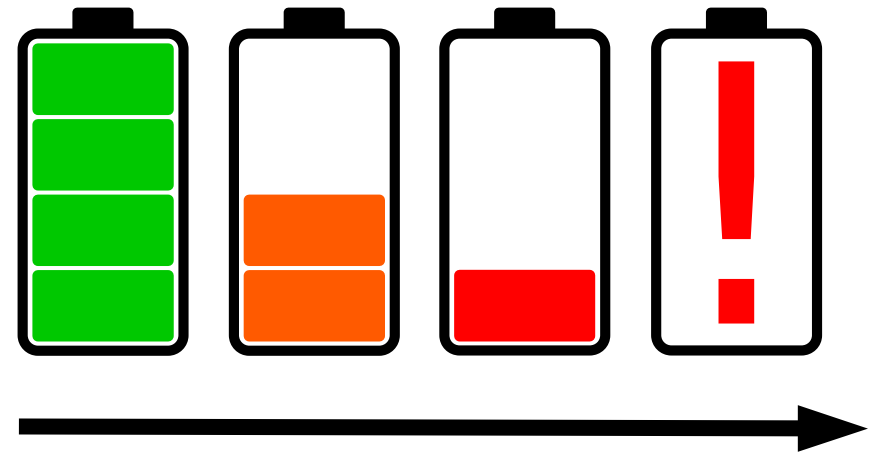
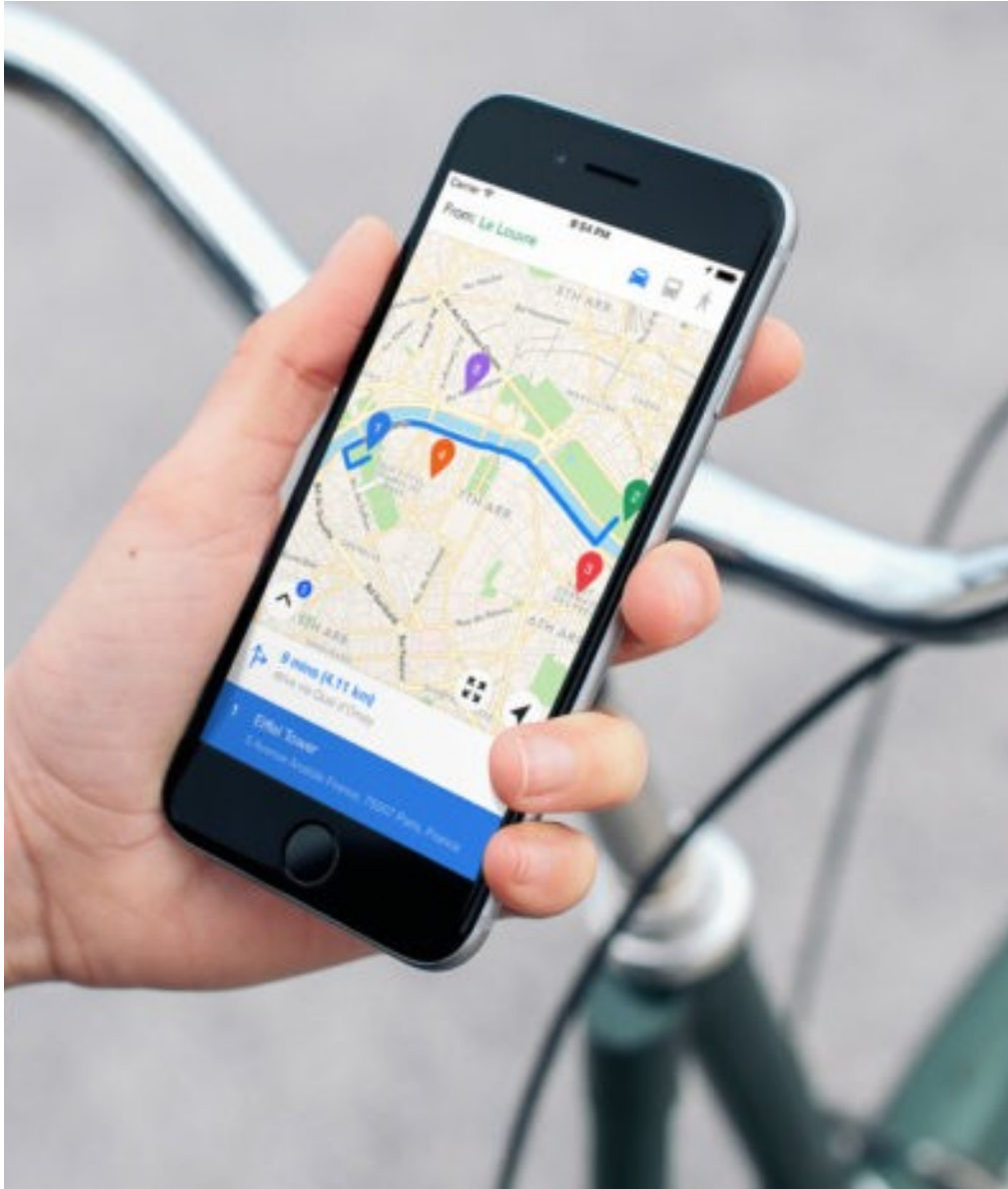


Fast and Robust GPS Fix Using One Millisecond of Data

*Pascal Bissig, Manuel Eichelberger, Roger Wattenhofer
IPSN 2017 – Pittsburgh*

Problem 1

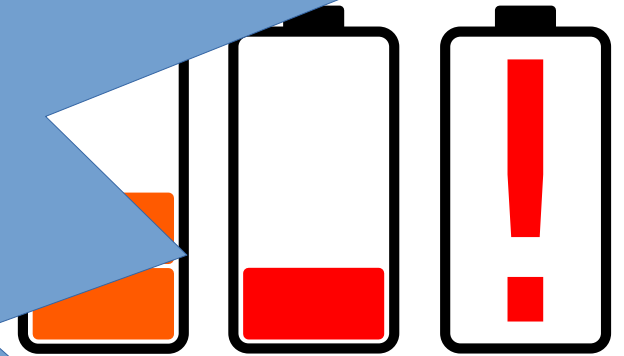


~~1 day~~
with GPS: 6 hours

Problem 1



Start here



~~1 day~~
with GPS: 6 hours

Problem II



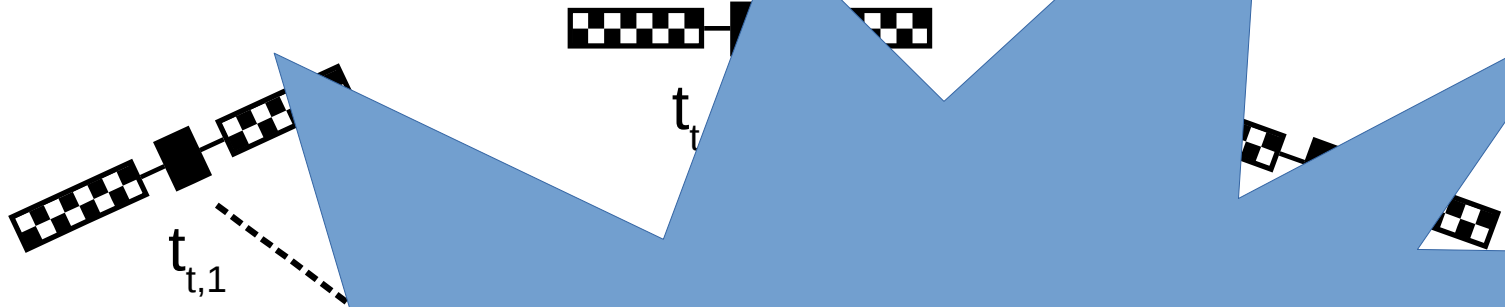
$t = 1 \text{ ms}$

$t = 0$: trigger \rightarrow GPS starts

$t = 30 \text{ s}$: position fix

time

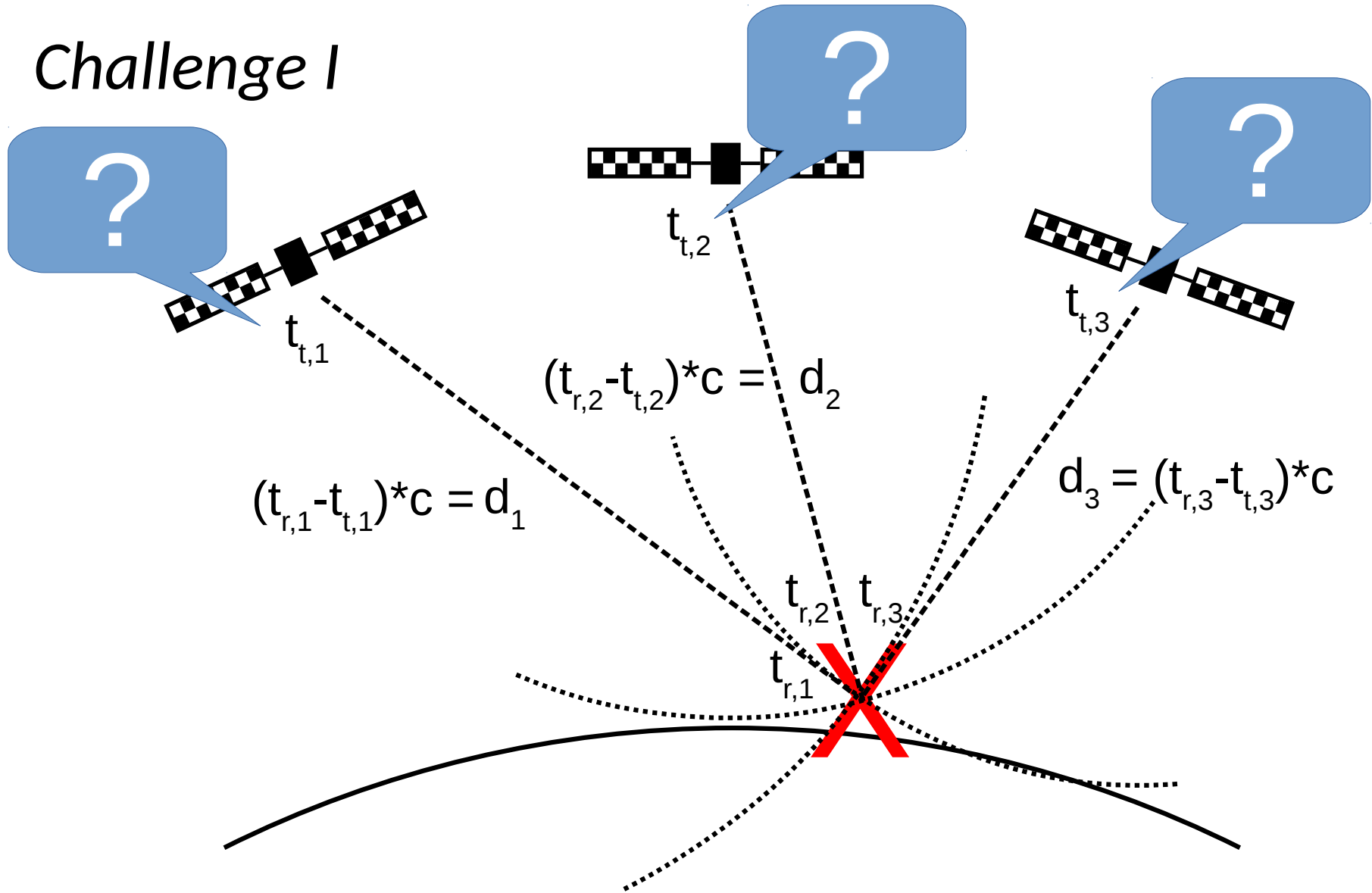
GPS on one slide



Why are people still doing research on this topic?

$$\|p_r - p_{s,i}\|_2 + \Delta t * c = (t_{r,i} - t_{t,i}) * c$$

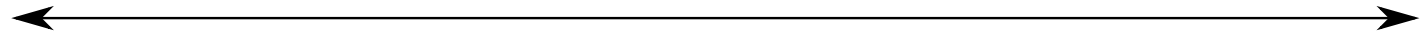
Challenge I



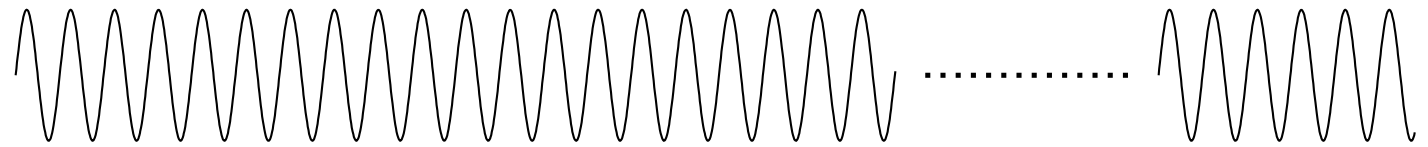
$$\|p_r - p_{s,i}\|_2 + \Delta t * c = (t_{r,i} - t_{t,i}) * c$$

GPS signals

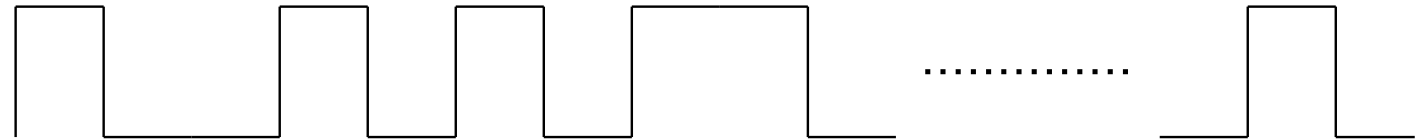
1 ms



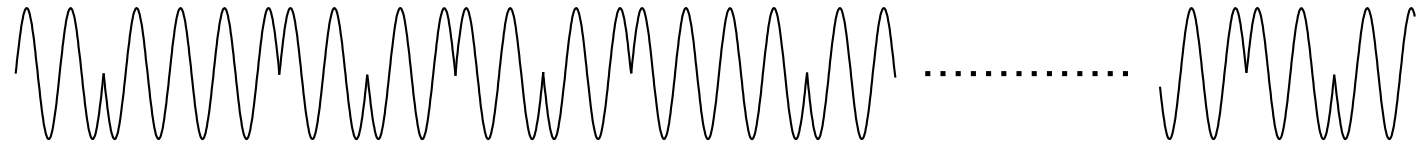
Carrier



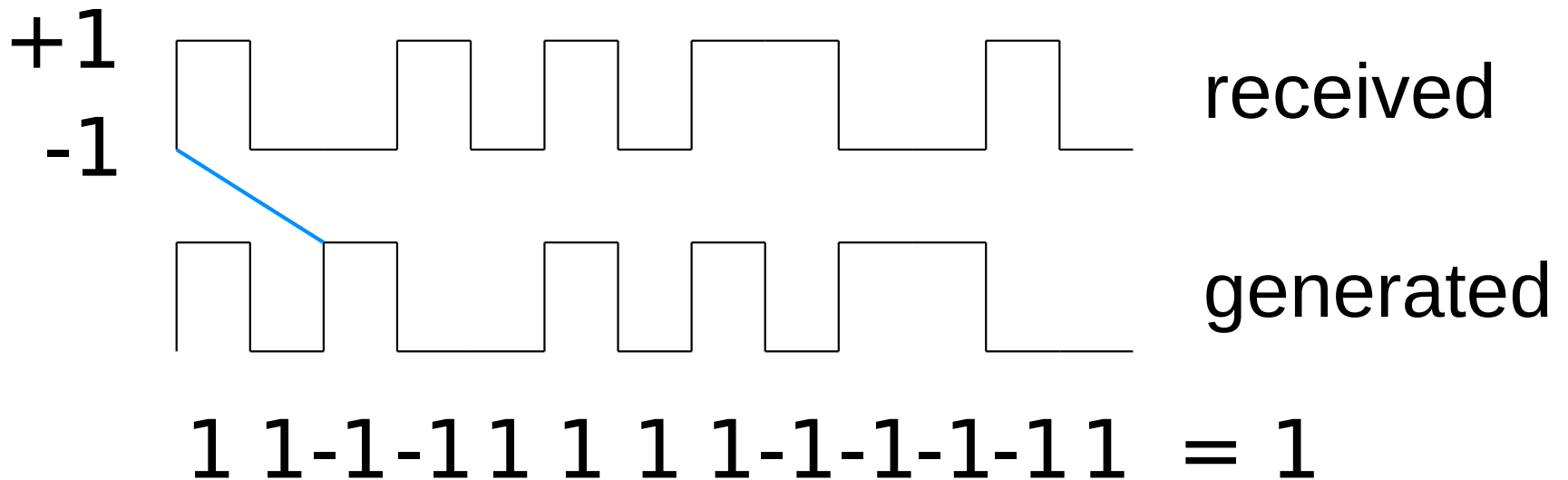
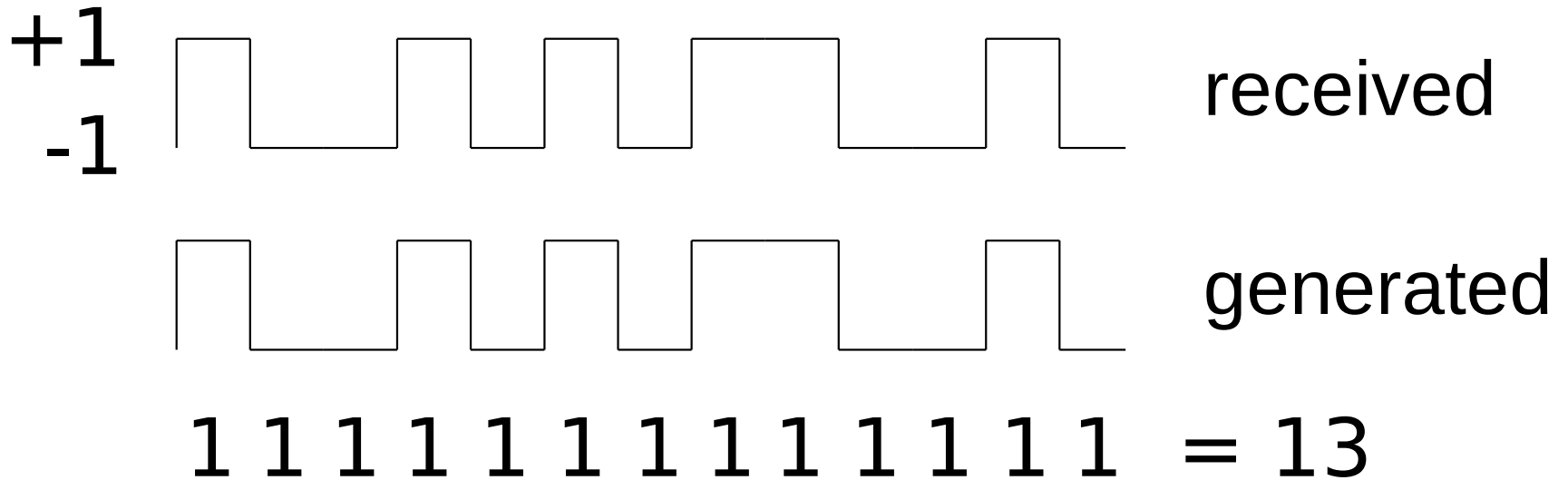
C/A code



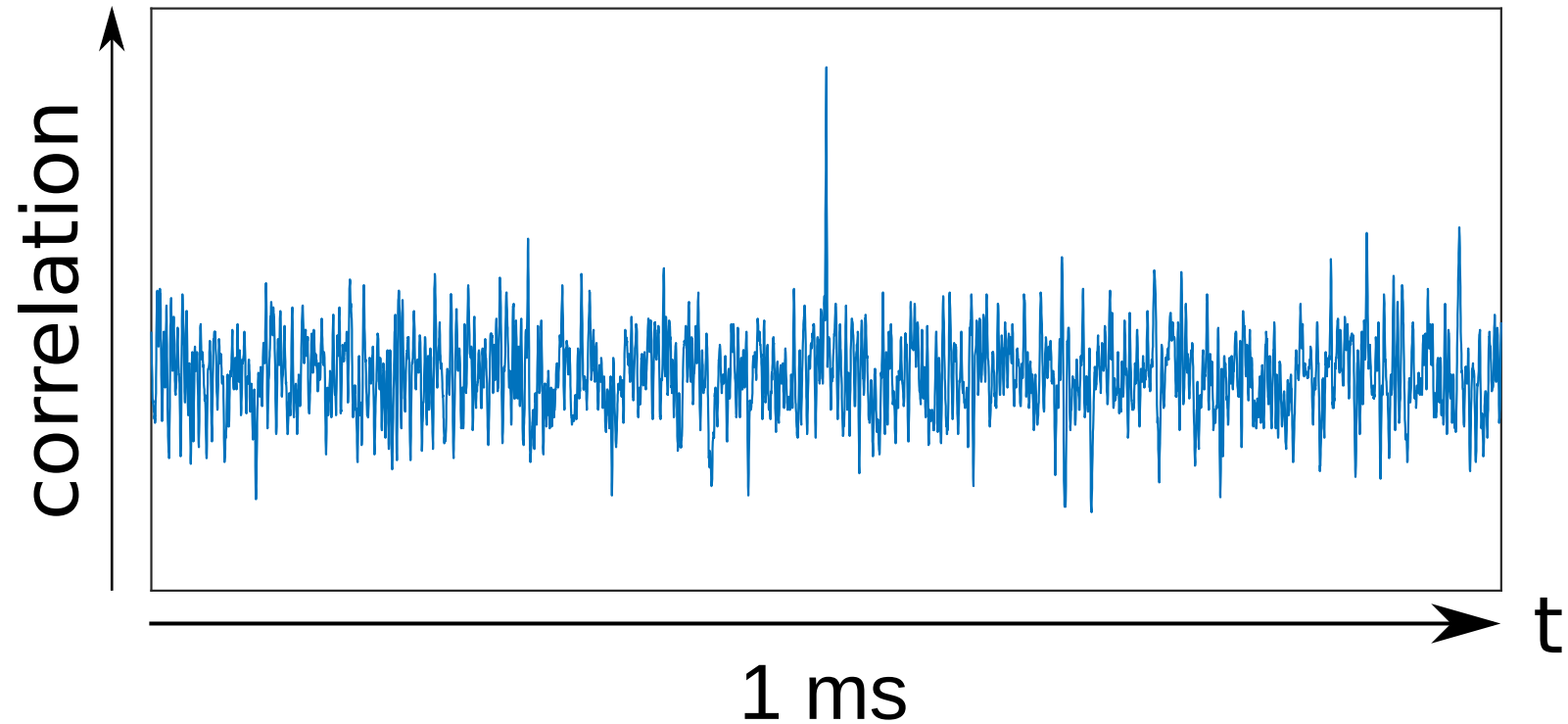
GPS signal



Correlation



Timing & Decoding

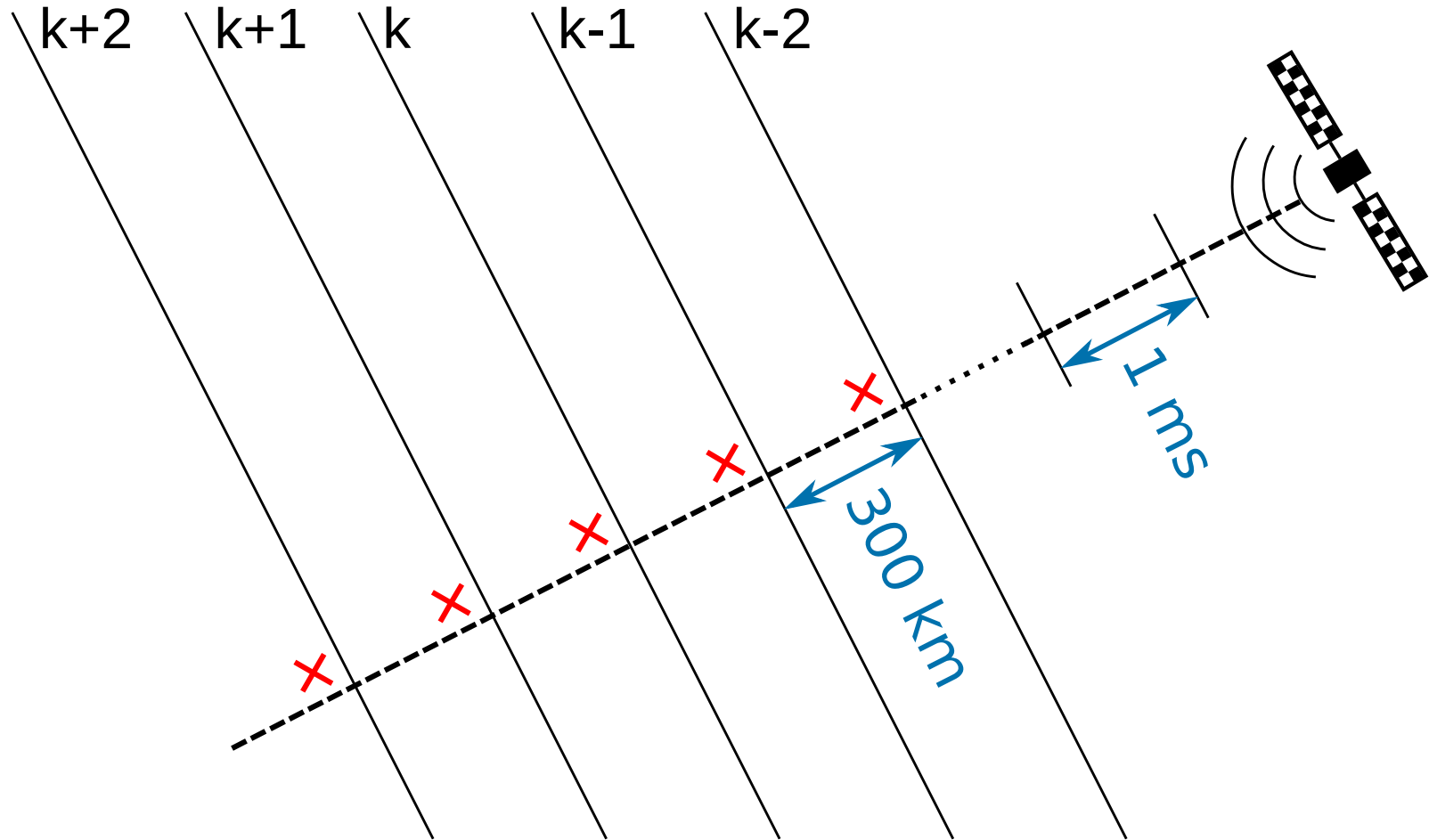


- 50 bps
- Time stamp sent every 6 seconds

Sub-ms time sync

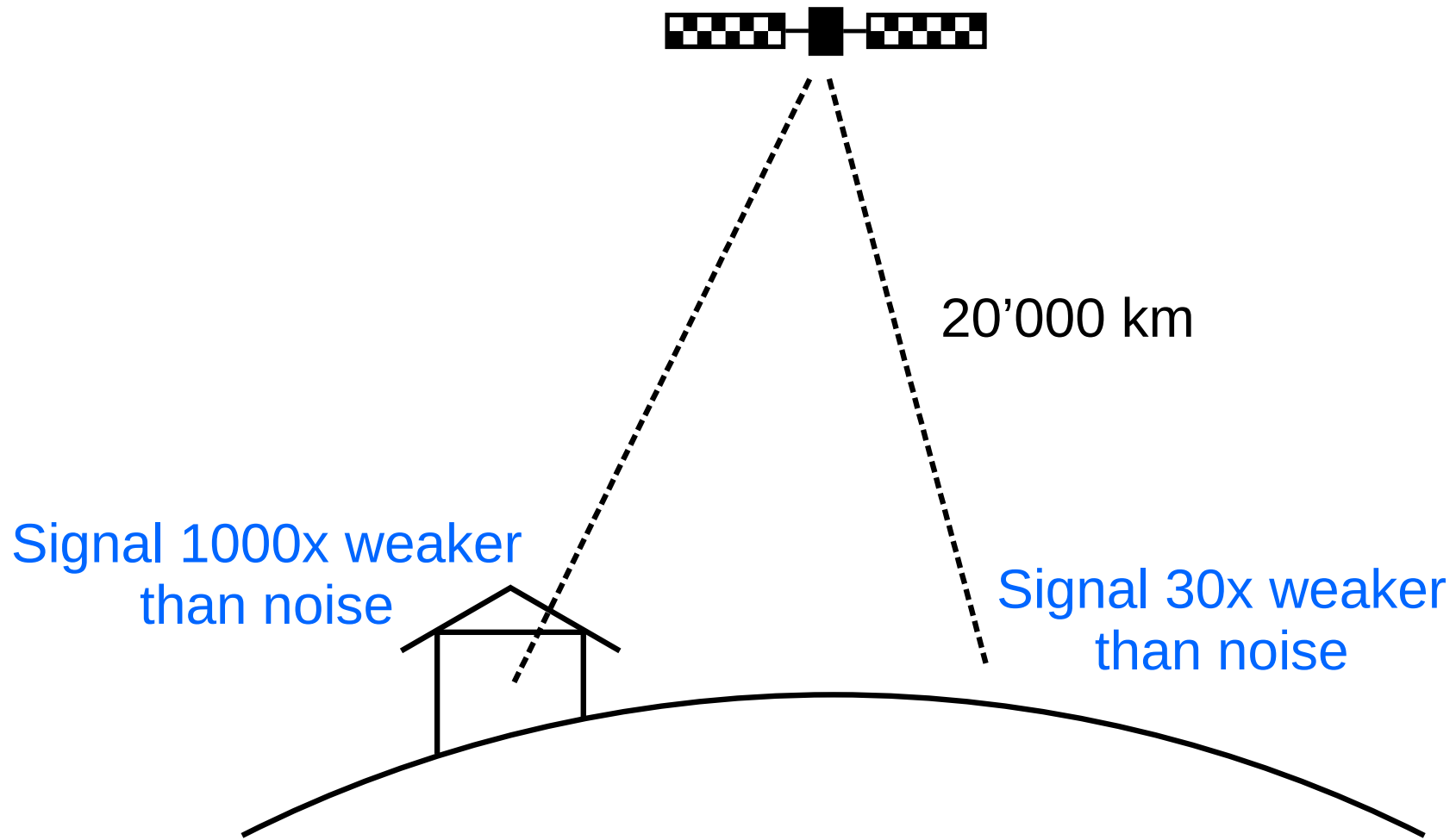
- We already have some time information
- $t_{\text{transmit}} = k * 1 \text{ ms}$

Coarse-Time Navigation (CTN)



- Known approximate position → whole ms time sync

Challenge II



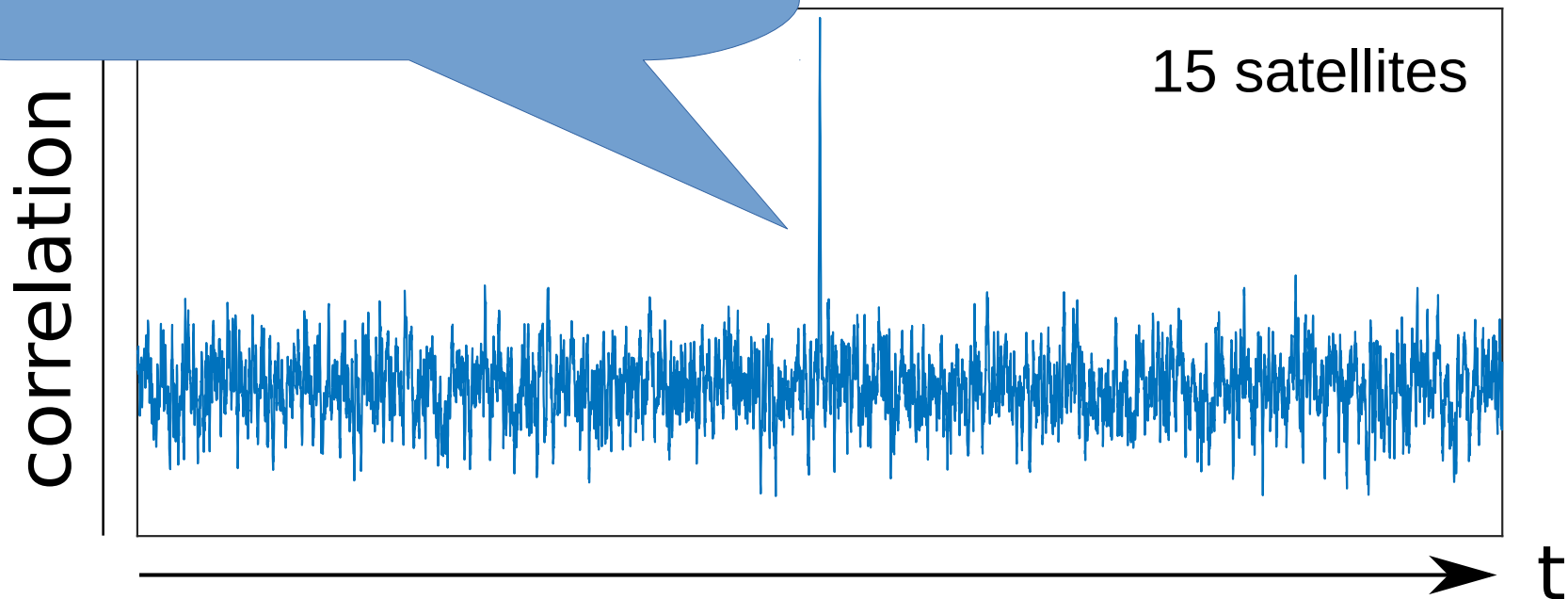
Noise



- 1 ms is iter

Sum over satellites

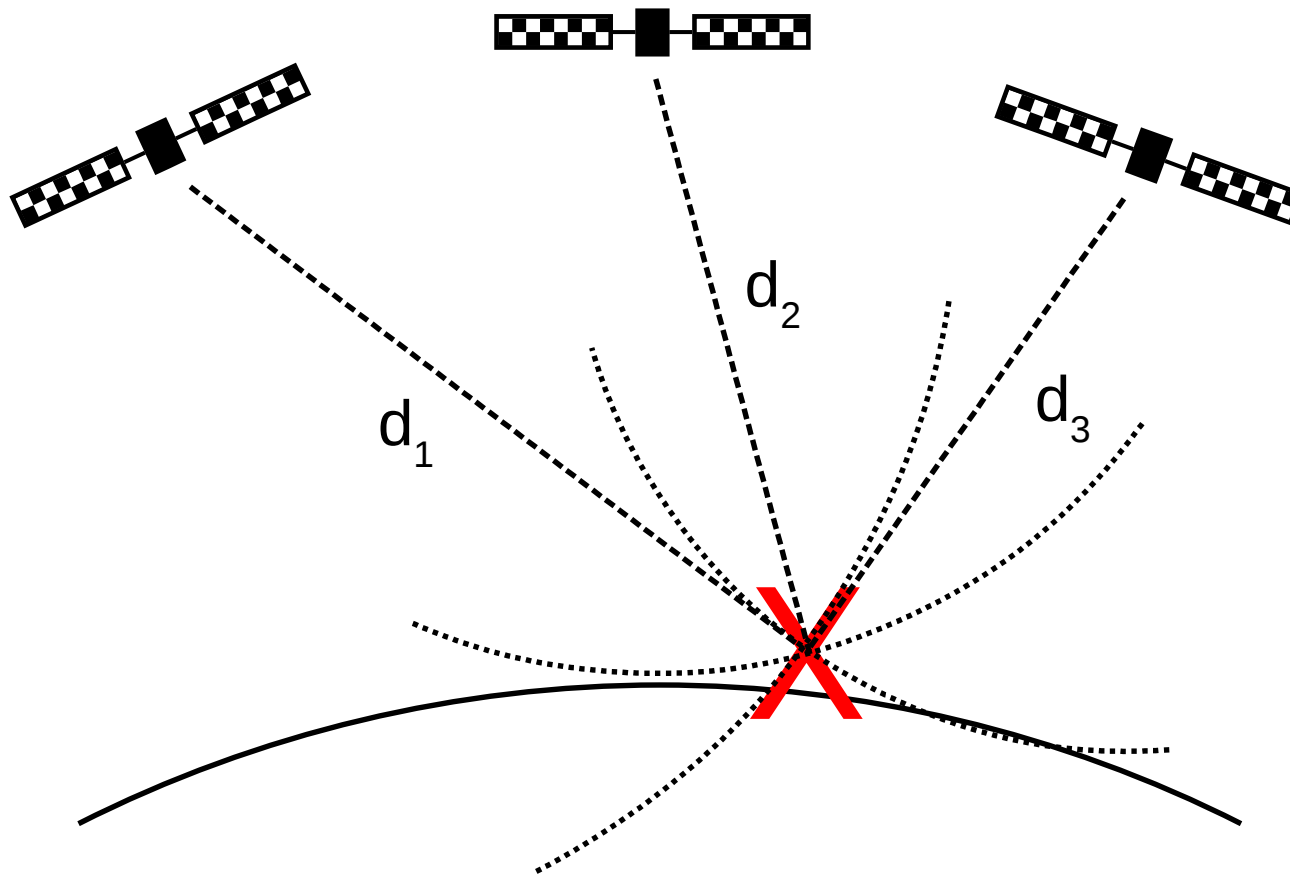
Signals from all satellites have to be aligned!



- Increased SNR

Hypotheses

- Receiver state (x, y, z, t)
- Satellite ranges known \rightarrow signal alignment known



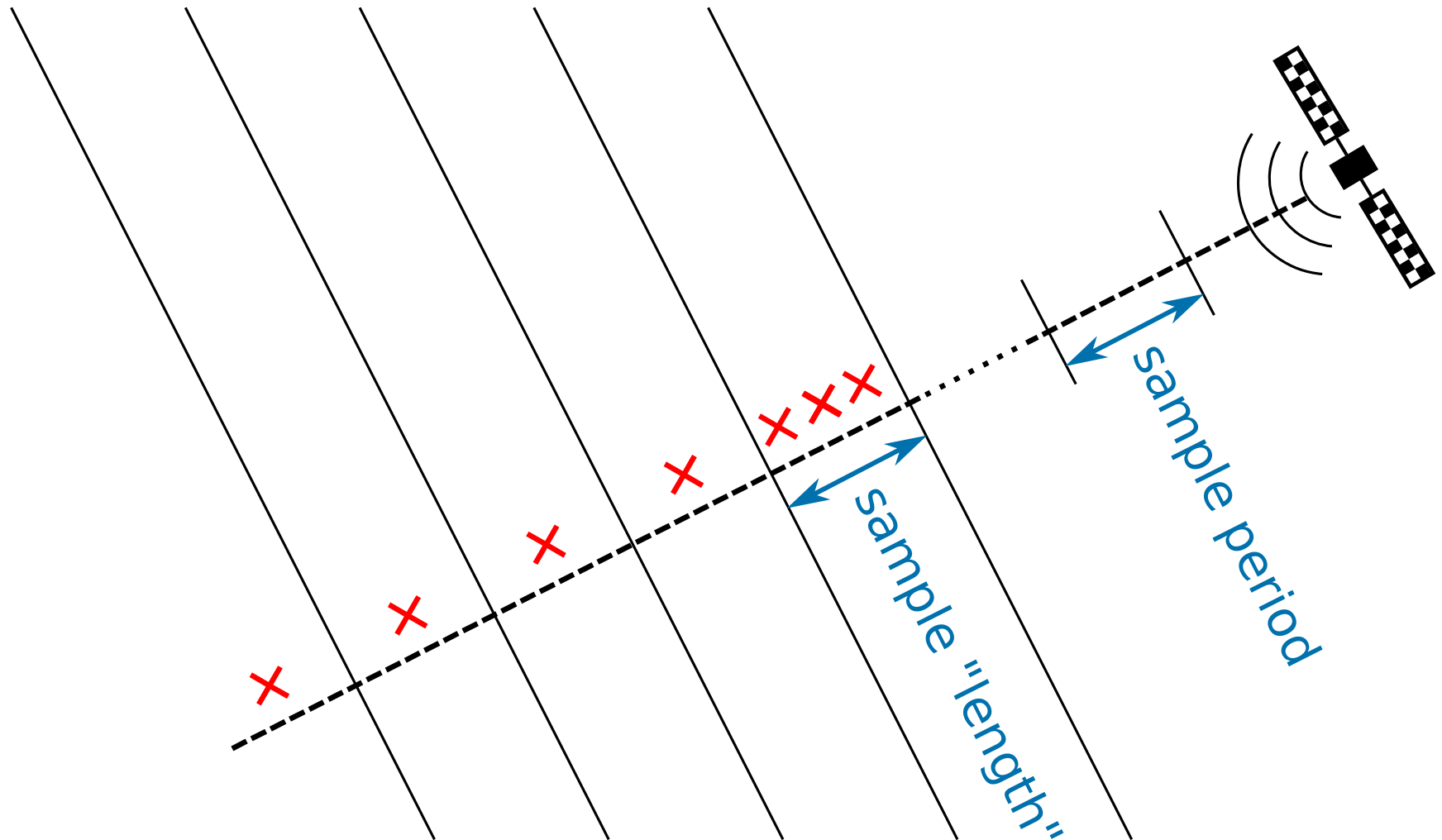
Best hypothesis?



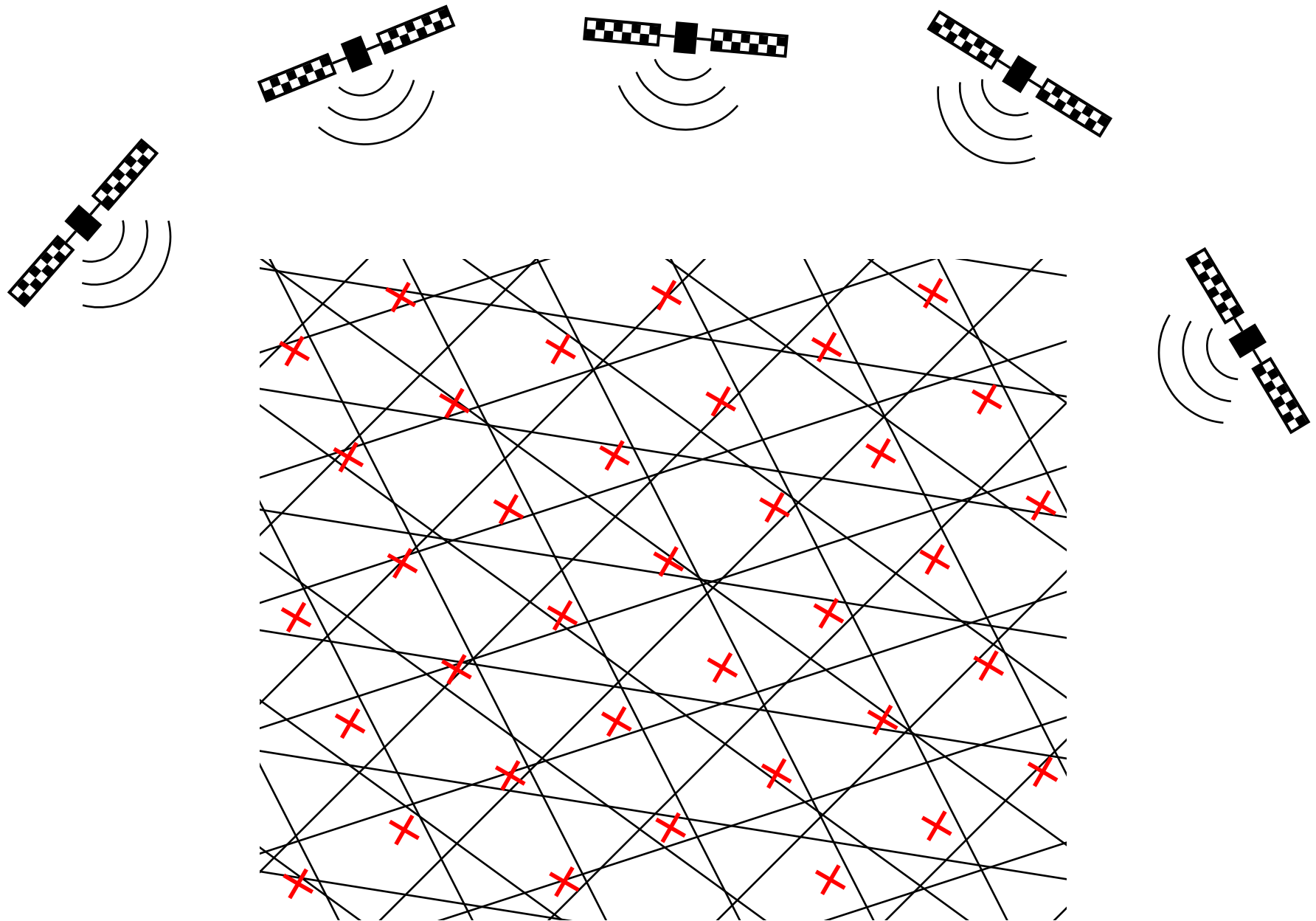
- M
- Number of hypotheses proportional to size of search space

Discretization of search space: 1D

- Discrete samples \rightarrow discrete positioning resolution

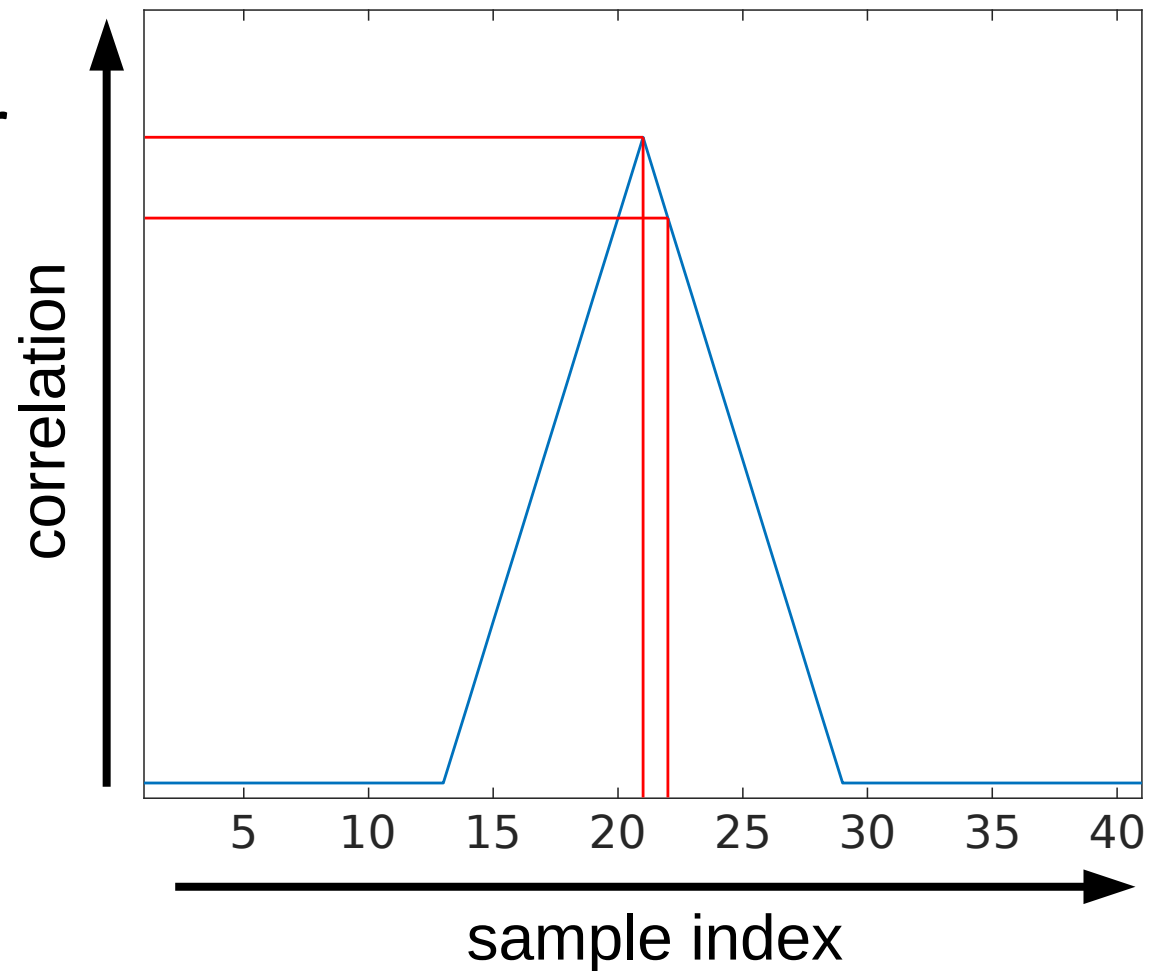


Discretization of search space: 2D



Off-by-one error

- Oversampling:
triangular peak
- 8 Msps \rightarrow $\sim 1/8$ lower
 \rightarrow - 0.6 dB
- Loss incurred only
for some satellites

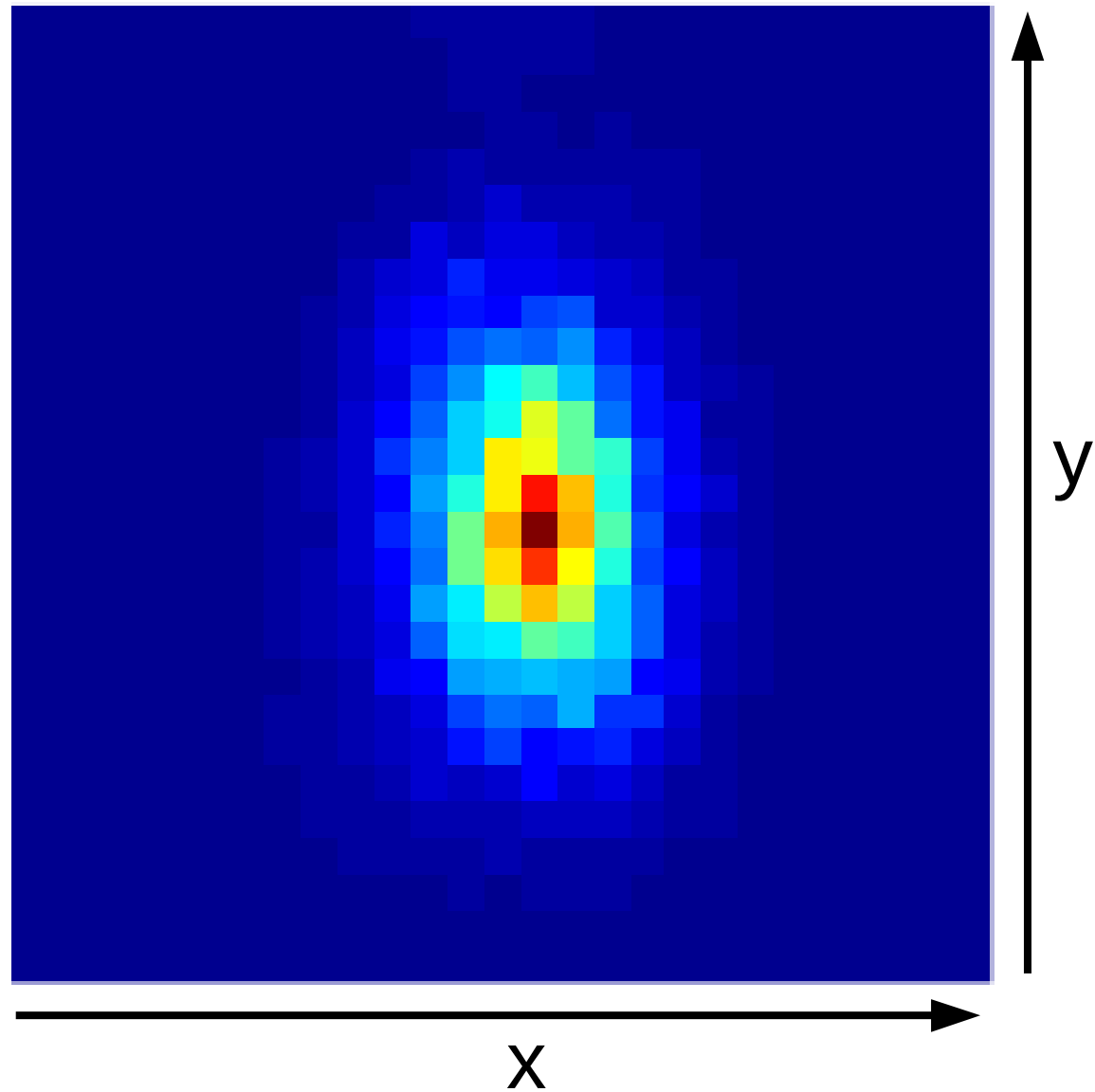


Challenge III

- 4D search
- Time offset → Satellite position error
- $10 \text{ km} * 10 \text{ km} * 1 \text{ km} * 1 \text{ min}, 8 \text{ Msps}$
→ 2.8 billion hypotheses

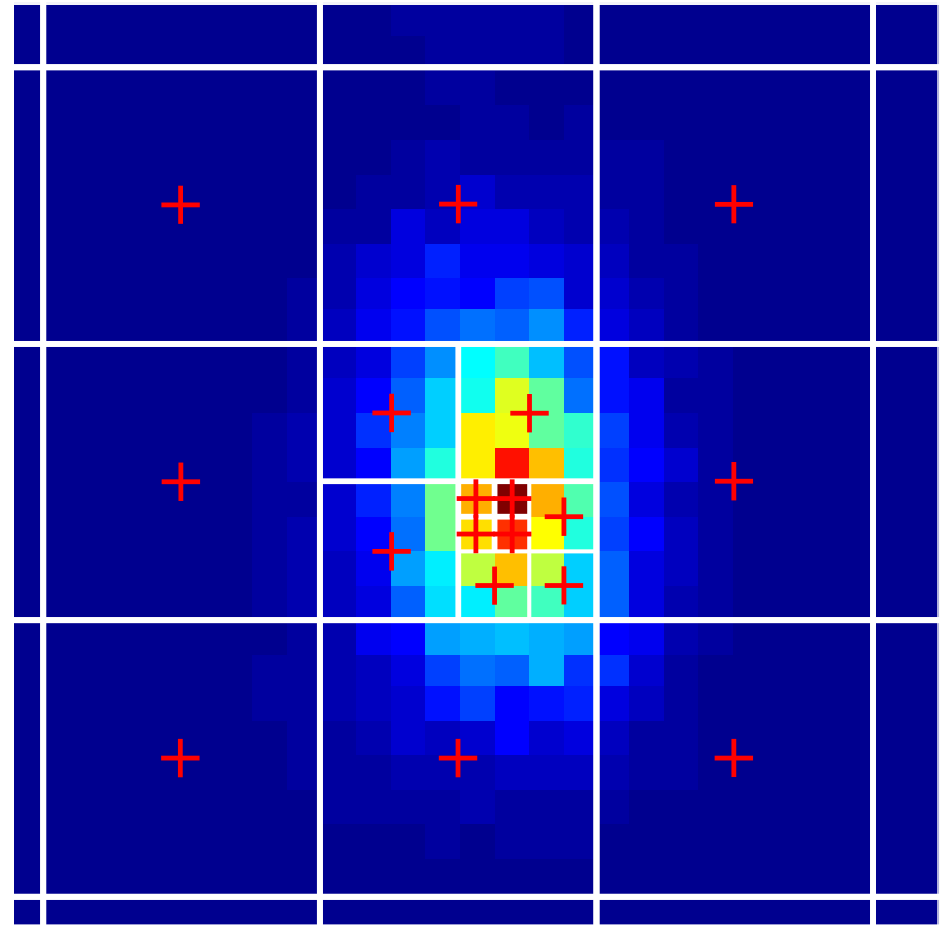
Exhaustive search

- Possible, but slow
- ~ 20 k evaluations / s
- Parallelizable



Branch and bound

- Explore promising regions first
- Discard “bad” regions
- Runtime: a few seconds (single thread, good SNR)

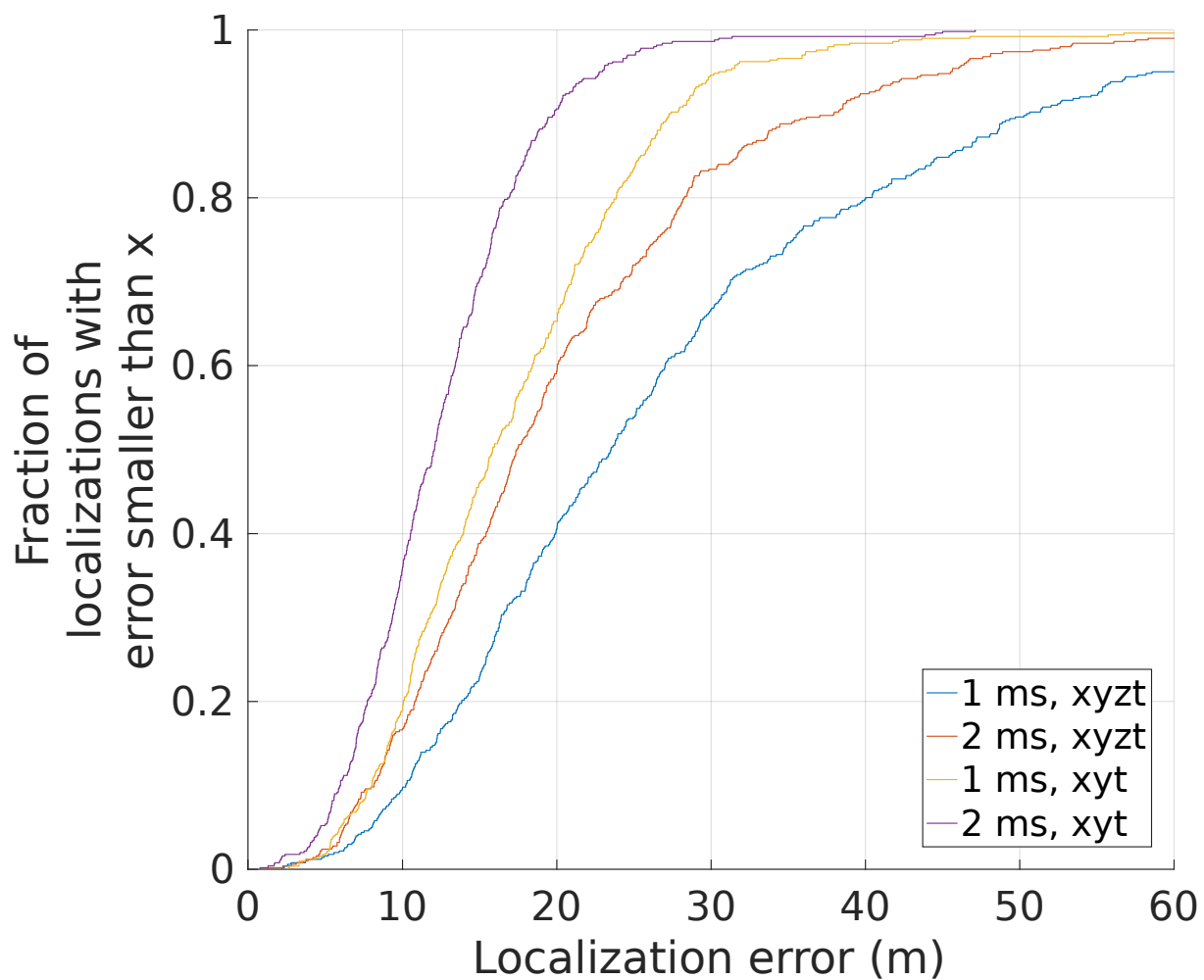


Related Work

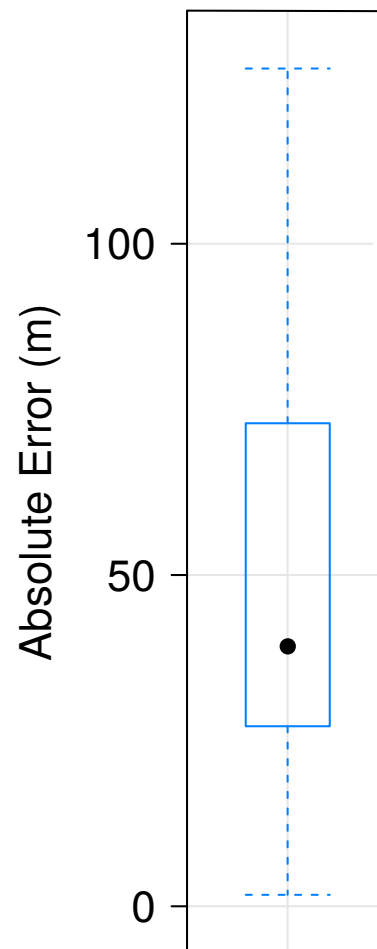
- Liu et al. “Energy Efficient GPS Sensing with Cloud Offloading” (SenSys’12, Best Paper)
 - CTN, suffer from noise
- Collective Detection
 - Various papers: 1) slow or 2) not optimal
 - Closas et al. “Maximum likelihood estimation of position in GNSS” (IEEE Signal Processing Letters, 2007)
 - Mathematical analysis of the superior robustness of “direct positioning”

Accuracy: 3D vs. 2D

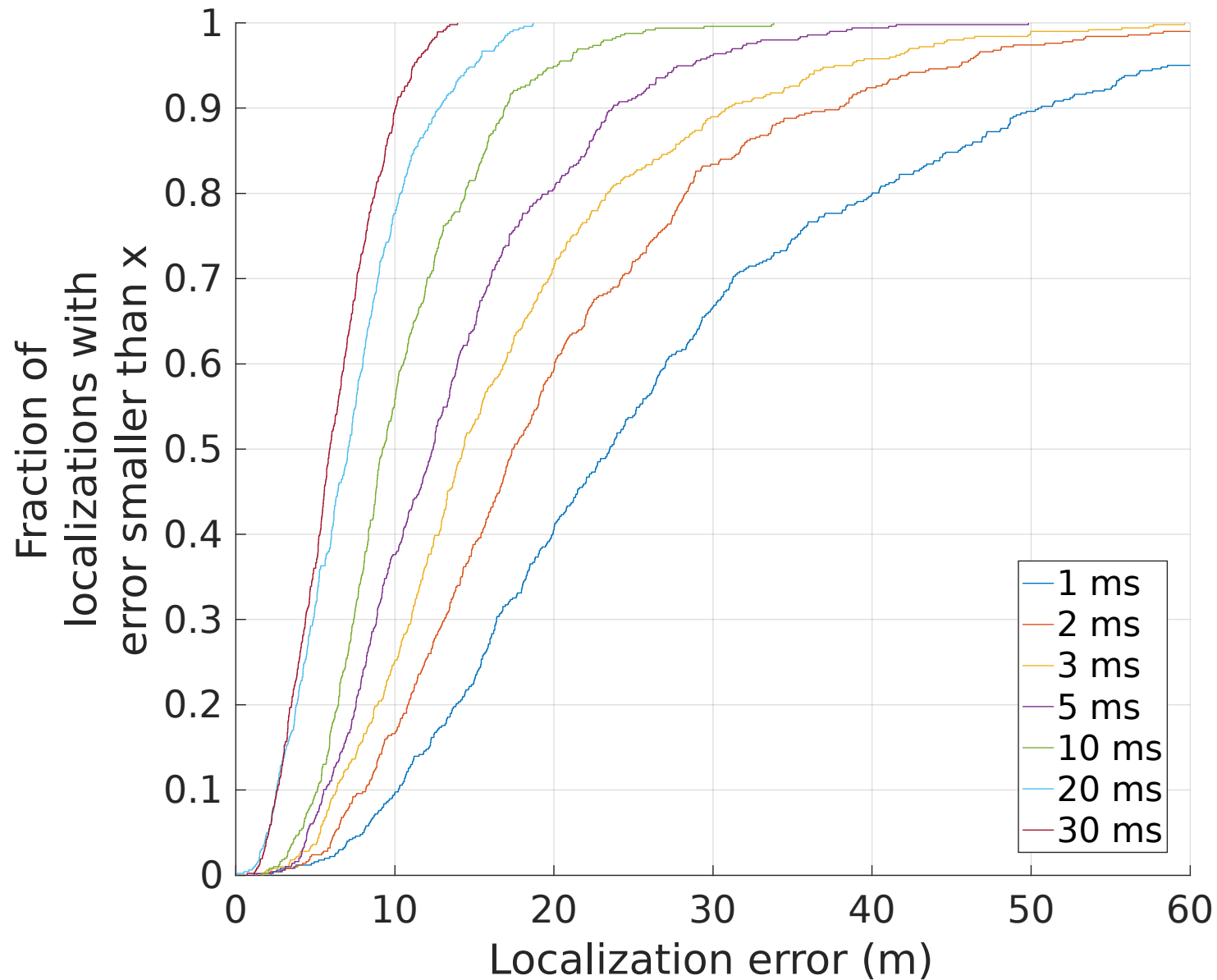
Our method



Liu et al. (2D, 2ms)



Accuracy: Average of k fixes

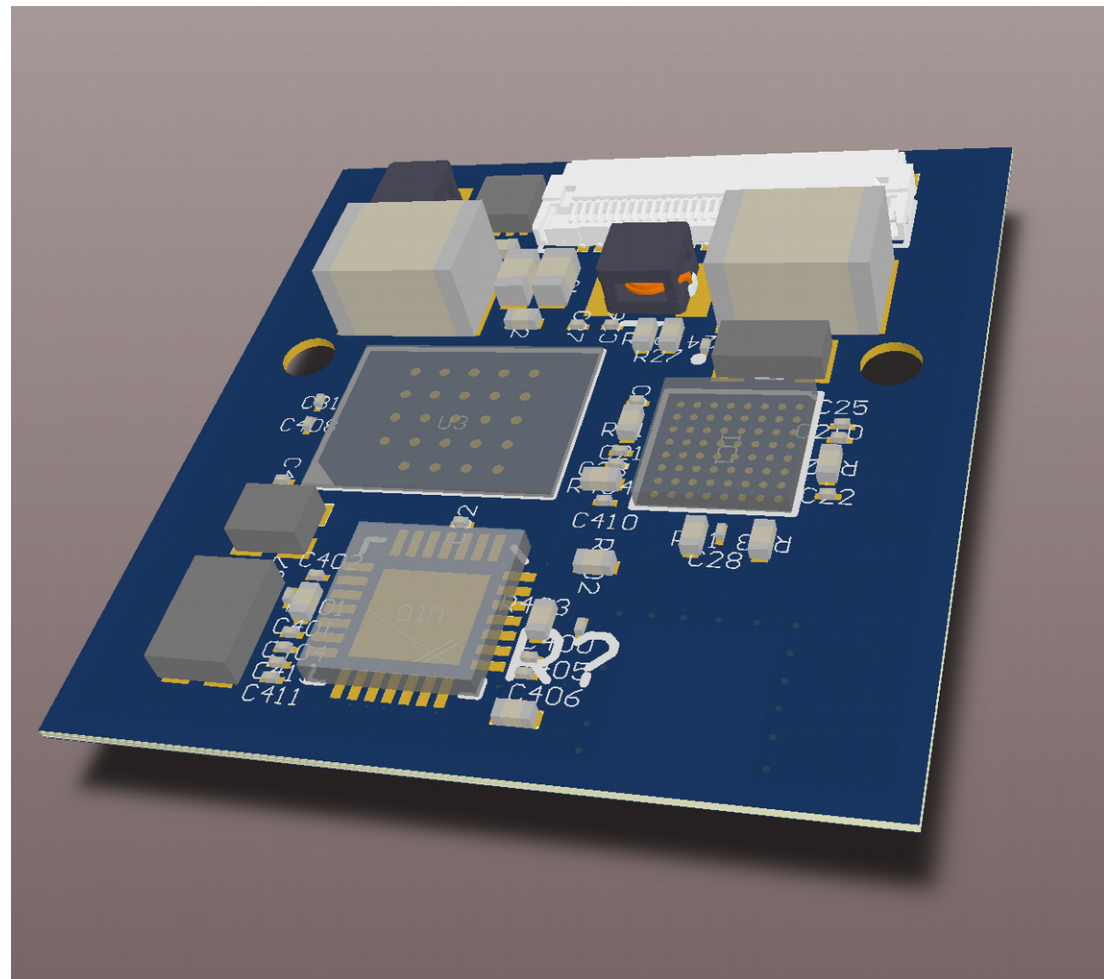


Tracking

- Branch-and-bound for initial fix
- First fix results in small search space
- Brute force subsequently

Sneak peek

- 23 x 19 mm
- Snapshot energy: 25 ms @ 100 mA = 2.5 mAs
- 140 mAh coin cell
- Energy for 3360 fixes



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