

Prof. R. Wattenhofer

Towards better graph generative models and globally accurate evaluation metrics

Graph generation is an interesting problem which is encountered when trying to generate novel molecules or proteins with desired properties or variations of social graphs that used to test hypotheses in social sciences. However, graph generation is a challenging problem due to the nonuniqueness of graphs and the complex non-local dependencies between their edges. Adding to this complexity, it is very challenging to compare different graph generation models. Typically, comparing graph distributions is performed by computing and comparing some statistics that are invariant to node permutations [10, 12, 14]. We believe that the existing statistics are insufficient because they are all based on local graph features and none of them are designed to



capture non-local graph properties such as the diameter of a graph, its coarse structure or its general spectral properties.

In this project, we will investigate new measures that are effective for capturing global graph properties. To do so, we take inspiration from the unpublished work [11, Chapter 3.2] where general graph spectral features are defined. The student tasks will include 1. designing experiments and datasets emphasizing the shortcomings of existing metrics, 2. developing the theory of [11, Chapter 3.2] from the perspective of graph distribution comparison 3. developing better graph generative models and 4. an experimental comparison to existing models and metrics [3, 8, 15, 2, 16, 6, 13, 1, 7, 5, 9, 4].

To develop a better graph generation model, we will aim to create a denoising generative model, which can better capture those global properties of the graph. We hope to achieve this, by generating a graph in a latent space of a graph auto encoder, similarly to what is done for high-definition image generation. The latent space would likely be represented as a set of embeddings, those could potentially be made hierarchical. The developed models would be evaluated on larger molecule, protein and potentially other graph generation (e.g. object meshes) tasks, to confirm better performance on larger graphs compared to existing models.

Requirements: Strong motivation, knowledge in deep learning, or a solid background in machine learning. Experience with Python and PyTorch or TensorFlow is an advantage as well as knowledge in graph theory, generative models and graph neural networks.

Interested? Please contact us for more details!

Contact

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