuring
684 fair compensation for resource-intensive tasks. Design and study of specific game-theoretic
685 mechanisms in our system model is outside the scope of this work.

686 **Atomic Composability.** Full atomic composability could be trivially achieved by keeping all
 687 composable state in a single reactive actor. However, this is not realistic when considering an
 688 open, diverse and growing ecosystem of applications. More importantly, it does not make use
 689 of the scalability advantages of our model. We can instead give users the option to request
 690 composability across reactive actors on-demand.

691 **Locking.** To this end we define a *locking* pattern that applications may independently opt
 692 into. Locking is unique in that it allows idle blocking while waiting for other calls to return.
 693 A reactive actor that supports locking has associated state *lockHolder*, *lockCollateral*,
 694 *lockStartTime*, *lockPrice*, and exposes functions *lock()*, *unlock()*, *getLockHolder()*, and
 695 *getLockPrice()*. The locking fee is the product of the current price for locking and the
 696 time the lock is held. The lock is valid until the required fee has exceeded the posted
 697 collateral. The price for locking can be updated by the reactive actor and may depend on
 698 the application as well as current usage statistics. For example, a decentralized exchange
 699 may count accesses or trading volume to a given liquidity pool and set the fee proportional
 700 to its recent popularity.

701 Any *lockPrice* larger than 0 prevents a permanent deadlock on the reactive actor.
 702 However, the application protocol designers need to ensure that at any time the price is
 703 fair, to prevent abuse of this feature. The price for holding a lock could even increase
 704 super-linearly in the time it is held. This would further discourage continuously preventing
 705 others from acquiring the lock.

706 This would require some support on the protocol side as well. At least, each transaction
 707 should receive a timestamp agreed upon by the validators. This would serve as the basis to
 708 determine how long each lock is held. Also, execution of other transactions at that reactive
 709 actor should be delayed until after the lock is released. Maybe with the exception of a call
 710 checking whether a lock is currently being held.

711 **Hard Example: Flash Loan.** Some particularities of the strong atomic transaction model
 712 are not easily translatable. Locking is necessary but not sufficient to enable full atomic
 713 composability. For example, there is no way to implement a flash loan using just the above
 714 locking interface.

715 A flash loan is a loan where there is no risk of default because the loan is only valid
 716 within an atomic and isolated transaction. In this case, the lender needs to be sure that the
 717 entire transaction may only commit if the loan is paid back. If not, it should be reverted
 718 and the loan paid back.

719 **Fully Atomic Transaction Cascades.** Locking can be extended to provide atomic and
 720 isolated execution of entire transaction cascades. To be able to revert transactions, an atomic
 721 transaction execution context is needed. Most importantly, objects stay within the execution
 722 context until the transaction commits. Otherwise, other transactions might be able to see
 723 partial effects of the cascade before it commits. This would also make reversion on abort
 724 impossible without affecting other transactions.

725 Within an atomic transaction context all additional calls that are made are considered
 726 to be atomic and part of the same execution context. These calls need to hold a lock of
 727 the recipient reactive actor. The context is passed along the entire transaction cascade.
 728 Any transaction within an atomic transaction context may only spawn new transactions
 729 within the same context. Locks can only be freed at the end of the transaction (i.e. once
 730 it commits or aborts). Conversely, if any of the locks run out of collateral, the transaction

731 aborts. If a particular transaction aborts, the entire transaction cascade aborts. Importantly,
 732 all consumed objects are returned to the sender.

733 Using this extension of our model even flash loans can be realized. The only additional
 734 thing that is required for safety is that the `lend()` method of the flash loan reactive actor
 735 can indicate that it needs to be called from an atomic execution context and may revert.

736 **B High-Throughput Quorum Consensus**

737 A reactive actor that is at the core of a popular application may experience high contention
 738 over a long time period. Continuously trying to get transactions accepted on the fast-
 739 path in this case inhibits both throughput and latency. On the other hand, continuously
 740 running a chained high-throughput consensus protocol at each reactive actor, where most
 741 instances only produce empty blocks, is a significant and unnecessary burden. To alleviate
 742 this, reactive actors should be able to individually toggle between single-shot POA and a
 743 high-throughput consensus mechanism. This could happen automatically based on certain
 744 heuristics (configured either at the system level or by each RA). Switching from uncontested
 745 to contested mode can be done by deciding a special message in the same manner as any
 746 transaction. Switching from contested back to uncontested mode can be done via the
 747 high-throughput consensus' epoch closing mechanism.

748 Existing high-throughput consensus protocols, like Narwhal & Tusk [23], Bullshark [51],
 749 Shoal/Shoal++ [50, 11] and Mysticeti [12] can be extended to achieve part (II) of Quorum
 750 Validity, which is what differentiates it from regular Validity. For this, a simple consensus
 751 rule can be added. This rule restricts whether an ordered transaction is actually delivered. In
 752 addition to the voting on blocks necessary for ordering, validators directly vote on transactions.
 753 Honest validators vote for a transaction if and only if there are no conflicting transactions in
 754 their pool. Only transactions reaching a threshold of direct votes are delivered for execution.
 755 If this threshold ensures a quorum intersection of at least $f + 1$, no conflicting transactions can
 756 be committed. This is the same rule that is added in MYSTICETI-FPC, to make the general
 757 consensus compatible with the reliable broadcast fast-path allowed for owned-object-only
 758 transactions.

759 **C Parallel Optimistic Broadcast**

760 The Parallel Optimistic Broadcast (POB) primitive has an interface consisting of:

- 761 - **function** BROADCAST(sn, tx): broadcast sn -th transaction
 762 - **callback** DECIDE(sn, tx): decide transaction tx

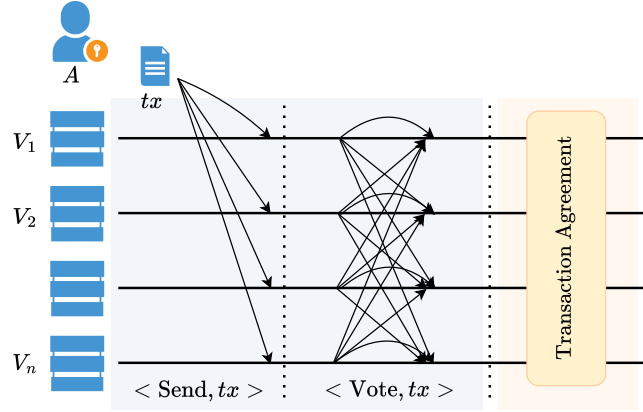
763 To issue a UA transaction tx , user A broadcasts it among all $V.A$ -s. Subsequently, $V.A$ -s
 764 FP-lock tx and vote for it, and if some $V.A$ obtains $n - p$ votes, they can decide tx and stop
 765 sending messages. After receiving $n - p - 2f$ votes for tx , $V.A$ SP-locks tx and proposes it
 766 to a Transaction Agreement instance number $tx.sn$ of A .

Parallel Optimistic Broadcast adheres to the following properties.

767 ► **Property 14 (Agreement).** *If two honest validators decide tx_1 and tx_2 in the same instance*
 768 *of Parallel Optimistic Broadcast, then $tx_1 = tx_2$.*

769 **Proof.** If both validators decide in the Transaction Agreement, the Agreement follows from
 770 the Agreement of Transaction Agreement.

771 If both validators decide in the fast path (here, we also call a decision done after receiving
 772 a proof on Line 25 a fast-path decision), that means that each of them obtained $n - p$ votes



■ **Figure 4** POB scheme. In the fast path (blue rectangle), a user A broadcasts their transaction tx . Then, validators cast their vote. In case the fast path fails, validators participate in the slow path (orange box), which consists of one instance of Transaction Agreement.

773 for tx (Line 19), meaning there is at least one common honest vote, and hence $tx_1 = tx_2$
 774 since no honest validator issues conflicting votes (Line 6).

775 If tx_1 was decided in the fast path, it means it got $n - p$ votes, so no conflicting transaction
 776 can obtain $n - p - 2f$ votes (the intersection is $(n - p) + (n - p - 2f) - n = n - 2p - 2f \geq f + 1$),
 777 hence no honest verifier will propose it to Transaction Agreement, hence, by the Validity
 778 property of the Transaction Agreement, tx_2 can't be decided. ◀

779 ► **Property 15 (Integrity).** *A transaction tx is decided at most once in the given instance*
 780 *and only if it was broadcast by the user.*

781 **Proof.** The only once part is ensured through checks (Lines 14 and 32), and if the user didn't
 782 emit the transaction, it will receive at most f votes, which is not sufficient neither for the
 783 fast path ($n - p > f$), nor to propose it to the Transaction Agreement ($n - p - 2f > f$). ◀

784 ► **Property 16 (Validity).** *If an honest user broadcasts a transaction tx , it is eventually*
 785 *decided.*

786 **Proof.** Since an honest user does not issue conflicting transactions, all honest verifiers will
 787 eventually FP-lock tx (Line 6) and broadcast their vote. Now, if at any time an honest
 788 verifier gets $n - p$ votes, it broadcasts the proof, hence all honest verifiers will eventually
 789 decide. If none of the honest verifiers receive $n - p$ votes, since the user is honest, they
 790 all will eventually get $n - f \geq n - p - 2f$ votes for tx and hence will propose it to the
 791 Transaction Agreement. Therefore, by the Validity property of Transaction Agreement, tx
 792 will be eventually decided in it and hence in Parallel Optimistic Broadcast (Line 34). ◀

793 ► **Property 17 (Fast Termination).** *Given the system is after GST, a user issuing the*
 794 *transaction is honest and at most p validators misbehave, every validator decides and stops*
 795 *sending messages in 2δ time after a user broadcasts its transaction.*

796 **Proof.** Assume an honest user broadcasts a transaction tx at time t . Then, since the system
 797 is after GST, all honest verifiers will receive it, and, since an honest user can not issue
 798 conflicting transactions, will FP-lock it (Line 9) and broadcast their vote for it (Line 12).
 799 Therefore, by the time $t + 2\delta$, every honest verifier will receive at least $n - p$ votes for tx and
 800 will fast-path decide it (Line 19). ◀

Algorithm 5 Parallel Optimistic Broadcast

```

1: Uses: Perfect Links  $ol$ , Transaction Agreement  $ta$ 

2: upon event  $\langle \text{broadcast} \mid tx \rangle$  ▷ On User  $A$ 
3:   for all  $V \in \mathcal{V}$  do
4:     trigger  $\langle ol.Send \mid V.A, tx \rangle$ 

5: upon event  $\langle ol.Deliver \mid A, tx \rangle$  ▷ On  $V.A$ 
6:   if  $FPLocked[tx.sn] \neq \perp$  and  $FPLocked[tx.sn] \neq tx$  then
7:      $vote \leftarrow \text{Sign}(\perp)$ 
8:   else
9:      $FPLocked[tx.sn] \leftarrow tx$ 
10:     $vote \leftarrow \text{Sign}(\text{Vote}(tx))$ 
11:   for all  $V \in \mathcal{V}$  do
12:     trigger  $\langle ol.Send \mid V.A, vote \rangle$ 

13: upon once received  $n - p$  votes for  $tx$  ▷ On  $V.A$ 
14:   if  $pobDecided$  then
15:     return
16:    $proof(tx) \leftarrow \text{aggregate}(n - p \text{ votes})$ 
17:   for all  $V \in \mathcal{V}$  do
18:     trigger  $\langle ol.Send \mid V.A, proof(tx) \rangle$ 
19:   trigger  $Decide(tx)$ 
20:    $pobDecided \leftarrow \text{True}$ 

21: upon event  $\langle ol.Deliver \mid V', proof(tx) \rangle$  ▷ On  $V.A$ 
22:   if  $verify(proof(tx))$  then
23:     for all  $V'' \in \mathcal{V}$  do
24:       trigger  $\langle ol.Send \mid V''.A, proof(tx) \rangle$ 
25:     trigger  $Decide(tx)$ 

26: upon once received  $n - p - 2f$  votes for  $tx$  ▷ On  $V.A$ 
27:   if  $SPLocked[tx.sn] \neq \perp$  and  $SPLocked[tx.sn] \neq tx$  then
28:     return
29:    $SPLocked[tx.sn] \leftarrow tx$ 
30:   trigger  $ta[tx.sn].Propose(tx)$ 

31: upon event  $\langle ta[tx.sn].Decide \mid tx \rangle$  ▷ On  $V.A$ 
32:   if  $pobDecided$  then
33:     return
34:   trigger  $Decide(tx)$ 
35:    $pobDecided \leftarrow \text{True}$ 

```

Algorithm 6 Parallel Optimistic Agreement (Part 1)

```

1: Uses: Outer Links  $ol$ , Inner Links  $il$ , Quorum Consensus  $qc$ , Transaction Agreement  $ta$ 
2: function INITIATE( $k$ ,  $pool$ ) ▷ On  $V.X$ 
3:    $poaInstance \leftarrow k$ 
4:   if  $leaderOracle(k) = V$  then
5:     for all  $V' \in \mathcal{V}$  do  $ol.Send(V'.X, \langle k, B := pool \rangle)$ 
6:    $Timer.Restart()$ 

7: upon event  $\langle ol.Deliver \mid L, \langle k, B \rangle \rangle$  do ▷ On  $V.X$ 
8:   if  $leaderOracle(k) = L$  then  $block[k] \leftarrow B$ 

9: upon once  $poaInstance = k$  and  $block[k] \neq \perp$  and  $Timer \leq 3\Delta$  and
    $\forall tx \text{ RA-RA transaction} \in block[k] : tx \in pool$  do ▷ On  $V.X$ 
10:   $repliesFPLOCK[k] \leftarrow 0$ 
11:   $successFPLOCK[k] \leftarrow true$ 
12:  for all  $tx : \text{UA-RA transaction} \in block[k]$  do ▷ In parallel
13:    trigger  $\langle il.Send \mid FPLOCK(tx), tx.sender \rangle$ 

14: upon event  $\langle il.Deliver \mid FPLOCK(tx), X \rangle$  do ▷ On  $V.A$ 
15:   if not  $VerifySig(tx.sender, tx)$  then
16:     trigger  $\langle il.Send \mid false, X \rangle$ ; return
17:   if  $FPLOCKed[tx.sn] = \perp$  then  $FPLOCKed[tx.sn] \leftarrow tx$ 
18:   if  $FPLOCKed[tx.sn] \neq tx$  then
19:     trigger  $\langle il.Send \mid false, X \rangle$ ; return
20:   if within  $\Delta$  time  $executed[tx.sn - 1]$  and  $tx.objects \subseteq ownedObjects$  then
21:     trigger  $\langle il.Send \mid true, X \rangle$ 
22:   else
23:     trigger  $\langle il.Send \mid false, X \rangle$ 

24: upon event  $\langle il.Deliver \mid status, A \rangle$  do ▷ On  $V.X$ 
25:    $repliesFPLOCK[k] \leftarrow repliesFPLOCK[k] + 1$ 
26:    $successFPLOCK[k] \leftarrow successFPLOCK[k] \wedge status$ 

27: upon once  $repliesFPLOCK[k] == |\{tx : \text{UA-RA transaction} \in block[k]\}|$  do ▷ On  $V.X$ 
28:    $Vote \leftarrow block[k]$ 
29:   if not  $successFPLOCK[k]$  then  $Vote \leftarrow \perp$ 
30:    $B_{fb} \leftarrow pool$ 
31:   for all  $V' \in \mathcal{V}$  do
32:     trigger  $\langle ol.Send \mid [k, Vote, B_{fb}], V'.X \rangle$ 

```

D Parallel Optimistic Agreement (Extended)

This section provides the full pseudocode and proofs showing that Algorithm 6, as presented in Section 5.3, achieves the properties laid out in Section 5.1.

► **Lemma 18.** *Given $tx \in B$ was fast-path decided, no honest validator can SP-Lock a*

Algorithm 6 Parallel Optimistic Agreement (Part 2)

```

33: upon event  $\langle ol.Deliver \mid U, \langle k, \text{Vote}, B_{fb} \rangle \rangle$  do ▷ On  $V.X$ 
34:    $votes[k] \leftarrow votes[k] \cup \{\text{Vote}\}$ 
35:   if  $\text{Vote} \neq \perp \wedge |\{v \in votes[k] \mid v = \text{Vote}\}| = n - p$  then
36:      $proof(B) \leftarrow aggregate(n - p \text{ votes})$ 
37:     for all  $V'' \in \mathcal{V}$  do
38:       trigger  $\langle ol.Send \mid V''.X, proof(B) \rangle$ 
39:     trigger  $\langle poa.Decide \mid k, B \rangle$ 
40:      $fallbackBlocks[k] \leftarrow fallbackBlocks[k] \cup \{B_{fb}\}$ 

41: upon event  $\langle ol.Deliver \mid V', proof(tx) \rangle$  ▷ On  $V.X$ 
42:   if  $verify(proof(tx))$  then
43:     for all  $V'' \in \mathcal{V}$  do
44:       trigger  $\langle ol.Send \mid V''.A, proof(tx) \rangle$ 
45:     trigger  $\langle poa.Decide \mid k, B \rangle$ 

46: upon once  $poaInstance = k$  and  $Timer > 3\Delta$  and  $|votes[k]| = n - f$  do ▷  $V.X$ 
47:   if  $\nexists B : |\{v \in votes[k] \mid v = B\}| \geq n - p - 2f$  then
48:      $needFallbackBlocks \leftarrow true$  return
49:    $candidateB[k] \leftarrow B$  such that  $|\{v \in votes[k] \mid v = B\}| \geq n - 3f$ 
50:    $repliesSPLock[k] \leftarrow 0$ 
51:    $successSPLock[k] \leftarrow true$ 
52:   for all  $tx : \text{UA-RA transaction} \in candidateB[k]$  do ▷ In parallel
53:     trigger  $\langle il.Send \mid SPlock(tx), tx.sender \rangle$ 

54: upon event  $\langle il.Deliver \mid SPlock(tx), X \rangle$  ▷ On  $V.A$ 
55:   if  $SPlocked[tx.sn] = \perp$  then  $SPlocked[tx.sn] \leftarrow tx$ 
56:    $status \leftarrow SPlocked[tx.sn] == tx$ 
57:   trigger  $\langle il.Send \mid status, X \rangle$ 

58: upon event  $\langle il.Deliver \mid status, A \rangle$  ▷ On  $V.X$ 
59:    $repliesSPLock[k] \leftarrow repliesSPLock[k] + 1$ 
60:    $successSPLock[k] \leftarrow successSPLock[k] \wedge status$ 

61: upon once  $repliesSPLock[k] == |\{tx : \text{UA-RA transaction} \in candidateB[k]\}|$  do ▷
   On  $V.X$ 
62:   if  $successSPLock[k]$  then
63:     trigger  $\langle qc.Propose \mid B \rangle$  ; return
64:    $needFallbackBlocks \leftarrow true$ 

```

805 *conflicting transaction* tx' .

806 **Proof.** A validator attempts to SP-lock a UA-RA transaction tx' in four cases. Either
 807 because it received $n - p - 2f$ votes for a block containing tx' (Line 53), because it received
 808 $n - p - 2f$ votes for tx' in Parallel Optimistic Broadcast (Line 29, Algorithm 5), because
 809 it received $n - 2f$ fallback blocks containing tx' (Line 70), or because it decided a block

Algorithm 6 Parallel Optimistic Agreement (Part 3)

```

65: upon once needFallbackBlocks do ▷ V.X
66:    $candidateB_2[k] \leftarrow \{tx \mid |\{B_{fb} \in fallbackBlocks[k] \mid tx \in B_{fb}\}| \geq n - 2f\}$ 
67:    $SPLockedTx[k] \leftarrow \emptyset$ 
68:    $repliesSPLock_2[k] \leftarrow 0$ 
69:   for all  $tx : \text{UA-RA transaction} \in candidateB_2[k]$  do
70:     trigger  $\langle il.Send \mid SPLock_2(tx), tx.sender \rangle$ 

71: upon event  $\langle il.Deliver \mid SPLock_2(tx), X \rangle$  do ▷ On V.A
72:   if  $SPLocked[tx.sn] = \perp$  then  $SPLocked[tx.sn] \leftarrow tx$ 
73:    $status \leftarrow SPLocked[tx.sn] == tx$ 
74:   trigger  $\langle il.Send \mid \langle status, tx \rangle, X \rangle$ 

75: upon event  $\langle il.Deliver \mid \langle status, tx \rangle, A \rangle$  do ▷ On V.X
76:   if  $status$  then
77:      $SPLockedTx[k] \leftarrow SPLockedTx[k] \cup \{tx\}$ 
78:      $repliesSPLock_2[k] \leftarrow repliesSPLock + 1$ 

79: upon once  $repliesSPLock_2[k] == |\{tx : \text{UA-RA transaction} \in candidateB_2[k]\}|$  do ▷ On V.X
80:    $QCPropose \leftarrow SPLockedTx[k] \cup \{tx \in candidateB_2 \mid tx \text{ is RA-RA transaction}\}$ 
81:   trigger  $\langle qc.Propose \mid QCPropose \rangle$ 

82: upon event  $\langle qc.Decide \mid B_{qc} \rangle$  do ▷ On V.X
83:   for all  $tx : \text{UA-RA transaction} \in B$  do
84:      $A \leftarrow tx.sender$ 
85:     trigger  $\langle il.Send \mid UAINitiate(tx), V.A \rangle$ 

86: upon event  $\langle il.Deliver \mid UAINitiate(tx), V.X \rangle$  do ▷ On V.A
87:   if  $SPLocked[tx.sn] = \perp$  then  $SPLocked[tx.sn] \leftarrow tx$ 
88:   trigger  $\langle ta[tx.sn].Propose \mid SPLocked[tx.sn] \rangle$ 

89: upon event  $\langle ta[sn].Decide \mid tx' \rangle$  do ▷ On V.A
90:   if  $tx' = tx$  then trigger  $\langle il.Send \mid \text{"UA success"}, V.X \rangle$ 
91:   else trigger  $\langle il.Send \mid \text{"UA fail"}, V.X \rangle$ 

92: upon once received all Transaction Agreement responses do ▷ On V.X
93:    $B_{POA} \leftarrow B_{qc} \setminus \{tx \mid tx \text{ failed in Transaction Agreement}\}$ 
94:   trigger  $\langle poa.Decide \mid poaInstance, B_{POA} \rangle$ 

```

810 containing tx' in Quorum Consensus (Line 87). We want to show that given some honest
 811 validator Fast-Path decided a block containing tx , none of the above can hold.

812 Let's start with $n - p - 2f$ votes. If a validator received $n - p - 2f$ votes for a block
 813 containing tx' , it means that at least $n - p - 3f \geq p + 1$ honest validators FP-locked tx'

(Line 13). The same argument holds for tx' in Parallel Optimistic Broadcast (Line 9). But those wouldn't then vote for block B that contains tx , since an FP-lock attempt in Line 13 would fail. Hence, no validator can receive $n - p$ votes for B , thus no fast decision of B is possible. A contradiction.

Next, assume that a validator SP-locked tx' due to receiving $n - 2f$ fallback Blocks with tx' . This implies that at least $n - 3f$ honest validators broadcasted a fallback block with tx' and hence at least $n - 3f \geq 2p + 1$ honest validators have tx' in their pool (Line 30), meaning they have $FPLocked[tx.sn] = tx'$ (Line 10) and therefore can not FP-lock tx , and wouldn't vote for a block containing tx . Thus, a Fast-Path decision of a block containing tx is not possible, contradiction.

Finally, assume that a validator SP-locked tx' due to deciding a block containing tx' in Quorum Consensus. By the part (II) of the Quorum Validity property, that means that at least $n - 3f \geq 2p + 1$ honest validators proposed tx' to Quorum Consensus, and hence SP-Locked it for one of the first two reasons (Lines 55 or 72) which we've shown to be impossible given tx was fast-path decided. ◀

Agreement Property. If two validators decide blocks B and B' in the fast path, that means that each of them received at least $n - p$ votes (Line 35), hence there must be at least $(n - p) + (n - p) - n = 3f + 1$ common votes, therefore at least $2f + 1$ honest validators voted for both B and B' meaning $B = B'$ since an honest validator only votes once (Line 27).

Assume two honest validators V and V' decided blocks B and B' respectively in the slow path. By the agreement property of the Quorum Consensus, V and V' decided the same block B_{qc} in Quorum Consensus, hence they have the same set of UA-RA transactions to send to Transaction Agreements and by the Agreement Property of the Transaction Agreement, the same subset S of those was not decided. Thus, $B = B' = B_{qc} \setminus S$.

Therefore, what is left to show is that if an honest validator V decides B in the fast path and another honest validator decides B' in Quorum Consensus, then $B = B'$.

If V decides B in the Fast Path, it means that it received $n - p$ votes for B . Hence among every $n - f$ votes there will be at least $n - p - 2f$ votes for B . We would like to show that every honest validator will propose B to Quorum Consensus, and hence B will be decided in Quorum Consensus.

To do so, we need to show that a condition in Line 62 will hold, namely that every UA-RA transaction $tx \in B$ will be successfully SP-locked. We show it by showing that no conflicting transaction tx' can be SP-locked.

So every honest validator will propose B to the Quorum Consensus. Denote with B_{qc} a block decided in Quorum Consensus. By the condition (I) of Quorum Validity, if tx is in the proposal of every honest validator, then tx is in the decided block, that is $tx \in B \rightarrow tx \in B_{qc}$. Denote with $S \subset B_{qc}$ a subset of UA-RA transactions in B_{qc} that were not decided in the corresponding Transaction Agreement. We will show that $tx \in B \rightarrow tx \notin S$. Indeed, assume $tx \in B$. Then, by Lemma 18, all honest validators will propose it (Line 88) to the Transaction Agreement, and by the Quorum Validity of the Transaction Agreement tx will be decided. This allows us to conclude that $B \subseteq B_{qc} \setminus S = B'$

Next, note that $B_{qc} \subseteq B$. Indeed, by condition (II) of Quorum Validity, if tx is in B_{qc} , then it was proposed by at least $n - 3f \geq 1$ honest validators, and hence, as we've showed that every honest validator proposes B , tx must be in B . This gives us $B' = B_{qc} \setminus S \subseteq B_{qc} \subseteq B$ ◀

Termination Property. There will either be an honest validator that received $n - p$ votes for some block B , or there will be not. In case there will be, it will broadcast the proof, hence every honest validator will eventually receive it and will eventually decide and stop

861 sending messages. If none of the honest validators ever receive $n - p$ votes, we argue by the
862 termination of a slow path:

863 By 3Δ time after the start of the instance (Line 46) an honest validator will propose to
864 the Quorum Consensus (Line 63 or 81). They eventually decide in the Quorum Consensus
865 by the Termination property of Quorum Consensus and will propose to multiple Transaction
866 Agreements (Line 85). By the Termination property of the Transaction Agreement, all
867 instances will terminate and a validator will decide in POA (Line 94). ◀

868 **Fast Termination Property.** Let's consider some honest validator V . Given the system is
869 in the synchrony period, by the Common Termination property, $L.X$ will start the instance
870 at most Δ time after $V.X$ started and hence $L.X$'s proposal B will reach $V.X$ at most 2Δ
871 time after $V.X$ started. For every UA-RA transaction $tx \in B$, by assumption, a user who
872 emitted tx is honest, and hence V will successfully FP-lock tx since there is no conflicting
873 transaction and since V will be ready to execute tx by the time 2Δ by Lemma 34. Also, by
874 Lemma 33, for every RA-RA transaction $tx \in B$ V will emit tx at most Δ time after L did.
875 Hence $V.X$ will issue a vote for B .

876 Therefore, due to synchrony, and by the assumption that at most p validators misbehave,
877 every honest validator will acquire $n - p$ votes for B within 3Δ time after its own start and
878 will Fast-Path decide B . ◀

879 **Validity Property.** For simplicity, we only consider the validity of a block decided in the
880 Slow Path, since by the Agreement Property, it's the same block as the one decided in the
881 Fast Path.

882 Consider a block B decided in the Slow Path. Let's first prove condition (I) of the Validity
883 Property: If a transaction tx is present in the pool of all honest validators at the start of the
884 protocol and L is honest, then tx is included in B .

885 Consider such tx . An honest validator $V.X$ proposes to the Quorum Consensus either a
886 block B_1 for which V received at least $n - p - 2f$ votes (Line 63) or a block B_2 consisting
887 of transactions that were present in $n - 2f$ fallback blocks (Line 81). Since L is honest, B_1
888 is its proposal, and it contains tx . So does B_2 because among every $n - f$ fallback blocks
889 there will be at least $n - 2f$ blocks from honest validators and each such block contains
890 tx (by condition to form a Quorum Consensus proposal from fallback blocks at Line 66).
891 Therefore, every honest validator's proposal to Quorum Consensus will contain tx , and by the
892 (I) condition of a Quorum Validity tx will be in the decided block B_{qc} of Quorum Consensus.
893 If tx is an RA transaction, it will trivially be in the decided block, so assume tx is a UA-RA
894 transaction. After deciding B_{qc} , every honest validator will propose tx to the corresponding
895 Transaction Agreement (Line 88), since no conflicting transaction can be SP-Locked since
896 an honest user doesn't issue conflicting transactions. Therefore, tx will be decided in its
897 Transaction Agreement instance by the Quorum Validity, and hence be included in B .

898 Now let's prove condition (II) of Validity, namely that if a transaction is included in the
899 decided block, it was emitted.

900 Consider some $tx \in B$. By condition (II) of Quorum Validity, tx is in the proposal of at
901 least $n - 3f \geq 1$ honest validators, and an honest validator proposes a UA-RA transaction tx
902 to Quorum Consensus only if it SP-locked tx (lines 53, 63 or 70, 81), which is only possible
903 if $n - 3f \geq 1$ honest validators have tx in their pool which implies (Line 11) that this
904 transaction was emitted. And an honest validator proposes an RA transaction only if it was
905 present in $n - 2f$ fallback blocks (Line 80), meaning at least $n - 3f \geq 1$ honest validators
906 included it in their fallback blocks, meaning they have it in their pool (Line 30), meaning
907 emitted it (Line 13, Algorithm 4). ◀

908 **No Conflict Property.** For the sake of contradiction, assume that there were POA instances
 909 POA_1 and POA_2 in which blocks B_1 and B_2 were decided, containing respectively tx_1 and
 910 tx_2 , which are conflicting. Now, either one of those blocks were decided in the fast path or
 911 none were.

912 Consider the case where w.l.o.g. B_1 was decided in the fast path. This means that at least
 913 $n - p - f$ honest validators FP-locked tx_1 , and hence B_2 can receive at most $2f + p < n - p$
 914 votes, hence can not be fast-path decided. Moreover, given tx_1 was fast-path decided, by
 915 Lemma 18 no honest validator can SP-Lock tx_2 , therefore, no honest validator proposes tx_2
 916 to the Transaction Agreement instance number $tx_2.sn$, therefore, by the Quorum Validity of
 917 Transaction Agreement, tx_2 can not be decided in the Transaction Agreement, and hence in
 918 the slow path.

919 Finally, assume that both B_1 and B_2 were decided in the slow path. But this implies that
 920 tx_1 and tx_2 were both decided in the Transaction Agreement instance number $tx_1.sn$ for
 921 user $tx_1.sender$ (which are the same values as $tx_2.sn$ and $tx_2.sender$), which is not possible
 922 due to the agreement property of Transaction Agreement. ◀

923 **E** Pseudocode for Transaction Execution

Algorithm 7 Transaction Execution (UA-RA and RA-RA)

```

1: upon event  $\langle \text{once poa.Decide} \mid k, B \rangle$  do ▷ On  $V.X$ 
2:    $pool \leftarrow pool \setminus B$ 
3:   for all  $tx \in \text{DeterministicOrder}(B)$  do
4:     if  $tx \in \text{executed}$  then continue
5:      $executed \leftarrow executed \cup \{tx\}$ 
6:      $effects \leftarrow \text{VM.Execute}(tx.Code_{pre}, tx.consumedObjects)$ 
7:      $effects \leftarrow \text{VM.Execute}(tx.Call, effects)$ 
8:      $effects \leftarrow \text{VM.Execute}(tx.Code_{post}, effects)$ 
9:     for all  $raratx \in effects.raratxs$  do
10:      if  $raratx.consumedObjects \not\subseteq ownedObjects$  then
11:        continue
12:       $ownedObjects \leftarrow ownedObjects \setminus raratx.consumedObjects$ 
13:      trigger  $\langle \text{il.Send} \mid raratx.receiver, raratx \rangle$ 
14:      if  $tx$  is UA-RA then
15:        trigger  $\langle \text{il.Send} \mid tx.sender, Executed(tx, effects) \rangle$ 
16:       $poa.Initiate(k + 1)$ 

17: upon event  $\langle \text{il.Deliver} \mid \langle Executed(tx), effects \rangle, V.X \rangle$  do ▷ On  $V.A$ 
18:   if  $executed[tx.sn]$  then return
19:   await  $executed[tx.sn - 1]$  and  $tx.consumedObjects \subseteq ownedObjects$ 
20:    $ownedObjects \leftarrow ownedObjects \setminus tx.consumedObjects \cup effects.createdObjects$ 
21:    $executed[tx.sn] \leftarrow \text{true}$ 

```

924 **F** System Analysis

925 **F.1** Formal Correctness Properties

926 Properties for reactive actors follow the schema of Total Order Broadcast [25].

927 ► **Property 19** (Reactive Actor Agreement). *For any honest validators V_1 and V_2 , a reactive*
 928 *actor X and a transaction tx , if $V_1.X$ executes tx , then $V_2.X$ eventually executes tx .*

929 ► **Property 20** (Reactive Actor Validity). *If an honest user emits a UA-RA transaction, it is*
 930 *eventually executed by all correct validators.*

931 *If a reactive actor on any honest validator emits an RA-RA transaction, it is eventually*
 932 *executed by all correct validators.*

933 ► **Property 21** (Reactive Actor Total Order). *For any reactive actor X , honest validators*
 934 *V_1, V_2 , and transactions tx_1, tx_2 , if $V_1.X$ executes tx_1 before tx_2 , then $V_2.X$ executes tx_1*
 935 *before tx_2 .*

936 ► **Property 22** (Reactive Actor Integrity). *For any reactive actor X , honest validator V and*
 937 *transaction tx , $V.X$ executes tx at most once and only if tx was emitted.*

938 User actor properties follow the schema of Byzantine Reliable Broadcast [17].

939 ► **Property 23** (User Actor Validity). *If a correct user emits a user actor transaction, this*
 940 *transaction is eventually executed by every honest validator.*

941 ► **Property 24** (User Actor Integrity). *Every correct validator executes each user actor*
 942 *transaction at most once and only if it was emitted.*

943 ► **Property 25** (User Actor Agreement). *For any user actor A , honest validators V_1, V_2 and*
 944 *user actor transactions tx_1, tx_2 both with sender A and the same sequence number, if $V_1.A$*
 945 *executes tx_1 and $V_2.A$ executes tx_2 , then $tx_1 = tx_2$.*

946 **F.2** Formal Fast Execution Properties

947 ► **Property 26** (Fast UA Transaction Execution). *Given an honest user A issues a UA*
 948 *transaction tx , the system is after GST, and at most p validators are faulty, tx is executed*
 949 *after 2 communication steps.*

950 ► **Property 27** (Fast UA-RA Transaction Execution). *Given an honest user A issues a UA-RA*
 951 *transaction tx to a reactive actor X , the system is after GST, the leader L of the next POA*
 952 *instance of X is honest and starts the instance as soon as it receives a transaction from A ,*
 953 *and at most p validators misbehave, then tx is executed after 3 communication steps.*

954 ► **Property 28** (Fast RA-RA Transaction Execution). *Given a reactive actor issues an RA*
 955 *transaction tx to a reactive actor Y , the system is after GST, the leader L of the next POA*
 956 *instance of Y is honest and starts the instance as soon as it receives a transaction from X ,*
 957 *and at most p validators misbehave, then tx is executed after 2 communication steps.*

958 **F.3** Proofs for All System Properties

959 **Reactive Actor Agreement.** If $V_1.X$ executes tx , it means that it decided a block B con-
 960 taining tx . Assume $V_1.X$ decided B in the k -th instance of POA. By the Multi-Termination
 961 and Agreement properties of POA, $V_2.X$ will eventually decide in the k -th instance of POA
 962 for X and its decision will be B . Therefore, $V_2.X$ will also eventually execute tx . ◀

963 ► **Corollary 29** (Reactive Actor Agreement). *For two honest validators V_1 and V_2 , and a*
 964 *reactive actor X , if $V_1.X$ emits tx , then $V_2.X$ eventually emits tx .*

965 **Proof.** Let tx' be a transaction executing a *Call* of which made $V_1.X$ emit tx . By the
 966 Reactive Actor Agreement property, $V_2.X$ will eventually execute tx' having the same state
 967 and the same set of owned objects as $V_1.X$ had when executing tx' . Therefore, $V_2.X$ will
 968 also emit tx . ◀

969 ► **Remark 30.** Definition 7 is independent of a validator since if a transaction was emitted by
 970 a reactive actor of one validator, by Corollary 29 of the Reactive Actor Agreement property,
 971 every honest validator will eventually emit it.

972 ► **Definition 31.** *Consider an execution E and two honest validators V_1 and V_2 . We define*
 973 *a direct ancestor according to V_1 relation for two transactions tx_1 and tx_2 executed by V_1*
 974 *in E the following way: tx_1 is a direct ancestor of tx_2 if either (i) tx_1 and tx_2 are emitted*
 975 *by the same user actor and $tx_1.sn = tx_2.sn - 1$ or (ii) tx_2 consumes objects created by tx_1 .*
 976 *Define an ancestor relation as a transitive closure of a direct ancestor relation.*

977 ► **Lemma 32.** *Consider two honest validators V_1 and V_2 and execution E . If V_1 executes*
 978 *some transaction tx at time t in E and V_2 executes all ancestors of tx according to V_1 by at*
 979 *most $\max(t + \Delta, GST + \Delta)$ then V_2 executes tx by at most $\max(t + \Delta, GST + \Delta)$.*

980 **Proof.** In case tx is either UA-RA, RA-RA or RA, this follows from the Reactive Actor
 981 Agreement and Common Termination properties without a need for the ancestor premise.
 982 Therefore, we focus on the case of tx being a UA transaction. Denote $A := tx.sender$ and tx'
 983 a transaction with $sender = A$ and $tx'.sn = tx.sn - 1$. Note that if V_1 executed tx , it means
 984 it decided it in Parallel Optimistic Broadcast (Line 2, Algorithm 3), meaning V_2 will also
 985 eventually decide it in Parallel Optimistic Broadcast and will put it into *pending* (Line 4).
 986 And V_2 will be ready to execute tx (Line 5) by the time of at most $\max(t + \Delta, GST + \Delta)$
 987 since by the state of the Lemma, by that time V_2 will execute all ancestors of tx . ◀

988 ► **Lemma 33.** *If an honest validator executes a transaction tx at time t , then every honest*
 989 *validator executes tx at time at most $\max(t + \Delta, GST + \Delta)$.*

990 **Proof.** For UA-RA and RA-RA transactions, this follows from the Reactive Actor Agreement
 991 and Common Termination properties. We now give proof for UA transactions.

992 For the sake of contradiction, consider an execution E of the protocol, two honest
 993 validators V_1 and V_2 , and a UA transaction tx such that in E V_1 executes tx at time t and
 994 V_2 does not execute tx by $\max(t + \Delta, GST + \Delta)$.

995 By Lemma 32, if V_1 executes tx but V_2 does not, it means that there is a transaction that
 996 is an ancestor of tx according to V_1 that is not executed by V_2 . Repeat the proof process for
 997 that ancestor. Since there is a finite number of ancestors of each transaction and an ancestor
 998 relation is transitive, we end up with an ancestor of tx that is not executed by the time
 999 $\max(t + \Delta, GST + \Delta)$ but all its ancestors are, which contradicts Lemma 32. ◀

1000 ► **Lemma 34.** *Consider a user actor A controlled by honest user U and a transaction tx*
 1001 *from A .*

1002 *If U emits tx at time t , then for every honest validator V , $V.A$ will have executed $[tx.sn - 1]$*
 1003 *and $tx.objects \subseteq ownedObjects$ by $\max(t + \Delta, GST + \Delta)$.*

1004 **Proof.** Since U is honest and emits tx , we conclude that U saw effect of some transactions
 1005 $tx_1, \dots, tx_k$ that made $executed[A][tx.sn]$ and $tx.objects \subseteq objects[A]$ hold. It means that

1006 $\forall i \in [k]$ U received at least $f + 1$ votes for tx_i , meaning there is at least one honest process
 1007 which executed tx_i , which by Lemma 33 implies that every honest validator will execute tx_i
 1008 by $\max(t + \Delta, GST + \Delta)$. Therefore, for every honest validator $V.A$ $executed[tx.sn - 1]$ and
 1009 $tx.objects \subseteq ownedObjects$ will hold by $\max(t + \Delta, GST + \Delta)$. ◀

1010 **Reactive Actor Validity.** First, consider an honest user U issues a UA-RA transaction tx to
 1011 a reactive actor X . Since U is honest, checks in Line 9 of Algorithm 4 will pass and each
 1012 honest validator will put tx into its *pending* set. Moreover, by Lemma 34, a condition in
 1013 Line 11, Algorithm 4 will eventually hold for every honest $V.A$ and it will send tx to $V.X$
 1014 (Line 12). So, tx will eventually end up in the pool of every honest validator (Line 14), let's
 1015 denote this time point with t . Now consider a point in time after t and after GST when
 1016 an honest validator L becomes a leader of POA for X . If by this time L already executed
 1017 tx , then by the Reactive Actor Agreement tx will be eventually executed by every honest
 1018 validator. Otherwise, L will include tx in its proposal and by the (I) part of the Validity
 1019 property of POA, tx will be decided and then executed (Lines 6 and 7).

1020 Now, we give a prove for an RA-RA transaction from a reactive actor X to a reactive
 1021 actor Y . Corollary 29 states that if for some honest validator V_1 , $V_1.X$ emitted tx , then
 1022 for every other honest validator V_2 , $V_2.X$ will eventually emit tx . Therefore, tx will end up
 1023 in the pool of $V.Y$ for every honest validator V , and by the same logic as with a UA-RA
 1024 transaction, tx will be eventually executed by every honest validator. ◀

1025 **Reactive Actor Total Order.** A reactive actor validator executes a transaction only if it
 1026 decides a block in POA containing this transaction.

1027 Let B_1 be the block containing tx_1 and k_1 be the number of POA instance in which B_1
 1028 is decided. Analogously we define B_2 and k_2 for tx_2 .

1029 Given $V_1.X$ executed tx_1 before tx_2 and since processes execute blocks sequentially, we
 1030 conclude that $k_1 \leq k_2$. If now $k_1 < k_2$, then $V_2.X$ executes tx_1 before tx_2 because of the
 1031 sequential execution of blocks. And if $k_1 = k_2$, then $B_1 = B_2$, and this block is executed in
 1032 the same order by $V_1.X$ and $V_2.X$ due to the deterministic block execution. ◀

1033 **Reactive Actor Integrity.** If tx is executed by $V.X$, it means that $V.X$ decided a block
 1034 containing tx . $V.X$ can decide either on the Fast Path (Line 39, Algorithm 6) or on the slow
 1035 path (Line 94, Algorithm 6).

1036 If a block containing tx is decided on the fast path, it means it received at least $n - p - f \geq 1$
 1037 honest votes (Line 35), meaning it passed the checks of an honest validator. In case tx
 1038 is a UA-RA transaction, this means that tx is correctly signed by a user (Line 15) and a
 1039 validator successfully FP-locked tx (Line 13), meaning it has $executed[tx.sn - 1] = true$
 1040 and $tx.objects \subseteq ownedObjects$ (Line 20), therefore tx is emitted. In case tx is an RA-RA
 1041 transaction, it means that it is contained in the pool of an honest validator (Line 9), hence it
 1042 was issued by a reactive actor of an honest validator, and hence it is emitted.

1043 If tx is included in the block decided on the slow path, then by the (II) part of Quorum
 1044 Validity, there are $n - 3f \geq 1$ honest validators who proposed a block containing tx to the
 1045 Quorum Consensus. An honest validator includes tx in its proposal either if it received
 1046 $n - p - 2f$ votes for the block containing tx (Line 63) or if it received $n - 2f$ fallback
 1047 blocks containing tx (Line 81). In case it received $n - p - 2f$ votes, there were at least
 1048 $n - p - 3f \geq p + 1$ honest votes for a block containing tx , which by the argument above implies
 1049 that tx is emitted. In case it received $n - 2f$ fallback blocks containing tx , it means that at
 1050 least $n - 3f \geq 1$ honest validators included tx into their fallback block, meaning tx was in
 1051 their pool, meaning it was either sent by a reactive actor (Line 13, Algorithm 4) and thus
 1052 emitted, or it was sent by a user actor (Line 12, Algorithm 4) and hence checked for a correct

1053 user signature (Line 9) and for $executed[tx.sn - 1] = true$ and $tx.objects \subseteq ownedObjects$
 1054 (Line 11) and thus emitted.

1055 Every transaction is executed at most once by a reactive actor since it maintains an
 1056 *executed* set and skips a transaction if it was executed already (Line 4, Algorithm 4). ◀

1057 **User Actor Validity.** Consider an emitted transaction tx issued by user A with $tx.sender =$
 1058 A . Given that A is honest, by the Validity Property of Parallel Optimistic Broadcast, tx will
 1059 eventually be decided in the Parallel Optimistic Broadcast and will end up in a *pending* set
 1060 of every honest validator (Line 4, Algorithm 3). And by Lemma 34, for every honest $V.A$
 1061 $executed[tx.sn - 1]$ and $tx.objects \subseteq ownedObjects$ will eventually hold (Line 5) and thus
 1062 $V.A$ will execute tx (Line 7). ◀

1063 **User Actor Integrity.** A correct validator executes a transaction only if it previously put
 1064 it into a *pending* set (Line 5, Algorithm 3). A correct validator puts a transaction into a
 1065 *pending* set only if it delivers it in a Parallel Optimistic Broadcast instance (Line 4). By the
 1066 Integrity property of the Parallel Optimistic Broadcast, at most one transaction with a given
 1067 sequence number will be decided in the given instance, and hence, at most one transaction
 1068 with a given sequence number will be executed.

1069 Furthermore, a transaction is put in the *pending* set only if it is correctly signed and is
 1070 executed only if the condition in Line 5 holds, meaning only if a transaction is emitted. ◀

1071 **User Actor Agreement.** We consider all possible cases for tx_1 and tx_2 to be either UA or
 1072 UA-RA transactions.

1073 In case both tx_1 and tx_2 are UA transactions, we can conclude that $V_1.A$ and $V_2.A$
 1074 delivered them in the same Parallel Optimistic Broadcast instance, hence $tx_1 = tx_2$ by the
 1075 Agreement property of Parallel Optimistic Broadcast.

1076 If tx_1 and tx_2 are both UA-RA transactions, we conclude that they were both decided in
 1077 the POA and hence, due to the No Conflict property of POA, $tx_1 = tx_2$.

1078 Finally, it can not be that tx_1 is a UA transaction, and tx_2 is a UA-RA transaction.
 1079 That is because, given Agreement properties of Parallel Optimistic Broadcast and POA, we
 1080 can assume that both tx_1 and tx_2 were decided in the slow path, that is in the instance
 1081 number $tx_1.sn$ (same as $tx_2.sn$) of Transaction Agreement of A . But then $tx_1 = tx_2$ by the
 1082 Agreement property of Transaction Agreement.

1083 ◀

1084 **Fast UA Transaction Execution.** Each honest validator will terminate the Byzantine Reli-
 1085 able Broadcast of tx in two communication steps. And by Lemma 34, every honest validator
 1086 will be ready to execute tx by that time. ◀

1087 **Fast UA-RA Transaction Execution.** The first communication step is a user's broadcast of
 1088 tx , so, in particular, L receives it. Then we apply the Fast Termination property of POA
 1089 which adds two additional communication steps. ◀

1090 **Multi-termination.** Due to the Termination property of POA, it's sufficient to show that
 1091 $V.X$ will initiate k -th instance. This we prove by induction on k .

1092 The first POA instance is initiated immediately when the reactive actor entity is initialized.
 1093 Now, assume a validator decides in the $k - 1$ instance. This would trigger a $poa.Decide(k - 1, \cdot)$
 1094 event (Line 1, Algorithm 4) and thus a $poa.Initiate(k)$ event (Line 16). ◀